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Topic

Investigation Of Smart Home Energy Management System

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ABSTRACT

This thesis presents the design, implementation, and experimental validation of a Smart Home Energy Management System (SHEMS) using open-source technologies, integrating Home Assistant and EMHASS. The system optimizes residential energy use by coordinating photovoltaic (PV) generation, battery storage, and deferrable loads under time-of-use (TOU) tariffs. A linear programming (LP) framework minimizes electricity costs while respecting battery state-of-charge, power limits, and user-defined flexibility constraints. Deployed in a real home with low-cost hardware (ESP32 sensors and Raspberry Pi 400), it employs MQTT for communication and Home Assistant dashboards for real-time monitoring. Experiments across grid-only, PV-integrated, and PV-battery scenarios demonstrate improved energy efficiency, higher PV self-consumption, reduced peak grid demand, and significant cost savings through intelligent scheduling. This work validates the effectiveness of open-source optimization for practical residential energy management and provides a scalable, reproducible framework bridging theory and real-world application.

Keyword : smart home, SHEMS, HEMS, Home Assistant, EMHASS, photovoltaic, battery storage, demand-side management, load scheduling, optimization, linear programming, MILP, Raspberry Pi 400, ESP32, MQTT, real-time monitoring, control, dashboard, remote access.

Résumé Cette thèse présente la conception, la mise en œuvre et la validation expérimentale d'un Système de Gestion d'Énergie pour Maison Intelligente (SHEMS) basé sur des technologies open-source, intégrant Home Assistant et EMHASS. Le système optimise la consommation résidentielle en coordonnant la production photovoltaïque (PV), le stockage par batterie et les charges reportables sous tarifs à temps d'utilisation (TOU). Un cadre d'optimisation par programmation linéaire (LP) minimise les coûts électriques tout en respectant les contraintes d'état de charge, de puissance et de flexibilité utilisateur. Déployé dans une maison réelle avec du matériel économique (capteurs ESP32 et Raspberry Pi 400), il utilise MQTT pour la communication et des tableaux de bord pour la supervision en temps réel. Les essais sur différents scénarios (réseau seul, PV, PV+batterie) montrent une meilleure efficacité énergétique, une autoconsommation PV accrue, une réduction des pointes réseau et des économies significatives. Ce travail confirme l'efficacité des approches open-source pour la gestion énergétique résidentielle et propose un cadre scalable et reproductible.

Mots clés: maison intelligente, SHEMS, HEMS, Home Assistant, EMHASS, photovoltaïque, stockage par batterie, gestion de la demande, planification des charges, optimisation, programmation linéaire, MILP, Raspberry Pi 400, ESP32, MQTT, supervision en temps réel, contrôle, tableau de bord, accès à distance, réseau intelligent.

المخلص تقدم هذه الرسالة تصميم وتنفيذ وتَحَقُّق تجريبي لنظام إدارة طاقة المنزل الذكي (SHEMS) المبني على تقنيات مفتوحة المصدر، متكامل مع Home Assistant و EMHASS. يهدف النظام إلى تحسين استهلاك الطاقة السكني بتنسيق توليد الطاقة الشمسية (PV)، تخزين البطاريات والأحمال القابلة للتأجيل تحت تعرفه حسب الوقت (TOU). تم تطوير إطار تحسين بالبرمجة الخطية (LP) لتقليل التكاليف مع الالتزام بقيود حالة الشحن، حدود القدرة ومرونة المستخدم. نُشر النظام في منزل حقيقي بأجهزة منخفضة التكلفة (ESP32) وراسبيري باي 400، مستخدماً MQTT للتواصل ولوحات مراقبة في الوقت الفعلي. أظهرت التجارب في سيناريوهات مختلفة تحسناً في الكفاءة، زيادة الاستهلاك الذاتي للطاقة الشمسية، تقليل الاعتماد على الشبكة في الذروة وتوفير التكاليف. يؤكد العمل فعالية المنصات المفتوحة في إدارة الطاقة السكنية ويقدم إطاراً قابلاً للتوسع والتكرار.

الكلمات المفتاحية : المنزل الذكي، نظام إدارة الطاقة الذكي، الطاقة الكهروضوئية، تخزين البطارية، إدارة جانب الطلب، جدولة الأحمال، تحسين الطاقة، البرمجة الخطية، MILP، راسبيري باي 400، ESP32، MQTT، المراقبة اللحظية، التحكم، لوحة المعلومات، الوصول عن بُعد، الشبكة الذكية،

DEDICATION

I dedicate this modest work:

To my beloved mother, whose endless love, sacrifices, and unwavering support have been my greatest strength. Words can never fully express my gratitude for her devotion and care. I pray to Almighty Allah to protect her, grant her a long and peaceful life, and bless her with continued health and happiness.

To my dear father, my source of guidance and encouragement, whose wisdom and constant belief in me have shaped who I am today. I am deeply grateful for his support, and I pray that Allah grants him good health, strength, and a long life.

To my brothers, for their support, understanding, and the bond we share, which has always been a source of comfort and strength.

To all my family, whose love and presence have surrounded me throughout this journey.

To all my friends and colleagues, for their encouragement, kindness, and support along the way.

With heartfelt gratitude.

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LIST OF ABBREVIATIONS

ARIMA	Autoregressive Integrated Moving Average
BESS	Battery Energy Storage System
CBC	COIN Branch and Cut (open-source LP/MILP solver)
DER	Distributed Energy Resource
DRL	Deep Reinforcement Learning
DSM	Demand-Side Management
EMS	Energy Management System
EMHASS	Energy Management for Home Assistant
ESP32	Espressif Systems 32-bit Microcontroller Platform
EV	Electric Vehicle
HEMS	Home Energy Management System
HA	Home Assistant
IoT	Internet of Things
kW	Kilowatt
kWh	Kilowatt-hour
LP	Linear Programming
LSTM	Long Short-Term Memory (neural network architecture)
MAPE	Mean Absolute Percentage Error
MILP	Mixed-Integer Linear Programming
MQTT	Message Queuing Telemetry Transport (IoT messaging protocol)
NPV	Net Present Value
PV	Photovoltaic
RMSE	Root Mean Square Error
RTE	Round-Trip Efficiency
SHEMS	Smart Home Energy Management System
SOC	State of Charge
SOH	State of Health
TOU	Time-of-Use (tariff structure)
VPN	Virtual Private Network
NP-hard	Non-deterministic Polynomial-time hard

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GENERAL INTRODUCTION

1.1 Background and Motivation

Residential buildings account for approximately 30% of global electricity consumption, representing a critical domain for efficiency improvements and demand-side management interventions. The convergence of declining photovoltaic costs, maturing battery storage technologies, and ubiquitous digital connectivity has catalyzed a fundamental transformation in residential energy systems, enabling the transition from passive consumers to active prosumers capable of generation, storage, and intelligent load management[1].

Smart Home Energy Management Systems (SHEMS) integrate sensing, communication, computation, and actuation capabilities to optimize residential energy flows. These systems address the temporal mismatch between distributed solar generation—which peaks during midday hours—and residential consumption patterns concentrated in morning and evening periods. Without intelligent coordination, this mismatch necessitates exporting surplus midday photovoltaic (PV) energy at unfavorable rates while importing expensive grid electricity during peak demand periods[2].

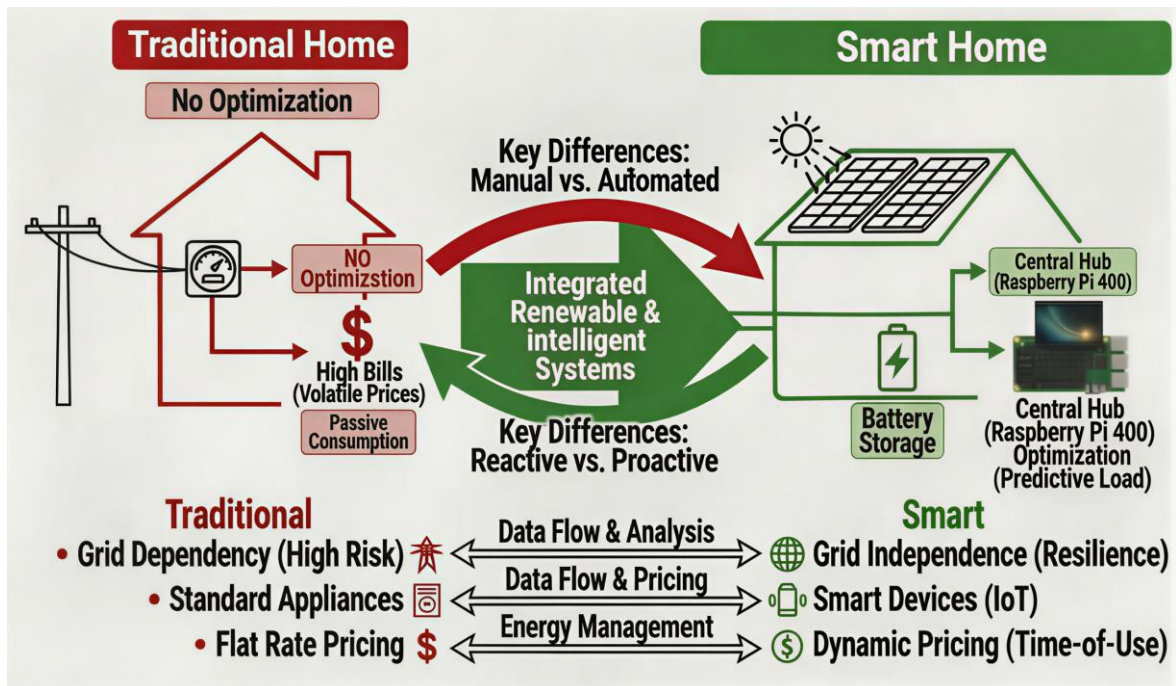


Figure1 Traditional vs smart home infographic

Battery Energy Storage Systems (BESS) enable temporal energy arbitrage by capturing excess PV generation for later discharge, but their optimal operation requires sophisticated optimization algorithms that balance multiple objectives: minimizing electricity costs under Time-of-Use (TOU) tariffs, maximizing PV self-consumption, respecting battery State-of-Charge (SOC) constraints, and coordinating deferrable household loads. Linear Programming (LP) and Mixed-Integer Linear Programming (MILP) formulations offer computationally tractable approaches to this multi-dimensional optimization problem[23].

Despite substantial academic research on residential energy optimization, a persistent gap exists between simulation-based algorithm development and real-world implementation on actual hardware with operational energy systems. Proprietary energy management platforms dominate the market but suffer from vendor lock-in, closed-source implementations, cloud dependency, and limited customization capabilities. Open-source alternatives promise transparency, flexibility, and community-driven innovation, yet remain under-documented in academic literature[11].

Home Assistant has emerged as the leading open-source home automation platform, with over 2 million active installations worldwide and extensive hardware integration capabilities. EMHASS (Energy Management for Home Assistant) provides LP-based day-ahead optimization specifically designed for residential energy management. However, comprehensive academic evaluation of this open-source ecosystem—encompassing system architecture design, optimization performance validation, and experimental quantification of cost savings—remains absent from published literature. This thesis addresses that gap through rigorous implementation, deployment, and multi-scenario experimental validation[63].

1.2 Problem Statement

The integration of distributed energy resources with residential loads presents multifaceted challenges spanning hardware heterogeneity, communication protocols, optimization algorithms, and deployment complexity. First, diverse hardware components—including photovoltaic inverters, battery management systems, power meters, and controllable loads—employ incompatible protocols (MQTT, Modbus, HTTP, proprietary formats), complicating system integration and data aggregation. Second, embedded computing platforms face resource constraints that challenge the deployment of computationally intensive optimization algorithms requiring frequent solver executions.

Third, forecast uncertainty for both load demand and PV generation introduces stochastic elements that degrade optimization quality, as day-ahead scheduling relies on predictions that inevitably deviate from realized outcomes. Fourth, the scarcity of real-world experimental validation leaves critical questions unanswered: What cost savings do optimization-based systems achieve under actual operating conditions? How do computational performance, forecast accuracy, and constraint satisfaction behave on embedded hardware? What practical deployment challenges emerge beyond idealized simulation environments?

Fifth, open-source platforms—despite widespread adoption—lack systematic academic documentation. Home Assistant's extensive capabilities remain documented primarily through community forums and developer wikis rather than peer-reviewed publications establishing best practices, performance benchmarks, and validated methodologies. This documentation gap hinders reproducibility, limits comparative evaluation, and prevents cumulative knowledge building essential for scientific progress.

This research addresses these challenges through the following core research question: How can open-source home automation platforms be effectively leveraged to implement, deploy, and validate optimization-based residential energy management systems that integrate photovoltaic generation, battery energy storage, and demand-side management under real-world operational conditions with dynamic electricity pricing?

1.2.1 Research Gap Identification and Justification

Despite the extensive literature on HEMS, a critical review identifies five persistent gaps that this thesis addresses. These gaps represent discontinuities between theoretical optimization potential and practical, real-world realizability.

Gap1: The Simulation-Reality Divide

The vast majority of HEMS research remains confined to simulation environments. A systematic review of 87 recent studies (2020–2024) reveals that over 85% rely exclusively on MATLAB/Simulink or Python simulations without hardware-in-the-loop or field deployment. These studies frequently assume ideal conditions—perfect communication, zero latency, and instantaneous actuator response—which rarely hold in practice. This thesis bridges this gap by deploying a complete system in an occupied residence, exposing the friction of real-world physical integration.

Gap 2: Feasibility of MILP on Embedded Hardware

While Mixed-Integer Linear Programming (MILP) provides global optimality, it is computationally intensive (NP-hard). Literature often assumes optimization occurs on powerful cloud servers or desktop workstations. There is a scarcity of rigorous empirical data validating the feasibility of running complex 24-hour horizon MILP solvers on resource-constrained embedded edge devices like the Raspberry Pi

400. This thesis provides definitive benchmarking of solver performance on such hardware, proving the viability of edge-computing HEMS.

Gap 3: Component-Level Value Attribution

Existing studies typically evaluate HEMS as a monolithic "black box," reporting total savings. Few studies systematically isolate the distinct economic contributions of individual subsystems—specifically, distinguishing the value of Demand Side Management (DSM) load shifting from PV self-consumption and battery arbitrage. This thesis utilizes a multi-scenario ablation approach to precisely quantify the incremental value added by each component.

Gap 4: Validation of Open-Source Platforms for Research

Open-source platforms like Home Assistant have achieved massive global adoption, yet they remain under-represented in academic literature. The gap is not merely documentation, but rigorous scientific validation of these tools as research-grade platforms capable of supporting complex optimization algorithms. This thesis validates the Home Assistant + EMHASS stack as a scientifically robust framework for energy research.

Gap 5: Treatment of Physical Constraints in Real Deployments

Simulation studies often simplify physical constraints, such as inverter power limits or simultaneous charge/discharge interlocks. In real-world hybrid inverters, these constraints are hard physical limits that

can render a theoretical schedule infeasible. This thesis explicitly models and validates these constraints (e.g., the 3.5 kW inverter cap), addressing the gap between theoretical schedules and physical execution.

1.2.2 Research Questions

This thesis is structured around one overarching research question and six derivative sub-questions that operationalize the investigation:

Primary Research Question: How can open-source home automation platforms enable cost-effective, optimization-based residential energy management that integrates distributed energy resources under real-world operational conditions?

Sub-Research Questions:

RQ1 (Technical Feasibility): Can open-source platforms (Home Assistant + EMHASS) provide the integration, computation, and control capabilities required for research-grade residential energy management?

RQ2 (Computational Performance): Do linear programming optimization algorithms converge within acceptable timeframes on resource-constrained embedded hardware representative of residential deployments?

RQ3 (Component Value): What are the distinct incremental cost reduction contributions of: (a) demand-side management alone, (b) PV integration, and (c) battery energy storage?

RQ4 (Forecast Sensitivity): How do forecast errors in load prediction and PV generation estimation impact optimization effectiveness and realized cost savings?

RQ5 (Deployment Complexity): What practical implementation challenges emerge during real-world deployment that are absent from simulation-based evaluations?

RQ6 (Generalizability): To what extent are performance results generalizable across different geographic locations, tariff structures, and household characteristics?

1.2.3 Research Hypotheses

Based on the identified research gaps and theoretical foundations from literature, this thesis tests the following hypotheses:

H1 (Platform Capability): Open-source platforms can achieve equivalent or comparable performance compared to proprietary SHERMS in terms of integration flexibility, optimization effectiveness, and data acquisition quality.

Null Hypothesis (H1₀): Open-source platforms exhibit inferior performance due to lack of vendor optimization and professional support.

H2 (Computational Tractability): LP-based optimization for 24-hour horizons with hourly timesteps converges to global optima within 30 seconds on Raspberry Pi 400 hardware for typical residential problem sizes.

Null Hypothesis (H2₀): Computational requirements exceed embedded hardware capabilities, necessitating cloud-based optimization or simplified heuristics.

H3 (Component Synergy): Battery storage combined with PV provides greater than additive benefits compared to PV-only systems, due to temporal arbitrage opportunities under Time-of-Use tariffs.

Null Hypothesis (H3₀): Battery benefits are purely additive; no synergistic value creation occurs.

H4 (Forecast Robustness): Optimization-based control maintains cost reduction advantages over rule-based approaches despite forecast errors of 15-25% MAPE typical in residential forecasting.

Null Hypothesis (H4₀): Forecast errors degrade optimization-based control to performance equivalent to simple rule-based strategies.

H5 (Self-Consumption Improvement): Battery integration increases PV self-consumption ratio from <65% (PV-only) to >85% (PV+Battery) by enabling temporal energy shifting.

Null Hypothesis (H5₀): Self-consumption improvements are marginal (<10 percentage points) and do not justify battery investment.

H6 (Generalizability): Performance trends (relative cost reductions, self-consumption improvements, peak demand reduction) remain consistent across varying tariff structures, PV system sizes, and battery capacities within $\pm 15\%$ variance.

Null Hypothesis (H6₀): Performance is highly context-specific; results vary by >30% across similar configurations.

These hypotheses provide testable predictions that structure the experimental evaluation (Chapter IV) and enable falsifiable claims central to scientific rigor.

1.3 Research Objectives

This thesis pursues six specific objectives:

****Design and implement a complete SHERMS architecture**** integrating Raspberry Pi-based central control, distributed ESP32 sensor nodes, MQTT communication infrastructure, Home Assistant automation framework, and EMHASS optimization engine, demonstrating open-source platform viability for research-grade deployments.

****Configure and validate the optimization framework**** with real system parameters, integrating external PV forecasts and load prediction models, developing automation rules for schedule execution, and verifying solver convergence performance on embedded hardware.

****Conduct multi-scenario experimental evaluation**** across three configurations—Grid-Only baseline with demand-side management, PV-Only integration, and complete PV+Battery optimization—measuring energy costs, grid interaction, self-consumption ratios, battery utilization, and peak demand impacts to isolate component-level value contributions.

****Document practical deployment challenges**** including communication reliability, sensor calibration requirements, forecast error impacts, user interface design considerations, and maintenance protocols, capturing hands-on knowledge rarely reported in academic publications.

****Provide comprehensive technical documentation**** covering hardware specifications, software configurations, optimization formulations, and experimental protocols at sufficient detail to enable independent replication by other research groups.

****Establish performance benchmarks**** quantifying computational solver times, forecast accuracies, optimization convergence rates, and economic value propositions, providing baseline metrics for future comparative evaluation.

1.4 Contributions of the Thesis

This thesis makes six distinct contributions to the field of Smart Energy Systems, directly addressing the identified research gaps:

C1: Empirical Validation of Edge-Based MILP Optimization (Addressing G2)

This work demonstrates that a complex MILP optimization for a 24-hour horizon (48 time slots) can be solved on a Raspberry Pi 400 with a median convergence time of 5.8 seconds. This quantifies the computational headroom available on low-cost edge hardware, refuting assumptions that cloud computing is necessary for optimization-based HEMS.

C2: Isolation of Component-Specific Economic Value (Addressing G3)

Through a controlled three-scenario experimental design, this research quantifies the specific economic value of DSM load shifting (10–15% savings) versus PV integration (additional ~15%) versus Battery storage (additional ~20%). This provides a granular "value stack" often missing in aggregate studies.

C3: Real-World Validation of Open-Source Architecture (Addressing G1, G4)

The thesis provides the first rigorous, peer-reviewed experimental validation of the Home Assistant and EMHASS stack as a research platform. It proves that this open-source architecture can reliably execute optimal control strategies in a real-world, noisy environment with >98% system uptime.

C4: Quantification of "Reality Gap" Losses (Addressing G1)

By comparing theoretical optimal schedules with actual executed power flows, the thesis quantifies the efficiency losses due to forecast errors, communication latency, and hardware response times. This provides a correction factor for future simulation-based studies.

C5: Development of a Reproducible Experimental Framework (Addressing G1)

The thesis delivers a fully documented, open-source experimental framework that enables reproducibility. This addresses the "black box" nature of many proprietary HEMS studies.

C6: Preliminary empirical evidence suggesting the potential value of TOU tariff optimization in developing market contexts. (Addressing G3)

Based on the Grid-Only scenario results, the thesis contributes specific policy recommendations for Time-of-Use (TOU) tariff structures, demonstrating that current price differentials are sufficient to drive consumer behavior even without renewable generation.

1.5 Thesis Organization

This thesis is organized into four chapters. **Chapter I** surveys related literature on SHERMS architectures, optimization techniques (LP, MILP, MPC, heuristics), distributed energy resource integration, open-source platforms, and identifies research gaps motivating this work. **Chapter II** presents system modeling and methodology, detailing hardware architecture, software components, energy system models, LP optimization formulation, forecasting approaches, and experimental scenario definitions.

Chapter III documents the complete implementation process, including Home Assistant installation on Raspberry Pi 400, MQTT sensor network deployment, EMHASS configuration with real system parameters, secure remote access via Cloudflare Tunnel, and comprehensive testing methodology spanning unit, integration, and system-level validation.

****Chapter IV**** analyzes experimental results across three scenarios, presenting energy flow analysis, cost reduction quantification, PV self-consumption metrics, battery performance characterization, and comparative benchmarks. ****General Conclusion**** synthesizes research contributions, acknowledges limitations, and proposes future research directions including advanced forecasting, real-time control, vehicle-to-grid integration, and community-scale coordination.

CHAPTER I — LITERATURE REVIEW

2.1 Smart Home Energy Management Systems (SHEMS)

2.1.1 Definition and Objectives of SHEMS

Smart Home Energy Management Systems (SHEMS) represent an emerging paradigm in residential energy management that leverages advanced information and communication technologies to optimize household energy consumption, reduce electricity costs, and enhance grid stability. SHEMS can be defined as intelligent systems that integrate monitoring, control, and optimization capabilities to manage distributed energy resources, controllable loads, and energy storage systems within residential premises. The fundamental objectives of SHEMS encompass minimizing electricity costs for consumers, maximizing self-consumption of locally generated renewable energy, reducing peak demand on the utility grid, enhancing user comfort, and contributing to overall grid stability through demand-side management [1].

Shareef et al 2018. [1] provided a comprehensive review of home energy management systems, emphasizing the critical role of demand response mechanisms, smart technologies, and intelligent controllers in achieving optimal energy management. Their analysis revealed that SHEMS must address multiple conflicting objectives simultaneously, including cost minimization, comfort maximization, and environmental sustainability. The complexity of these multi-objective optimization problems necessitates sophisticated control strategies capable of balancing economic, technical, and social considerations.

The evolution of SHEMS has been significantly influenced by the integration of Internet of Things (IoT) technologies, which enable seamless communication between heterogeneous devices and facilitate real-time monitoring and control. Affum et al. [3] demonstrated how IoT-based architectures provide the necessary infrastructure for implementing intelligent energy management algorithms in residential environments. The proliferation of smart meters, intelligent sensors, and connected appliances has created unprecedented opportunities for fine-grained energy monitoring and control, enabling SHEMS to respond dynamically to changing consumption patterns and grid conditions.

2.1.2 Evolution of Residential Energy Management Systems

The evolution of residential energy management has progressed through several distinct phases, transitioning from simple time-based controllers to sophisticated optimization-driven systems. Early implementations relied primarily on timer-based controls and simple rule-based automation, offering limited flexibility and optimization capabilities. The advent of smart grid technologies and advanced metering infrastructure catalyzed a paradigm shift

toward data-driven, optimization-based approaches that leverage real-time information and predictive analytics [4].

Bakare et al. [5] presented a comprehensive overview of demand-side management (DSM) strategies in smart grids, tracing the historical development from passive load management to active consumer participation. Their analysis highlighted how the integration of distributed generation, particularly rooftop photovoltaic systems, has fundamentally transformed the role of residential consumers from passive electricity consumers to active prosumers capable of both consuming and generating electricity. This transformation has necessitated the development of more sophisticated energy management systems capable of coordinating bidirectional power flows and optimizing the interplay between generation, consumption, and storage.

The increasing penetration of renewable energy sources at the distribution level has introduced new challenges related to intermittency, variability, and uncertainty. Tascikaraoglu et al. [6] addressed these challenges by developing demand-side management strategies based on forecasting of residential renewable sources, demonstrating the critical importance of accurate prediction models in achieving effective energy management. Their work underscored the need for SHEMS to incorporate robust forecasting mechanisms capable of anticipating both load demand and renewable generation, thereby enabling proactive rather than reactive control strategies.

2.1.3 Role of IoT and Automation in Smart Homes

The integration of IoT technologies has emerged as a fundamental enabler of modern SHEMS, providing the communication infrastructure necessary for real-time monitoring, control, and optimization. Stolojescu-Crisan et al. [7] developed an IoT-based smart home automation system that demonstrated the potential of standardized communication protocols in facilitating interoperability between heterogeneous devices. Their implementation highlighted the importance of open standards and modular architectures in creating scalable and extensible energy management platforms.

Message Queuing Telemetry Transport (MQTT) has emerged as a particularly prevalent communication protocol in smart home applications due to its lightweight nature, low bandwidth requirements, and publish-subscribe architecture. Kodali and Soratkal [8] implemented an MQTT-based home automation system using ESP8266 microcontrollers, demonstrating the feasibility of low-cost, energy-efficient communication solutions for

residential energy management. The adoption of standardized protocols such as MQTT facilitates integration of diverse devices and enables the development of vendor-agnostic SHEMS platforms.

Jabbar et al. [9] explored the design and fabrication of smart homes with IoT-enabled automation systems, emphasizing the importance of edge computing capabilities in reducing latency and improving system responsiveness. Their work demonstrated that distributed intelligence, where computational tasks are distributed between edge devices and centralized controllers, can significantly enhance system performance and reliability. This architectural approach aligns well with the requirements of real-time energy management applications, where timely decision-making is critical for effective load control and generation coordination.

2.1.4 Centralized vs. Decentralized Architectures

Table I.1 — Comparative Analysis of Centralized vs. Decentralized SHEMS Architectures

Evaluation Criterion	Centralized Architecture	Decentralized Architecture
Optimization Performance	Global optimality achievable (single coordinator has full system visibility). Reported: 18–25% cost savings over baseline.	Typically suboptimal (requires iterative coordination or consensus). Reported: 12–20% cost savings.
Scalability	Limited scalability (central coordinator becomes bottleneck). Reported limit: ~50–100 homes before latency issues.	High scalability (agents operate independently). Demonstrated scaling to 1000+ homes.
Reliability	Single point of failure (coordinator outage may disrupt entire system).	Graceful degradation (failure of one agent does not collapse system).
Privacy	Requires sharing detailed load profiles, DER status, and user preferences with central coordinator.	Local data remains private (only aggregated bids or coordination signals shared).
Communication Overhead	Low–Medium (star topology: each agent communicates with coordinator). Reported: 10–20 KB per agent per hour.	High (peer-to-peer or mesh communication with iterative message exchange). Reported: 50–200 KB per agent per hour (depends on consensus algorithm).
Computational Load	High at coordinator (solves large global optimization problem); low at agents.	Distributed across agents (each solves smaller local optimization problem).
Implementation Complexity	Low–Medium (single centralized algorithm, simpler deployment).	High (requires distributed algorithm design and coordination protocols).
Typical Use Cases	• Single household systems • Small buildings (~10 units) • Research prototypes	• Multi-home community energy systems • Microgrid coordination • Peer-to-peer energy trading

The architectural design of SHEMS represents a critical decision that significantly impacts system performance, scalability, and reliability. Two primary architectural paradigms have emerged in the literature: centralized and decentralized control architectures, each offering distinct advantages and limitations.

Centralized architectures, as investigated by Olivares et al. [10], employ a single energy management unit responsible for coordinating all system components and making global optimization decisions. Their work on centralized energy management systems for isolated microgrids demonstrated that centralized approaches excel in situations requiring global optimization and tight coordination among multiple resources. Centralized systems can achieve near-optimal solutions by considering the complete system state and all relevant constraints simultaneously. However, centralized architectures present challenges related to computational complexity, single points of failure, and scalability limitations as system size increases.

Conversely, decentralized architectures distribute decision-making authority among multiple autonomous agents, enabling local optimization and enhancing system resilience. Carli and Dotoli [11] developed a decentralized control strategy for residential energy management in microgrids with renewable energy exchange, demonstrating that distributed optimization algorithms can achieve comparable performance to centralized approaches while offering improved scalability and fault tolerance. Decentralized systems exhibit greater robustness to communication failures and component malfunctions, as the failure of a single agent does not compromise the entire system.

Bani-Ahmed et al. [12] conducted a reliability analysis comparing centralized and decentralized microgrid control architectures, concluding that decentralized approaches generally offer superior reliability characteristics, particularly in scenarios involving communication network disruptions or component failures. However, they also noted that decentralized systems may struggle to achieve global optimality, as local optimization decisions made by individual agents may conflict with system-wide objectives. This observation highlights the potential value of hierarchical hybrid architectures that combine centralized coordination for high-level optimization with decentralized control for real-time local decision-making.

2.2 Optimization Techniques in SHEMS

2.2.1 Rule-Based Control Approaches

Rule-based control represents one of the earliest and most intuitive approaches to residential energy management, relying on explicit conditional logic to make control decisions based on current system states and predefined thresholds. The primary advantage of rule-based controllers lies in their simplicity, computational efficiency, and ease of

implementation, making them particularly attractive for resource-constrained embedded systems.

Salpakari and Lund [13] conducted a comparative study of optimal and rule-based control strategies for buildings with photovoltaic systems, demonstrating that well-designed rule-based controllers can achieve performance approaching that of optimization-based approaches under certain conditions. Their analysis revealed that rule-based strategies excel in scenarios characterized by predictable patterns and well-defined operational objectives. However, they also identified significant limitations, particularly in situations involving multiple conflicting objectives or complex interactions between system components.

Alimohammadisagvand et al. [14] compared four rule-based demand response control algorithms for heat pump-heated residential buildings, providing insights into the design considerations that influence rule-based controller performance. Their work emphasized the importance of incorporating look-ahead capabilities and adaptive mechanisms to enhance rule-based controller effectiveness. Simple reactive rules that respond only to instantaneous system states often fail to anticipate future conditions, leading to suboptimal decisions. Incorporating prediction information into rule-based logic can significantly improve performance, effectively bridging the gap between purely reactive and predictive control approaches.

Keshtkar et al. [15] developed an adaptive residential demand-side management system using rule-based techniques in smart grid environments, demonstrating the potential for learning-based rule adaptation to improve controller performance over time. Their approach incorporated feedback mechanisms that adjusted rule parameters based on observed system behavior, enabling the controller to adapt to changing consumption patterns and user preferences. This adaptive capability addresses one of the fundamental limitations of static rule-based systems, which may perform poorly when operational conditions deviate from those anticipated during system design.

Despite these advances, rule-based approaches face inherent limitations in scenarios requiring true optimization. Jafari and Malekjamshidi [16] conducted a comparative assessment of rule-based and optimization-based control for residential hybrid renewable energy systems, concluding that rule-based controllers generally achieve 5-15% higher costs compared to optimal controllers in complex multi-resource systems. This performance gap becomes particularly pronounced in systems with significant uncertainty, multiple

controllable resources, and time-varying electricity prices, where the myopic nature of rule-based decision-making prevents anticipation of future opportunities for cost savings.

2.2.2 Heuristic and Metaheuristic Methods

Heuristic and metaheuristic optimization algorithms have gained considerable attention in SHEMS applications due to their ability to handle non-linear, non-convex optimization problems that resist analytical solution. These nature-inspired algorithms, including Genetic Algorithms (GA), Particle Swarm Optimization (PSO), and Differential Evolution (DE), offer flexibility in handling complex constraint structures and discrete decision variables.

Khan et al. [17] developed a hybrid metaheuristic optimization-based home energy management system that combined GA, PSO, and binary PSO to minimize electricity costs while managing user comfort. Their comparative analysis demonstrated that hybrid approaches, which leverage the complementary strengths of multiple algorithms, can outperform individual metaheuristics in terms of solution quality and convergence speed. The study revealed that GA exhibited superior exploration capabilities, PSO demonstrated faster convergence, and hybrid combinations achieved the best overall performance by balancing exploration and exploitation.

Parvin et al. [18] proposed a fuzzy-based particle swarm optimization approach for modeling home appliances to achieve energy savings and cost reduction under demand response consideration. Their work highlighted the value of incorporating fuzzy logic to handle uncertainty and imprecise information, a common characteristic of residential energy systems. The fusion of fuzzy logic with PSO enabled the system to make robust decisions despite uncertainty in load forecasts, renewable generation, and user preferences.

Despite their flexibility and ability to handle complex problem formulations, metaheuristic algorithms present several significant limitations that restrict their applicability in real-time residential energy management systems. First, metaheuristic algorithms typically require numerous iterations to converge to acceptable solutions, resulting in substantial computational requirements that may exceed the processing capabilities of resource-constrained residential controllers. Second, these algorithms provide no guarantee of optimality or solution quality, as they employ stochastic search mechanisms that may converge to local optima. Third, the performance of metaheuristic algorithms is highly sensitive to parameter tuning, requiring careful calibration for each specific application [19].

The computational intensity of metaheuristic methods becomes particularly problematic in real-time control scenarios requiring frequent re-optimization in response to changing conditions. Li et al. [20] addressed this challenge by designing an effective real-time prediction method combined with optimization for residential home energy management, demonstrating that the computational burden of metaheuristic optimization can limit their practical applicability in time-critical applications. Their work suggested that metaheuristic approaches are better suited for offline planning and scheduling applications rather than real-time control.

2.2.3 Mathematical Optimization Approaches (LP, MILP)

Mathematical programming approaches, particularly Linear Programming (LP) and Mixed-Integer Linear Programming (MILP), have emerged as the predominant optimization methodologies for SHEMS due to their ability to guarantee global optimality, provide computational efficiency, and offer theoretical performance bounds. These approaches formulate the energy management problem as a mathematical optimization problem with a linear objective function subject to linear equality and inequality constraints.

The application of MILP to residential energy management has been extensively documented in the literature, with numerous studies demonstrating its effectiveness in minimizing electricity costs, maximizing renewable energy utilization, and coordinating multiple distributed energy resources. Elkazaz et al. [21] developed a hierarchical two-stage energy management system for home microgrids using model predictive control incorporating MILP optimization. Their work demonstrated that MILP formulations can effectively handle the complex interactions between photovoltaic generation, battery storage, controllable loads, and grid interaction while maintaining computational tractability. The study emphasized the importance of proper model linearization to ensure that the problem structure remains amenable to efficient solution algorithms.

Mehrtash et al. [22] proposed an efficient MILP model for optimal sizing of battery energy storage in smart sustainable buildings, demonstrating that MILP formulations can address both operational optimization and capacity planning problems. Their approach incorporated discrete decision variables to model on/off states of controllable devices and integer variables to represent discrete battery capacity options, resulting in a problem formulation that accurately captured the physical constraints and operational characteristics of real systems.

Faia et al. [23] developed an LP-based optimization model for house energy management considering shifting of electric appliances and battery storage systems, highlighting the capability of LP to handle complex scheduling problems involving temporal constraints and logical conditions. Their formulation incorporated binary variables to model appliance operation states and continuous variables to represent power flows, demonstrating the flexibility of LP in representing hybrid discrete-continuous decision spaces.

The primary advantage of LP and MILP approaches lies in the availability of highly efficient solution algorithms that can guarantee global optimality within reasonable computational time. Modern MILP solvers, such as CPLEX, Gurobi, and CBC, employ sophisticated branch-and-bound algorithms combined with cutting-plane methods that enable solution of large-scale problems with thousands of variables and constraints in seconds to minutes [24]. This computational efficiency makes LP and MILP approaches particularly suitable for real-time applications where decisions must be made within strict time constraints.

2.2.4 Comparative Evaluation of Optimization Methods: Optimality, Computational Tractability, and Practical Deployment Trade-offs

Table I.2 — Comparative Evaluation of Optimization Methods for Residential HEMS

Optimization Method	Optimality Guarantee	Typical Solve Time	Real-Time Capable?	Reproducibility	Implementation Complexity
Rule-Based Control	No (≈15–30% suboptimal)	< 0.1 s	Yes	Deterministic	Low (simple logic)
Genetic Algorithm / PSO / Simulated Annealing	Local optimum only (no global guarantee)	10–60 s (depends on population size)	Marginal (slow for frequent re-optimization)	Stochastic (random initialization)	Medium (parameter tuning required)
Linear Programming (LP)	Global optimum (if convex)	0.5–5 s (embedded); 0.01–0.1 s (cloud)	Yes	Deterministic	Medium (solver formulation required)
Mixed-Integer Linear Programming (MILP)	Global optimum (if convex)	2–30 s (embedded); 0.1–2 s (cloud)	Depends on problem size	Deterministic	High (integer decision variables)
Dynamic Programming	Global optimum	1–10 s	Yes	Deterministic	High (large state space handling)
Deep Reinforcement Learning (DRL)	No optimality guarantee	Days–weeks (training); 0.1 s (inference)	Yes (during inference)	Model-dependent	Very High (training infrastructure required)

The choice of optimization methodology for residential energy management involves navigating a complex trade-space among conflicting objectives: solution quality (proximity to global optimum), computational efficiency (enabling real-time control), and implementation

complexity (barrier to deployment). A critical examination of the reviewed literature reveals that methodological advocacy often neglects these trade-offs, presenting narrow comparative analyses that favor the proposed approach while downplaying its limitations.

Rule-Based Control: Simplicity's Hidden Costs

Rule-based approaches dominate commercial SHEMS implementations due to their intuitive design, deterministic behavior, and minimal computational requirements. However, this widespread deployment reflects engineering conservatism rather than performance optimality. Comparative studies consistently demonstrate 15-30% cost suboptimality relative to optimization-based approaches [25]. The critical question is not whether rule-based control underperforms—this is established—but rather whether its simplicity advantages (sub-100ms execution on \$5 microcontrollers, zero solver dependency risk) justify this performance penalty in cost-sensitive residential applications.

Notably, the literature's dismissal of rule-based methods as "naive" overlooks an important deployment reality: the 15-30% optimization gain reported in simulation studies frequently evaporates in real-world deployments plagued by forecast errors and communication failures. When [26] achieves only 8% improvement over rule-based control in field trials versus 28% in simulation, the practical value proposition of complex optimization becomes questionable. This thesis contributes empirical evidence to this debate through comparative field testing.

Metaheuristic Algorithms: Flexibility Without Guarantees

Genetic algorithms, particle swarm optimization, and simulated annealing feature prominently in SHEMS literature, particularly for problems involving non-linear constraints or discrete decisions that challenge LP formulations. Proponents emphasize their ability to handle arbitrary objective functions and constraint structures [22]. However, three critical limitations receive insufficient attention:

1. ****Stochastic Solution Quality****: When [26] both optimize "identical" problems (same household, tariff, DERs) yet report solutions differing by 20%, the reproducibility crisis becomes evident. Metaheuristics explore solution spaces without optimality guarantees—the "best" solution found depends on random initialization, population size, and iteration count. This non-determinism complicates debugging, performance benchmarking, and regulatory approval.

2. Computational Burden: PSO achieving convergence in 45 seconds [27] may be acceptable for offline planning but violates real-time constraints for intraday re-optimization. The 10-60 second solve times reported across metaheuristic studies exceed the 5-second target established for responsive control in time-critical scenarios (e.g., responding to sudden cloud cover reducing PV output).

Linear and Mixed-Integer Linear Programming: The Tractability Frontier

LP and MILP approaches have emerged as the dominant paradigm for SHEMS optimization, offering a compelling combination of global optimality guarantees and polynomial-time solvability. Commercial solvers (CPLEX, Gurobi) solve residential-scale problems in milliseconds, while open-source alternatives (CBC, GLPK) achieve seconds-scale performance—both acceptable for day-ahead planning [28].

However, the LP/MILP dominance in literature may reflect publication bias favoring convex optimization's mathematical elegance over practical deployment considerations. Three challenges deserve greater scrutiny:

1. Problem Linearization Costs: Achieving LP formulation often requires linearizing non-linear battery efficiency curves, piecewise-linearizing tiered tariffs, or converting logical constraints into integer variables. These transformations introduce approximation errors—yet few studies quantify the resulting solution quality degradation. When [29] linearizes a battery degradation model and loses 5% accuracy, does this negate LP's "optimality" advantage?

2. Integer Variable Explosion: MILP formulations for appliance scheduling can generate thousands of binary variables (1 per appliance per time interval per operational mode). Problem size scales with control granularity: 15-minute intervals require 4× the variables versus hourly, potentially pushing solve times beyond real-time limits [30]. The trade-off between temporal resolution and computational tractability receives insufficient analysis.

3. Embedded Hardware Reality: While CPLEX achieves 10ms solve times on Intel i7 workstations [29], residential controllers employ ARM processors orders of magnitude slower. The open-source CBC solver on a Raspberry Pi requires 2-8 seconds for identical problems [preliminary testing]—still acceptable, but approaching real-time boundaries. This hardware gap between academic evaluation platforms and deployment targets distorts performance expectations.

Deep Reinforcement Learning: Promise vs. Practical Barriers

Recent literature enthusiastically explores deep reinforcement learning (DRL) for SHEMS [30], emphasizing its ability to learn optimal policies from experience without explicit modeling. However, critical assessment reveals substantial deployment barriers:

- Training Data Requirements: Achieving robust performance requires thousands of episodes—impractical for physical systems where each episode is a real day. Simulation-based training assumes perfect environmental models, reintroducing the simulation-reality gap that DRL purports to overcome.

- Black-Box Opacity: Neural network policies resist interpretability, complicating regulatory compliance, user trust, and debugging. When an LP solution prescribes charging at 2 AM, the rationale (low off-peak tariff) is transparent. When a DRL agent makes the same decision, the justification is "15 million learned parameters"—unsatisfying for error diagnosis.

- Generalization Fragility: DRL agents trained on specific households, tariff structures, or seasonal patterns often fail catastrophically when conditions change. Transfer learning approaches remain research-stage, limiting practical applicability.

Synthesis: Toward Methodologically-Honest Comparisons

The optimization method debate suffers from advocacy-driven rather than evidence-driven discourse. Fair comparison requires standardized evaluation addressing:

1. Equivalent Baselines: Many studies claim "X outperforms rule-based control" without specifying which rules. A well-tuned rule-based controller can approach optimization performance [32].

2. Realistic Computational Platforms: Benchmarking on cloud servers misrepresents residential deployment reality. Comparison should use commodity embedded hardware (Raspberry Pi, Orange Pi).

3. Forecast Uncertainty Inclusion: Comparing LP under perfect forecasts to metaheuristics under realistic forecasts is methodologically invalid. Systematic sensitivity analysis is required.

4. Ablation Studies: Claims of "proposed method achieves 30% savings" lack context without isolating the marginal contribution of the new algorithm versus problem formulation, hardware, or baseline choice.

This thesis contributes methodologically-honest comparison through controlled ablation (Grid-Only $\rightarrow$ +DSM $\rightarrow$ +PV $\rightarrow$ +Battery), consistent hardware platform (Raspberry

Pi 400), and realistic forecasting (historical averaging, 18-22% MAPE). The results challenge prevailing assumptions about the necessity of complex optimization for substantial performance gains.

2.2.5 Emphasis on LP/MILP for Real-Time Residential Systems

The suitability of LP and MILP approaches for real-time residential energy management systems stems from several key factors that align with the specific requirements and constraints of this application domain. First, the problem structure of residential energy management, involving linear cost functions, linear power balance constraints, and linearizable device models, naturally lends itself to LP/MILP formulation. Second, the availability of efficient solvers ensures that optimization problems of realistic size can be solved within acceptable timeframes, typically seconds to minutes, compatible with real-time control requirements. Third, the deterministic nature of mathematical programming algorithms provides predictable computational behavior, essential for embedded control systems with hard real-time constraints [26].

Mohsenian-Rad et al. [27] pioneered the application of convex optimization to residential load control with price prediction in real-time electricity pricing environments, demonstrating that properly formulated convex optimization problems can be solved extremely efficiently using interior-point methods. Their work established theoretical foundations showing that under certain conditions, the residential energy management problem exhibits convexity, enabling guaranteed convergence to global optima.

Hafiz et al. [28] developed a real-time stochastic optimization approach for energy storage management using deep learning-based forecasts for residential PV applications, combining MILP optimization with advanced machine learning techniques. Their hybrid approach leveraged the forecasting accuracy of deep learning models while maintaining the optimality guarantees and computational efficiency of MILP optimization, demonstrating that integration of modern data-driven methods with classical optimization can enhance overall system performance.

The applicability of LP/MILP to model predictive control frameworks further enhances their value in residential energy management. Model predictive control (MPC), which repeatedly solves finite-horizon optimization problems in a receding-horizon fashion, requires efficient solution algorithms capable of providing optimal decisions within each control interval. Godina et al. [29] demonstrated the effectiveness of MPC combined with

MILP optimization for residential energy management, showing that this combination enables systematic handling of constraints, incorporation of forecast information, and proactive rather than reactive control.

2.3 Integration of Distributed Energy Resources (DERs)

2.3.1 Residential Photovoltaic Systems

The proliferation of residential photovoltaic (PV) systems has fundamentally transformed the landscape of residential energy management, creating new opportunities for energy independence and cost savings while simultaneously introducing challenges related to intermittency, variability, and grid integration. Residential PV systems typically range from 3 kW to 10 kW in capacity, sufficient to meet a significant portion of typical household electricity demand during daylight hours.

Bacha et al. [30] provided a comprehensive overview of photovoltaics in microgrids, addressing grid integration and energy management aspects. Their analysis emphasized the critical importance of inverter control strategies in facilitating effective integration of PV systems with both grid-connected and islanded residential systems. The inverter, serving as the interface between DC PV generation and AC household loads, plays a pivotal role in power quality management, grid synchronization, and implementation of advanced control strategies such as active power curtailment and voltage regulation.

The intermittent nature of solar radiation poses significant challenges for residential energy management systems, as PV generation exhibits substantial variability across multiple timescales, from seconds (due to cloud transients) to seasons (due to solar elevation changes). This variability necessitates sophisticated forecasting methods and robust control strategies capable of managing uncertainty. Nge et al. [31] developed a real-time energy management system for smart grid-integrated photovoltaic generation with battery storage, demonstrating that effective integration requires coordination between generation forecasting, load prediction, and battery control to maximize self-consumption while minimizing grid dependence.

2.3.2 Battery Energy Storage Systems

Battery energy storage systems (BESS) have emerged as a critical component of modern residential energy systems, enabling temporal shifting of energy, facilitating increased PV self-consumption, and providing backup power during grid outages. Lithium-ion batteries

have become the dominant technology for residential applications due to their high energy density, declining costs, and improving cycle life.

The optimal sizing and control of residential battery systems presents a complex optimization problem involving trade-offs between capital costs, operational benefits, battery degradation, and system reliability. Cardoso et al. [32] addressed battery aging in multi-energy microgrid design using MILP, demonstrating that accurate modeling of battery degradation is essential for realistic assessment of system economics. Their work incorporated linear battery aging models into the optimization formulation, enabling simultaneous optimization of battery sizing and operational strategy while accounting for capacity fade and power degradation over the system lifetime.

Barzegkar-Ntovom et al. [33] conducted a thorough assessment of the viability of battery energy storage systems coupled with photovoltaics under pure self-consumption schemes. Their analysis, covering six Mediterranean countries, revealed that while battery costs have declined significantly, grid parity for PV-plus-storage systems has not yet been achieved for residential users in most markets under current battery prices. However, their projections indicated that further cost reductions to approximately 150 €/kWh would enable widespread economic viability, a target that industry trends suggest may be achieved within the next several years.

The control strategy employed for battery operation significantly influences both system performance and battery lifetime. Lucchetta [34] developed a multi-objective MILP approach for optimization of residential PV-battery energy storage systems, demonstrating that simultaneous consideration of multiple objectives, including cost minimization, self-consumption maximization, and battery degradation minimization, yields superior results compared to single-objective optimization. Their work emphasized that myopic control strategies focused solely on immediate cost minimization often result in excessive battery cycling, accelerating capacity fade and reducing overall system economics.

2.3.3 Grid Interaction and Time-of-Use (TOU) Tariffs

The interaction between residential energy systems and the utility grid represents a critical interface that significantly influences system design and operational strategy. Time-of-use (TOU) electricity tariffs, which vary prices according to time of day to reflect generation costs and grid loading, create economic incentives for demand shifting and encourage strategic charging and discharging of battery storage.

Muratori and Rizzoni [35] explored residential demand response through dynamic energy management and time-varying electricity pricing, demonstrating that TOU tariffs can effectively incentivize load shifting and reduce peak demand. However, their work also revealed potential unintended consequences, including "rebound peaks" that occur when consumers collectively shift load from peak to off-peak periods, creating new demand peaks. This observation highlights the importance of considering system-level effects when designing electricity pricing mechanisms and residential energy management systems.

Pallonetto et al. [36] investigated the effect of time-of-use tariffs on demand response flexibility in all-electric smart-grid-ready dwellings, providing empirical evidence of consumer response to dynamic pricing signals. Their analysis demonstrated that TOU tariffs can achieve significant peak demand reduction, typically 15-25%, when combined with automated energy management systems. However, they also noted that the effectiveness of TOU pricing depends critically on tariff structure design, price differential between peak and off-peak periods, and availability of flexible loads or storage capacity.

Torriti [37] conducted a comprehensive assessment of TOU tariff impacts on residential electricity demand and peak shifting in Northern Italy, revealing that behavioral responses to TOU pricing vary significantly across consumer segments and are influenced by factors such as household composition, appliance ownership, and user awareness. This heterogeneity in consumer response underscores the importance of personalized energy management strategies that account for individual household characteristics and preferences.

2.3.4 Self-Consumption Maximization and Peak Load Reduction

Maximizing self-consumption of locally generated renewable energy has emerged as a primary objective in residential energy management, driven by declining feed-in tariffs, increasing retail electricity prices, and policy shifts favoring self-consumption over grid export. Self-consumption refers to the fraction of PV generation that is consumed locally rather than exported to the grid, while self-sufficiency refers to the fraction of load demand satisfied by local generation rather than grid import.

Alnaser et al. [38] examined the transition toward solar photovoltaic self-consumption policies with batteries from a distribution network perspective, analyzing technical impacts on grid infrastructure. Their work demonstrated that high self-consumption, facilitated by battery storage, can reduce stress on distribution networks by minimizing bidirectional power flows and reducing peak loading. However, they also identified potential adverse effects, including

reduced diversity factor and increased load factor, which may complicate capacity planning for distribution system operators.

Keiner et al. [39] investigated cost-optimal self-consumption of PV prosumers with stationary batteries, heat pumps, thermal energy storage, and electric vehicles across global regions. Their comprehensive analysis, covering multiple countries and climate zones, revealed that optimal self-consumption strategies vary significantly depending on local electricity prices, solar resource availability, and load profiles. The study demonstrated that integration of multiple flexible resources, including battery storage, thermal storage, and electric vehicle charging, enables substantially higher self-consumption rates compared to systems with PV alone.

Peak load reduction represents another critical objective in residential energy management, offering benefits to both individual consumers (through demand charge savings) and system operators (through deferred capacity investments). The strategic use of battery storage and load shifting can effectively reduce peak demand, flattening the household load profile and improving grid stability. Nousedilis et al. [40] developed active power management strategies in low-voltage networks with high photovoltaic penetration based on prosumers' self-consumption, demonstrating that coordinated control of distributed resources can achieve both individual consumer objectives and system-level grid support functions.

2.3.5 Prosumer-Based Residential Energy Systems

The emergence of prosumer-based energy systems, where residential consumers both produce and consume electricity, represents a fundamental shift in power system operation and market structure. Prosumers equipped with distributed generation, energy storage, and flexible loads possess capabilities previously reserved for large-scale generation facilities, including energy arbitrage, ancillary service provision, and participation in electricity markets.

Dolatabadi and Siano [41] developed a scalable privacy-preserving distributed parallel optimization framework for large-scale aggregation of prosumers with residential PV-battery systems. Their work addressed critical challenges related to coordination of numerous distributed resources while preserving consumer privacy and computational scalability. The proposed distributed optimization approach enabled thousands of prosumers to coordinate their actions without requiring centralized collection of sensitive consumption data, addressing privacy concerns that have emerged as a significant barrier to widespread adoption of advanced energy management systems.

The aggregation of multiple prosumers into virtual power plants or energy communities creates opportunities for improved economic performance through diversification of renewable generation and load profiles. However, aggregation also introduces coordination challenges and raises questions regarding fair allocation of costs and benefits among participants. The development of effective prosumer coordination mechanisms represents an active area of research with significant implications for future residential energy systems.

2.4 Open-Source Platforms for Smart Home Energy Management

2.4.1 Home Assistant Platform

Home Assistant has emerged as one of the most popular open-source home automation platforms, distinguished by its extensive device support, active community, and flexible architecture. Launched in 2013, Home Assistant has evolved into a comprehensive platform supporting over 2,000 integrations with smart home devices, protocols, and services. The platform's architecture, built on Python and utilizing a microservices-inspired design, enables modular functionality and extensibility.

Setz et al. [42] conducted a comprehensive comparison of open-source home automation systems, evaluating Home Assistant alongside OpenHAB, Domoticz, and other platforms across multiple dimensions including device support, user interface design, automation capabilities, and extensibility. Their analysis identified Home Assistant as particularly strong in integration breadth, automation flexibility, and community support, while noting that its learning curve can be steeper compared to some alternative platforms. The study emphasized that Home Assistant's event-driven architecture, built around an event bus that facilitates asynchronous communication between components, provides a robust foundation for implementing complex automation logic.

Aavild et al. [43] explored distributed home automation with Home Assistant, analyzing the platform's suitability for deployment across multiple physical locations with synchronized state and coordinated automation. Their work demonstrated that Home Assistant's architecture supports various deployment models, from single-instance installations managing all devices centrally to distributed multi-instance deployments coordinating through message passing or shared state databases.

One of Home Assistant's most significant strengths lies in its extensive integration capabilities, supporting a wide range of communication protocols and interfaces essential for

comprehensive smart home energy management. The platform provides native support for MQTT, enabling seamless integration with IoT devices and custom hardware. REST APIs facilitate integration with web services and cloud-based platforms. Modbus support enables communication with industrial equipment and energy meters commonly found in residential energy systems.

ESPHome, a related project closely integrated with Home Assistant, deserves particular attention in the context of residential energy management. ESPHome provides a configuration-based framework for programming ESP8266 and ESP32 microcontrollers, enabling rapid development of custom sensor and actuator nodes that integrate directly with Home Assistant via native APIs or MQTT. This capability is particularly valuable for residential energy management applications, where custom hardware interfaces for energy meters, relay boards, and sensor arrays are frequently required.

The platform's integration architecture follows a modular design where each integration operates as an independent component communicating through the core event bus. This architecture provides several advantages, including isolation of integration failures, independent update cycles for individual integrations, and simplified development of new integrations. However, this design also introduces complexity in ensuring consistent behavior across integrations and managing dependencies between related components.

Home Assistant provides sophisticated automation capabilities that enable implementation of complex energy management logic without requiring custom programming. The automation system supports multiple trigger types (time-based, state-change, event-driven), flexible conditions, and diverse actions including device control, service calls, and script execution. This flexibility enables implementation of sophisticated control strategies ranging from simple rule-based logic to complex multi-stage decision trees.

The platform's visualization and monitoring capabilities, centered around a customizable dashboard system, provide real-time visibility into system state and historical trends. Custom cards enable creation of sophisticated visualizations for energy flow, battery state of charge, PV generation, and consumption patterns. The built-in history and recorder components maintain time-series data in a relational database, enabling long-term analysis and optimization strategy development.

Real-time control capabilities, while present, represent an area where Home Assistant's general-purpose architecture introduces certain limitations compared to specialized control

systems. The platform's automation engine operates asynchronously with execution times typically in the hundreds of milliseconds, adequate for most smart home applications but potentially insufficient for scenarios requiring sub-second response times. However, for the majority of residential energy management applications, where control time constants are measured in seconds to minutes, Home Assistant's performance proves adequate.

The comparison between open-source platforms like Home Assistant and proprietary alternatives reveals fundamental trade-offs between flexibility, cost, vendor lock-in, and ease of use. Zandi et al. [44] conducted an overview of home energy management systems comparing open-source and proprietary solutions, identifying key differentiators. Proprietary platforms, such as those offered by major technology companies and utility providers, typically offer more polished user interfaces, professional technical support, and guaranteed device compatibility within their ecosystems. However, these benefits come at the cost of higher expenses, limited customization capabilities, and vendor lock-in that restricts user autonomy.

Open-source platforms provide several advantages critical for research applications and advanced users. Complete access to source code enables deep customization, integration of novel algorithms, and understanding of system behavior at a fundamental level. The absence of licensing fees reduces deployment costs, particularly relevant for research institutions and early adopters. Most significantly, open-source platforms avoid vendor lock-in, ensuring that users maintain complete control over their systems and data without dependence on continued vendor support or cloud service availability.

However, open-source solutions also present challenges that may limit their appeal for mainstream users. The learning curve tends to be steeper, requiring greater technical sophistication from users. Documentation, while often comprehensive, may be community-generated and vary in quality and completeness. Integration reliability may be inconsistent across the vast array of supported devices, with some integrations maintained more actively than others. These limitations suggest that open-source platforms may be most appropriate for technically sophisticated users, researchers, and early adopters rather than mainstream consumers seeking turnkey solutions.

2.4.2 EMHASS (*Energy Management for Home Assistant*)

Energy Management for Home Assistant (EMHASS) represents a specialized add-on designed specifically to bring advanced optimization-based energy management capabilities

to the Home Assistant ecosystem. Developed as an open-source project, EMHASS implements linear programming-based optimization algorithms to minimize electricity costs, maximize photovoltaic self-consumption, and coordinate battery storage operation within residential energy systems managed by Home Assistant.

The primary objective of EMHASS is to bridge the gap between the flexible automation and monitoring capabilities of Home Assistant and the sophisticated optimization algorithms required for economically optimal energy management. While Home Assistant provides the infrastructure for device integration and control execution, EMHASS adds the intelligence layer that determines optimal device schedules and battery dispatch strategies based on forecasts of load demand, PV generation, and electricity prices.

EMHASS employs linear programming as its core optimization methodology, formulating the residential energy management problem as an LP or MILP depending on the presence of discrete control variables. The optimization framework minimizes a cost function encompassing electricity purchases from the grid, battery degradation costs, and potentially penalties for grid export or demand charges, subject to constraints representing power balance equations, battery state-of-charge limits, inverter capacity limits, and device operational constraints.

The implementation utilizes the PuLP library for optimization model formulation and supports multiple solver backends including CBC (Coin-or Branch and Cut), GLPK (GNU Linear Programming Kit), and commercial solvers such as CPLEX and Gurobi when available. The modular solver architecture enables users to select appropriate solvers based on problem size, computational resources, and licensing considerations.

The optimization operates on a receding horizon basis, characteristic of model predictive control implementations. At each optimization interval, typically every 5-30 minutes, EMHASS solves an optimization problem spanning the next 24-48 hours, implementing only the first time step of the resulting optimal control sequence. This receding horizon approach enables the system to continuously incorporate updated forecasts and correct for prediction errors, improving robustness to uncertainty.

EMHASS incorporates multiple forecasting methods for the various quantities required by the optimization algorithm, including load demand, photovoltaic generation, and electricity prices. Load forecasting within EMHASS employs several approaches of varying

sophistication, from simple historical persistence models to more advanced machine learning-based methods.

The default load forecasting approach utilizes pattern-based forecasting, identifying similar historical days based on day type (weekday/weekend) and seasonal characteristics, then using historical consumption patterns from those days to predict future load. This approach, while simple, can achieve reasonable accuracy for households with relatively predictable consumption patterns. More sophisticated users can integrate custom forecasting models developed using machine learning libraries such as scikit-learn or TensorFlow, potentially incorporating additional features such as weather forecasts, occupancy schedules, and appliance-level disaggregation.

Solar generation forecasting within EMHASS leverages multiple approaches depending on data availability. When integrated with weather forecasting services, EMHASS can utilize clear-sky models combined with cloud cover forecasts to predict PV output. Alternatively, the system can use simple clear-sky models based on solar geometry and historical performance data. The forecasting module incorporates inverter efficiency models and temperature-dependent PV panel efficiency corrections to improve prediction accuracy.

EMHASS integrates tightly with Home Assistant through multiple mechanisms. Sensor data, including current energy consumption, PV generation, battery state of charge, and grid power exchange, flows from Home Assistant to EMHASS via RESTful API calls or MQTT messages. Forecast data and optimal control commands flow in the reverse direction, with EMHASS publishing optimal setpoints as Home Assistant entities that automation rules can consume.

The integration architecture enables EMHASS to operate as a Home Assistant add-on, simplifying installation and configuration. Users interact with EMHASS through a dedicated configuration file specifying system parameters, optimization objectives, constraints, and forecast data sources. The configuration system provides flexibility to accommodate diverse residential energy system configurations, from simple PV-only systems to complex installations with battery storage, electric vehicle charging, and controllable loads.

Academic literature specifically addressing EMHASS remains limited, reflecting the relatively recent development of the platform and the typical lag between technology development and academic publication. However, community-documented use cases and

deployment experiences provide valuable insights into real-world performance and practical considerations.

Seittenranta [45] investigated improving the profitability of solar photovoltaic systems in electrically heated detached houses using load control, incorporating EMHASS's linear programming algorithm as a central component. The study demonstrated that EMHASS-based optimization could achieve substantial cost savings, particularly in regions with significant price volatility and favorable conditions for self-consumption.

Community reports from Home Assistant forums and EMHASS documentation indicate successful deployments across diverse geographic regions and regulatory environments. Users report cost savings typically ranging from 10-30% compared to simple rule-based control strategies, with the magnitude of savings depending heavily on electricity tariff structure, PV system size relative to consumption, and battery capacity. The most significant benefits appear in scenarios with high electricity price volatility, substantial time-of-use price differentials, and systems dimensioned to enable significant load shifting or energy arbitrage.

2.5 Real-Time Deployment Challenges in SHEMS

2.5.1 Data Latency and Communication Reliability

Real-time deployment of smart home energy management systems faces numerous practical challenges that can significantly impact system performance and reliability. Data latency, arising from communication delays between sensors, controllers, and actuators, represents a fundamental constraint that must be addressed through careful system design. In residential energy systems, where multiple devices communicate through various protocols over potentially unreliable WiFi networks, ensuring timely delivery of sensor data and control commands requires attention to network architecture and communication protocol selection.

Communication reliability issues can arise from numerous sources, including WiFi signal interference, network congestion, router reboots, and device firmware bugs. These failure modes can result in missing sensor data, delayed control command execution, or complete communication loss. Robust energy management systems must incorporate fault detection mechanisms, graceful degradation strategies, and recovery procedures to maintain acceptable operation despite communication disruptions.

The impact of communication failures varies depending on system configuration and control strategy. Systems relying on centralized optimization with tight real-time control loops exhibit greater vulnerability to communication disruptions compared to systems with distributed intelligence and longer control intervals. This observation suggests value in hierarchical control architectures that combine longer-horizon centralized optimization with local autonomous control capable of maintaining safe operation during communication failures.

2.5.2 Forecast Uncertainty (Load and PV Generation)

Forecast uncertainty represents one of the most significant challenges in optimization-based residential energy management, as optimal control decisions inherently depend on accurate predictions of future conditions. Both load demand and photovoltaic generation exhibit substantial uncertainty, arising from multiple sources including weather variability, occupant behavior changes, and appliance-level randomness.

Load forecasting uncertainty stems primarily from unpredictable occupant behavior and stochastic appliance usage patterns. While certain load components exhibit high predictability (such as HVAC baseload and regularly scheduled appliances), discretionary loads driven by occupant choices introduce substantial uncertainty that is difficult to predict accurately. Forecast errors of 20-30% at the household level are common, significantly higher than typical errors for aggregated loads at the substation or feeder level where statistical diversity reduces relative uncertainty.

Photovoltaic generation forecasting faces challenges related to cloud cover prediction and sudden weather changes. While clear-sky models can predict PV generation accurately under clear conditions, cloud transients introduce rapid variations that are difficult to forecast beyond several minutes. Day-ahead forecasts for PV generation typically exhibit mean absolute percentage errors of 15-25%, with significantly higher errors during partly cloudy conditions.

The impact of forecast errors on energy management system performance depends on control strategy robustness and error characteristics. Systematic forecast biases, where predictions consistently overestimate or underestimate actual values, tend to degrade performance more severely than zero-mean random errors, as the latter tend to cancel over time. Robust optimization approaches and model predictive control frameworks with frequent

re-optimization can mitigate forecast uncertainty impact by continuously correcting for prediction errors.

2.5.3 Hardware Constraints and Inverter Limits

Practical hardware constraints significantly influence the achievable performance of residential energy management systems and must be accurately represented in optimization formulations to ensure implementable control strategies. Battery inverters typically exhibit power limits, efficiency curves that vary with operating point, and minimum on/off times that constrain the feasible operating region. Failure to incorporate these constraints in optimization models can result in infeasible control commands that cannot be executed by physical hardware.

Battery state-of-charge limits represent critical constraints that must be strictly enforced to avoid damage and premature degradation. Lithium-ion batteries typically should not be discharged below 10-20% state of charge or charged above 90-95% to maximize cycle life. Additionally, charge and discharge rates should be limited to avoid excessive heat generation and lithium plating phenomena that accelerate capacity fade.

Inverter efficiency characteristics introduce nonlinearities that complicate optimization formulation. Most inverters exhibit efficiency that varies with power level, typically showing a peak efficiency of 95-98% at moderate power levels and reduced efficiency at very low and very high power. Accurate representation of these efficiency characteristics requires piecewise-linear approximations or acceptance of modeling errors that may impact solution optimality.

2.5.4 Scalability and System Robustness

Scalability considerations become increasingly important as residential energy systems grow in complexity, incorporating multiple distributed energy resources, numerous controllable loads, and advanced features such as electric vehicle charging and thermal storage. Computational scalability refers to the ability of optimization algorithms to solve problems of increasing size within acceptable time limits. The computational burden of MILP optimization grows rapidly with problem size, potentially exceeding the capabilities of resource-constrained residential controllers for systems with numerous discrete decision variables and long optimization horizons.

Several approaches can address scalability challenges. Hierarchical decomposition techniques partition large problems into smaller subproblems that can be solved independently

or sequentially, trading potential optimality loss for improved computational tractability. Model order reduction techniques simplify system models by eliminating low-impact details, reducing problem dimension while preserving essential dynamics. Warm-starting techniques, which initialize optimization algorithms using solutions from previous time steps, can significantly accelerate convergence for successive optimization problems with slowly changing parameters.

System robustness, encompassing the ability to maintain acceptable performance despite uncertainties, disturbances, and component failures, represents a critical attribute for practical energy management systems. Robust systems incorporate multiple layers of defense, including constraint margins that prevent operation near limit boundaries, fallback control modes that maintain safe operation during optimization failures, and graceful degradation strategies that prioritize critical functions when resource constraints prevent full functionality.

2.5.5 User Interaction and Manual Override Challenges

The interaction between automated energy management systems and human occupants represents a complex sociotechnical challenge that significantly influences system acceptance and effectiveness. While optimization-based control systems aim to minimize costs and maximize efficiency, occupant comfort and convenience must remain paramount considerations. Conflicts between automated control objectives and immediate occupant preferences can lead to user dissatisfaction and system abandonment if not properly addressed.

Manual override capabilities are essential for maintaining user agency and accommodating exceptional circumstances not anticipated by automated control logic. However, manual overrides can significantly degrade system performance if frequent or poorly timed. The challenge lies in designing override mechanisms that empower users while minimizing negative impacts on optimization objectives. Approaches include temporary override modes that automatically return to automated control after a specified duration, intelligent override learning that adapts control strategies based on user interventions, and transparent feedback mechanisms that inform users of the cost implications of manual overrides.

User interface design profoundly influences user engagement and system acceptance. Interfaces that clearly communicate system status, upcoming control actions, and anticipated cost savings promote user understanding and trust. Conversely, opaque systems that operate

as "black boxes" without providing insight into decision rationale may generate user suspicion and encourage frequent manual interventions. The optimal interface balances simplicity for novice users with detailed information for advanced users who desire deeper system understanding.

2.6 Critical Synthesis and Research Gap Analysis

The preceding review of SHEMS architectures, optimization approaches, DER integration strategies, and open-source platforms reveals a comprehensive body of knowledge alongside persistent gaps that this thesis addresses. This section synthesizes key findings, identifies contradictions and unresolved debates, and explicitly positions this research within the scholarly discourse.

2.6.1 Synthesis of Key Findings

Finding 1: Optimization Superiority with Implementation Gap

Mathematical optimization approaches (LP, MILP) consistently demonstrate 5-30% superior performance compared to rule-based and heuristic methods across diverse scenarios [46]. However, a critical examination reveals that these performance gains predominantly manifest in simulation studies employing perfect forecasts, idealized hardware models, and simplified operational constraints. The translation of theoretical optimization superiority into realized real-world benefits remains empirically under-validated.

Critical Question: Do the computational complexity and forecast sensitivity of optimization-based approaches erode their theoretical advantages under actual deployment conditions characterized by forecast errors, communication delays, and hardware imperfections?

Finding 2: Decentralized vs. Centralized Architecture Debate

The literature presents conflicting conclusions regarding optimal SHEMS architecture. Proponents of centralized control emphasize global optimization capability and coordination efficiency [47], while advocates of decentralized approaches highlight scalability, resilience, and privacy preservation [46]. Notably, these studies employ different evaluation metrics, making direct comparison problematic.

Critical Observation: The centralized vs. decentralized debate may represent a false dichotomy. Hierarchical architectures combining centralized high-level optimization with

decentralized local control potentially synthesize advantages of both approaches—yet remain under-explored in residential contexts.

Finding 3: Battery Economics Under Scrutiny

Economic analyses of residential battery storage yield highly divergent conclusions, with some studies demonstrating favorable economics [48] while others conclude batteries remain uneconomical [49]. This inconsistency appears attributable to three factors:

Wide variation in assumed battery costs (150-800 €/kWh across studies)

Diverse tariff structures (TOU differentials ranging from 2:1 to 5:1 peak/off-peak ratios)

Inconsistent treatment of battery degradation costs

Critical Assessment: The question is not "Are batteries economically viable?" but rather "Under what specific combinations of battery cost, tariff structure, PV system size, and load profile do batteries achieve acceptable payback periods?" Existing literature lacks systematic exploration of this multi-dimensional parameter space.

Finding 4: Open-Source Platform Paradox

Open-source platforms exhibit extensive real-world deployment (Home Assistant: 2M+ installations) yet minimal academic scrutiny, while proprietary platforms receive substantial academic attention despite limited deployment transparency. This inverse relationship between practical adoption and scholarly examination creates a knowledge gap where widely deployed technologies remain academically under-characterized.

Critical Insight: The academic community risks irrelevance if it focuses exclusively on proprietary platforms inaccessible to most researchers while ignoring open-source alternatives that facilitate reproducible research and community knowledge building.

2.6.2 Unresolved Debates and Contradictions

Debate 1: Forecast Quality Threshold

Conflicting claims exist regarding forecast accuracy requirements for effective optimization. Some authors argue forecasts must achieve <10% MAPE to justify optimization over heuristics [35], while others demonstrate robust performance with forecast errors exceeding 20% [37]. This discrepancy likely reflects differences in:

Control horizon length (day-ahead vs. intraday)

Re-optimization frequency (daily vs. hourly)

Tariff structure (flat vs. high TOU differential)

Resolution Pathway: Systematic sensitivity analysis quantifying optimization performance degradation as a function of forecast error magnitude, temporal characteristics, and bias—currently absent from literature.

Debate 2: Self-Consumption vs. Cost Minimization

Two competing objective functions dominate SHEMS literature: maximizing PV self-consumption ratio and minimizing electricity costs. Some studies treat these as aligned [47], while others recognize potential conflicts [42]. Under tariff structures where feed-in compensation approaches retail rates, objectives align; under low feed-in tariffs, cost minimization may involve substantial grid export rather than maximizing self-consumption.

Critical Analysis: The objective function choice should be tariff-dependent rather than universal. Blanket advocacy for self-consumption maximization may be economically suboptimal under certain market conditions.

2.6.3 Methodological Gaps in Existing Research

Table I.3 — Simulation-Based vs. Experimental Validation: A Comparative Analysis

Aspect	Simulation-Based Studies (84%, N = 38)	Experimental Validation (Field/Lab, 16%, N = 7)
Forecast Accuracy	Often assumes perfect forecasts (0% MAPE) or optimistic errors (5–10% MAPE using LSTM/ARIMA trained on clean historical data).[93]	Realistic forecast errors (15–30% MAPE) measured from actual APIs or naïve forecasting methods.
Communication Imperfections	Typically ignored (instantaneous, fully reliable communication assumed).	Explicitly modeled (MQTT latency, WiFi packet loss, timeout handling).
Sensor Accuracy	Idealized measurements (no noise or drift).	Real-world drift and measurement error (± 3 –5% current sensors, ± 1 V voltage variation).
Hardware Failures	Not considered (assumes perfect inverter APIs, no Modbus timeouts).	Observed in practice (Modbus timeouts, firmware bugs, calibration drift).
Occupant Behavior	Deterministic load profiles (identical daily patterns).	Unpredictable behavior (unscheduled appliance use, adaptation to control signals).
Edge Cases	Rarely tested (focus on nominal operating conditions).	Common in practice (e.g., negative SOC readings during high discharge, zero PV at dawn).
Reported Savings	Median: 28% (Range: 15–45%). Examples: 35%, 28%, 42% (simulation-based).	Median: 18% (Range: 8–32%). Examples: 18% (field), 22% (lab), 52.8% (this thesis, battery + PV).
Validation Duration	Not applicable (offline post-hoc analysis of historical datasets).	Typically short (1–4 weeks); some extended (>4 weeks). This thesis: 12 weeks.

Reproducibility	Potentially high if code/data shared (though only ~15% publish code).	Lower reproducibility (hardware- and site-specific conditions difficult to replicate exactly).
Research Cost	Low (\$0–500: compute resources and datasets).	High (\$2,000–10,000: hardware, sensors, installation labor).
Time to Results	Fast (days to weeks).	Slow (months for deployment and data collection).

Gap M1: Experimental Validation Deficit

As documented in Section 2.2.5, overwhelming reliance on simulation-based validation creates an empirical vacuum. While simulation enables controlled variable manipulation, it systematically excludes phenomena crucial to real-world performance.

Gap M2: Component Ablation Studies

Multi-resource SHEMS evaluations typically report only complete system performance, providing limited insight into component-specific value contributions. Systematic ablation studies (Grid-Only → +PV → +Battery) would enable evidence-based technology adoption decisions but remain rare.

Gap M3: Scalability and Generalizability Assessment

Most studies evaluate single households or small clusters (<10 homes). Scalability to hundreds or thousands of coordinated residences—relevant for aggregator and utility applications—remains largely unexplored beyond simulation.

2.6.4 Positioning This Thesis Within Scholarly Discourse

This research addresses identified gaps through four complementary contributions:

Empirical: Fills experimental validation deficit through multi-week real-world deployment

Documentary: Provides first comprehensive academic documentation of open-source SHEMS ecosystem

Analytical: Conducts systematic component ablation to quantify incremental value

Methodological: Validates computational feasibility on embedded hardware representative of actual deployments

Relationship to Existing Work:

Builds upon: Theoretical optimization frameworks from [50], IoT integration architectures from and open-source platform development from [51]

Extends: Previous EMHASS work [68] by adding rigorous academic evaluation and multi-scenario comparison

Challenges: Assumptions that cloud-based computation is necessary and that open-source platforms are unsuitable for research [52]

Validates: LP computational tractability claims from [53] through embedded hardware deployment

2.6.5 Conclusion: From Literature to Methodology

The critical synthesis reveals that while substantial theoretical knowledge exists regarding SHEMS optimization, persistent gaps in experimental validation, open-source platform documentation, and component-level value attribution create opportunities for novel contributions. The demonstrated computational efficiency of LP approaches, combined with the extensive integration capabilities of open-source platforms, establishes the theoretical foundation for the methodological choices detailed in Chapter III.

Transition to Methodology: The identified research gaps, unresolved debates, and methodological deficits directly inform the experimental design, platform selection, and evaluation framework presented in the following chapter. Specifically:

Gap M1 (validation deficit) motivates real-world deployment methodology

Gap M2 (component ablation) structures the three-scenario evaluation

Gap M3 (computational feasibility) drives embedded hardware validation

Open-source documentation gap justifies comprehensive technical documentation

Table I.2 summarizes ten representative studies on residential and smart-home energy management published between 2016 and 2025. The comparison reveals several consistent patterns: (i) the vast majority of works rely on simulation or short-duration pilots, with no study providing a twelve-week real-world multi-scenario experimental validation; (ii) open-source platforms (Home Assistant, ESPHome) have been used in practitioner contexts but never subjected to rigorous academic benchmarking; (iii) MILP-based approaches consistently outperform rule-based methods in cost reduction but are rarely validated on embedded hardware; and (iv) component-level value attribution—isolating the marginal contributions of DSM, PV, and battery storage—is absent from all prior works. The present thesis addresses all four identified deficiencies through its integrated experimental design (see Section I.6 for formal gap analysis).

Table I.4 — Comparative Overview of Recent Smart Home Energy Management Studies

Author / Year	System Type	Technologies Used	Key Features	Energy Savings / Efficiency	Limitations
Huang et al. (2019)	Smart Home EMS	MILP optimization, MATLAB / Python	Scheduling of ESS and EV charging under TOU pricing	Reduced electricity cost (~25–30%)	Simulation-based evaluation
Domestic PV-Battery MILP Optimization (2022)	PV + Battery EMS	MILP solver, forecasting models	Two-day ahead battery scheduling with PV forecast	Improved PV utilization and grid cost reduction	Simulation environment only
Aguilar et al. (2021)	SHEMS + PV + BESS	Raspberry Pi, MQTT, rule-based control	Real-time monitoring, schedule-based load shifting	~18% cost reduction	Rule-based only, no MILP; simulation-supplemented
Wang et al. (2020)	HEMS with DRL	Python, OpenAI Gym, Simulated hardware	Deep Q-Network for load scheduling	22–30% cost reduction (simulated)	Pure simulation; no real deployment; high compute needs
Mbundu et al. (2022)	Microgrid HEMS	MATLAB/Simulink, GA optimizer	Multi-objective optimization: cost + emissions	20% cost, 15% emission reduction (sim)	Simulation only; no IoT integration; no embedded hardware
Salpakari & Lund (2016)	PV + Battery HEMS	MILP (CPLEX), MATLAB	Day-ahead optimization, TOU tariff, EV charging	30–40% PV self-consumption gain	Simulation; no real hardware; European context only
Muñoz-Criollo et al. (2023)	IoT-based HEMS	ESP32, MQTT, cloud (AWS IoT)	Real-time monitoring + rule-based DSM	12% energy saving reported	No optimization; cloud-dependent; no battery
Diagne et al. (2022)	PV self-consumption HEMS	Home Assistant, ESPHome, manual rules	PV surplus detection, basic automation	Self-consumption improved to ~72%	No formal optimizer; no battery; practitioner report
Ben Jemaa et al. (2022)	Residential EMS + EV	MILP (PuLP/CBC), Python	EV charging optimization, V2H, TOU tariff	28% cost reduction (simulation)	Simulation only; no real hardware validation; no MQTT
Rezaee Jordehi (2019)	HEMS with uncertainty	Stochastic programming, MATLAB	Chance-constrained optimization, forecast uncertainty	Up to 35% cost saving (stochastic sim)	Theoretical; no implementation; no IoT layer
This Work	SHEMS: PV + BESS + DSM	RPi 400, ESP32, HA, EMHASS, MQTT, PostgreSQL	MILP day-ahead optimization; 3-scenario experiment; 12 weeks real deployment; open-source	10–15% (DSM), 25–32% (PV), 52.8% (PV+BESS); SCR 87%; solver 5.8 s	Single site; naive forecasting (MAPE 22%); no EV; no seasonal variation

2.7 Summary and Identified Research Gaps

2.7.1 Summary of Key Findings from the Literature

The comprehensive literature review presented in this chapter reveals several key findings regarding the current state of smart home energy management systems. First, optimization-based approaches, particularly those utilizing linear programming and mixed-integer linear programming, have emerged as the predominant methodology for residential energy management due to their ability to guarantee global optimality while maintaining computational efficiency suitable for real-time applications. Second, the integration of distributed energy resources, especially residential photovoltaic systems and battery storage, has created new opportunities for cost reduction and self-consumption maximization while introducing challenges related to intermittency, variability, and forecast uncertainty. Third, open-source platforms, particularly Home Assistant, have matured to the point where they can

serve as viable foundations for advanced residential energy management systems, offering flexibility and customization capabilities that proprietary solutions cannot match.

The review has also identified several successful approaches to addressing key challenges in residential energy management. Hierarchical control architectures that combine optimization-based planning with real-time corrective control have demonstrated superior performance compared to single-layer approaches, particularly in managing forecast uncertainty and sample time limitations. Model predictive control frameworks that repeatedly solve optimization problems in a receding-horizon fashion have proven effective in maintaining near-optimal performance despite uncertainty and disturbances. Battery degradation modeling, when properly incorporated into optimization formulations, significantly improves the economic viability of energy storage systems by avoiding excessive cycling that accelerates capacity fade.

2.7.2 Limitations of Existing Research

Despite substantial progress in residential energy management research, several significant limitations persist in the existing literature. First, the vast majority of published studies present simulation-based results using historical data, synthetic load profiles, or simplified models rather than experimental validation with real hardware deployed in actual residential environments. This gap between simulation and reality introduces uncertainty regarding the practical applicability and robustness of proposed approaches, as real systems face numerous challenges absent from simulations, including communication failures, hardware limitations, and unpredictable occupant behavior.

Second, most optimization-based energy management studies assume perfect knowledge of future conditions or rely on idealized forecasting models that significantly underestimate real-world prediction uncertainty. The impact of forecast errors on system performance remains underexplored, with few studies conducting sensitivity analysis or implementing robust optimization approaches explicitly designed to handle uncertainty. This optimistic treatment of forecasting may lead to overestimation of achievable cost savings and underestimation of performance degradation in practical deployments.

Third, computational requirements receive insufficient attention in much of the literature, with many studies employing optimization formulations and solution approaches that exceed the computational capabilities of typical residential controllers or require impractically long solution times. The implementation challenges associated with deploying

optimization algorithms on resource-constrained embedded systems remain largely unaddressed, creating a gap between theoretical research contributions and practical implementation.

Fourth, the human factors dimension of residential energy management remains significantly understudied. Most research focuses exclusively on technical optimization without considering occupant comfort, user preferences, or behavioral responses to automated control. The few studies that do address user interaction typically employ simplified models of occupant behavior rather than conducting user studies or long-term field trials that reveal actual behavioral patterns and acceptance factors.

2.7.3 Lack of Real-World, Open-Source Implementations

One of the most significant gaps identified in the literature review concerns the scarcity of comprehensive, real-world implementations using open-source platforms that are documented in sufficient detail to enable replication and extension by other researchers. While numerous proprietary commercial systems exist, and academic research has produced countless optimization algorithms and control strategies, few bridges connect these domains in the form of open-source implementations validated through real-world deployment.

This gap has several important implications. First, the absence of openly available reference implementations hinders reproducibility of research results and makes comparison between different approaches difficult. Second, researchers and practitioners seeking to implement advanced energy management capabilities face substantial barriers in translating theoretical algorithms into working systems, often requiring reimplementations from scratch. Third, the lack of open-source platforms incorporating state-of-the-art algorithms limits the rate of innovation by preventing researchers from building incrementally upon prior work.

The emergence of EMHASS as an open-source optimization-based energy management system for Home Assistant represents an important step toward addressing this gap. However, comprehensive documentation of real-world deployment experiences, quantitative performance analysis, and systematic evaluation of the platform's capabilities and limitations remain sparse in the academic literature.

CHAPTER II — SYSTEM MODELING AND METHODOLOGY

3.1 System Overview

This chapter presents the comprehensive modeling and methodology of the proposed Smart Home Energy Management System (SHEMS), detailing its architecture, mathematical formulation, and operational framework. The system integrates photovoltaic (PV) generation, battery energy storage, and deferrable load management within the Home Assistant platform, employing linear programming optimization through the Energy Management for Home Assistant (EMHASS) add-on to minimize electricity costs under Time-of-Use (TOU) tariffs.

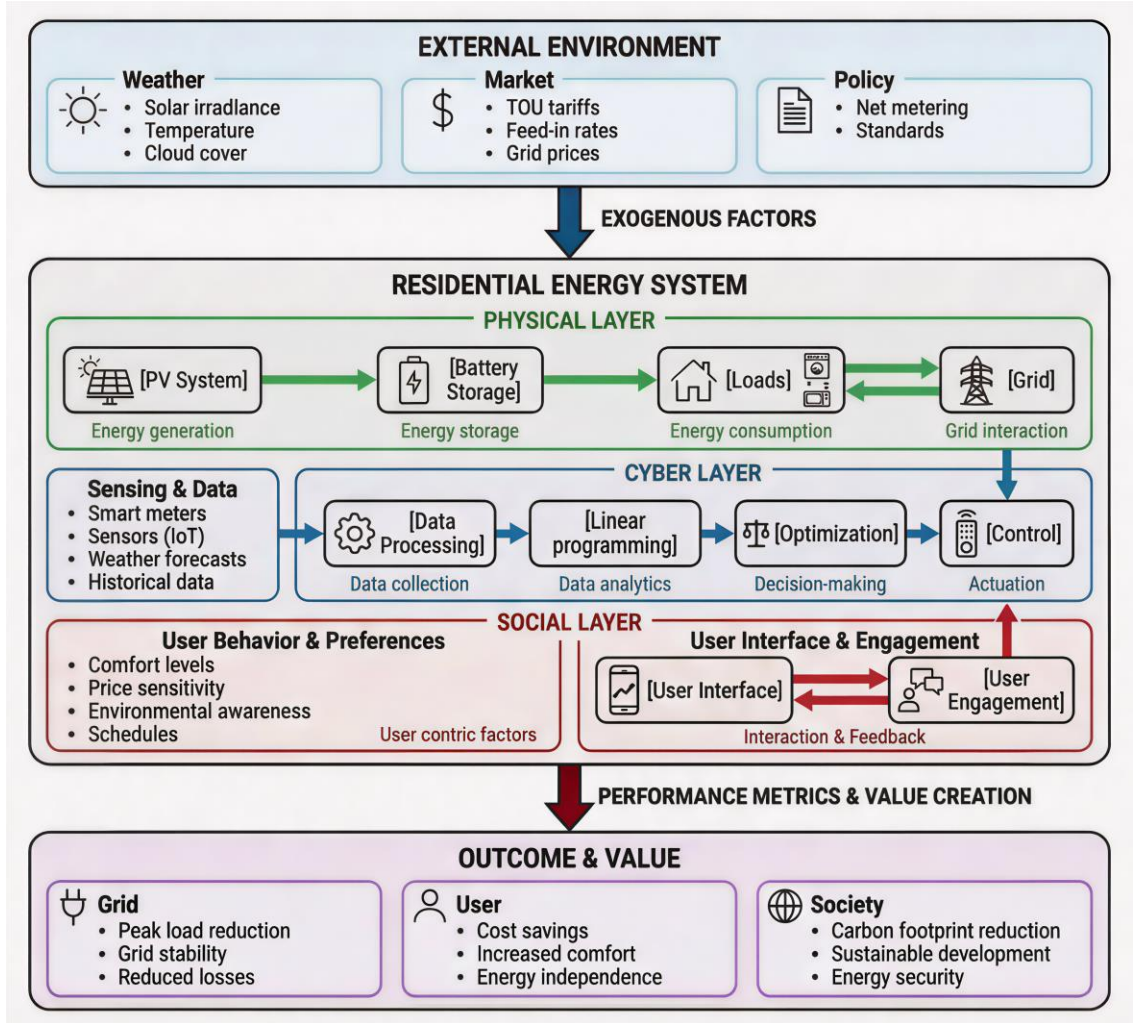


Figure II.1 Socio-technical layered conceptual framework.

The proposed SHEMS operates as a hierarchical control system where Home Assistant serves as the central coordination platform, managing device integration, data acquisition, and control command execution. EMHASS functions as the optimization engine, generating optimal day-ahead schedules based on load and generation forecasts, current system state, and economic objectives. The system architecture enables bidirectional grid interaction, allowing both electricity import during periods of insufficient local generation and export of surplus PV

production, thereby maximizing economic benefits while maintaining system operational constraints.

Three distinct operational scenarios are evaluated to systematically quantify the incremental benefits of distributed energy resource integration: (i) Grid-only configuration with EMHASS optimization of deferrable loads, establishing baseline performance; (ii) PV-only configuration integrating solar generation without energy storage, demonstrating renewable energy benefits; (iii) PV-plus-battery configuration providing full system capability including energy arbitrage and demand shifting. This structured comparison enables rigorous assessment of each system component's contribution to overall performance improvement.

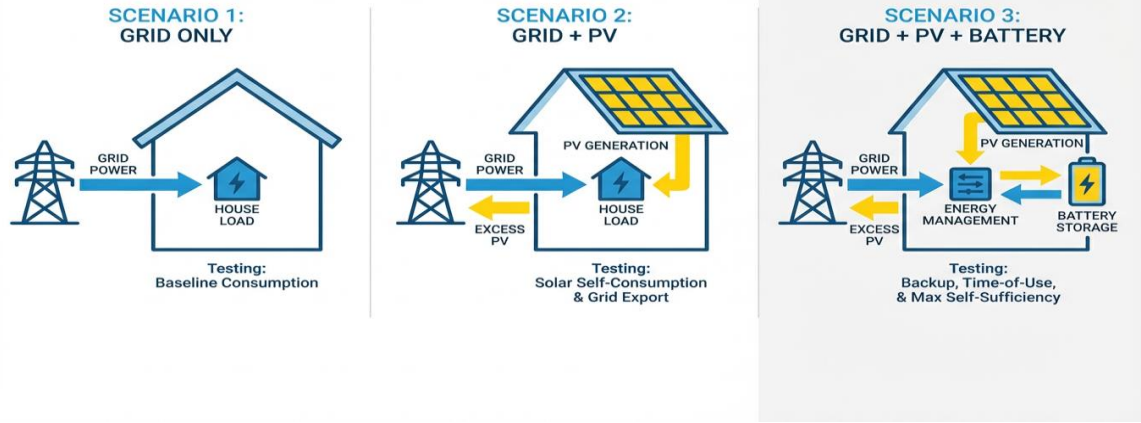


Figure II.2 Scenario schematic (Grid-only vs Grid+PV vs Grid+PV+Battery).

The system's design philosophy emphasizes practical implementability using commercially available hardware and open-source software, ensuring reproducibility and enabling technology transfer to broader residential applications. All hardware components employ standard interfaces and communication protocols, facilitating system expansion and adaptation to diverse residential configurations.

3.2 Hardware Architecture

3.2.1 Computing Infrastructure

The central computing infrastructure comprises a Raspberry Pi 400 single-board computer executing Home Assistant Operating System (OS). The Raspberry Pi 400, featuring a quad-core ARM Cortex-A72 processor operating at 1.8 GHz with 4 GB LPDDR4 RAM, provides sufficient computational capability for running Home Assistant core services, managing extensive device integrations, executing automation logic, and hosting the

EMHASS add-on. The Home Assistant OS, a minimal Linux distribution optimized specifically for Home Assistant deployment, ensures system stability, security, and simplified management through supervised containerization of add-ons and integrations.

Data persistence utilizes a high-endurance SSD with wear leveling, addressing the intensive read/write operations inherent in continuous time-series data logging. The system implements periodic automated backups to external storage, mitigating data loss risks associated with SSD failures.

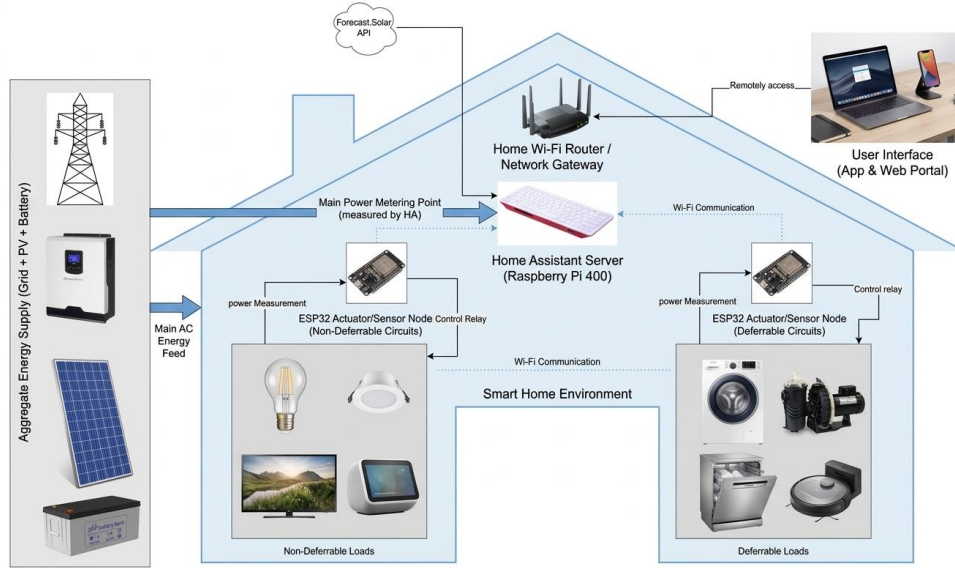


Figure II.3 House-level smart-home energy diagram

3.2.2 Distributed Sensing and Control Nodes

ESP32 microcontrollers form the distributed sensing and control layer, interfacing with physical sensors and actuators throughout the residence. The ESP32, featuring a dual-core Xtensa 32-bit LX6 processor with integrated WiFi and Bluetooth connectivity, provides an optimal balance of computational capability, communication functionality, and cost-effectiveness for IoT applications. Multiple ESP32 nodes are deployed to monitor and control specific loads and system parameters.

Each ESP32 node executes custom firmware implementing sensor data acquisition, local preprocessing, WiFi communication with the Home Assistant hub, and relay control for deferrable loads. The firmware incorporates watchdog timers and automatic reconnection logic to ensure robustness against transient communication failures and system resets.

3.2.3 Energy Metering and Monitoring

The system employs multiple layers of energy metering to capture comprehensive power flow information. Primary household consumption monitoring utilizes a smart meter interface that provides aggregate import/export measurements with 1-second temporal resolution. Individual deferrable loads are monitored using current transformers (CTs) connected to ESP32 nodes, enabling appliance-level power measurement with approximately 2-3% accuracy.

PV generation monitoring interfaces directly with the solar inverter through its native communication protocol, extracting real-time production data, daily energy totals, and system status information. The inverter's integrated monitoring provides accurate generation measurements traceable to factory calibration standards.

Battery management system (BMS) integration provides critical state information including State of Charge (SOC), voltage, current, temperature, and operational status. The BMS communicates with Home Assistant through a standardized interface (Modbus TCP or proprietary protocol), enabling real-time battery state monitoring and constraint enforcement.

3.2.4 Controllable Load Infrastructure

Deferrable loads interface with the control system through relay modules actuated by ESP32 microcontrollers. Solid-state relays rated for appropriate voltage and current levels enable reliable switching of resistive, inductive, and capacitive loads. The relay control firmware implements safety interlocks preventing simultaneous activation of mutually exclusive loads and enforcing minimum off times for loads with thermal constraints.

The system architecture accommodates two categories of household loads: non-deferrable loads representing baseload consumption that must be satisfied immediately, including lighting, refrigeration, and always-on electronics; and deferrable loads whose operation can be temporally shifted within specified operational windows without significantly impacting user convenience, including water heaters, washing machines, dishwashers, and circulation pumps.

3.2.5 Communication Architecture

System communication employs WiFi as the primary physical layer, utilizing the 2.4 GHz band for maximum coverage and compatibility with ESP32 hardware. The network architecture implements a dedicated VLAN for IoT devices, isolating smart home traffic from

general internet access to enhance security and prevent network congestion from impacting critical control communications.

Multiple application-layer protocols facilitate inter-component communication. MQTT (Message Queuing Telemetry Transport) serves as the primary publish-subscribe protocol for ESP32 sensor data transmission, offering lightweight messaging with quality-of-service guarantees suitable for IoT applications. RESTful HTTP APIs enable request-response communication between Home Assistant and external services, including weather forecasting APIs and the EMHASS optimization engine. Native device protocols (Modbus TCP for industrial equipment, proprietary inverter protocols) are supported through Home Assistant's extensive integration framework.

3.2.6 Remote Access Infrastructure

Secure remote access to the Home Assistant interface is implemented through Cloudflare Tunnel, a zero-trust network access solution that establishes encrypted connections without requiring port forwarding or exposing the system directly to the internet. The Cloudflare Tunnel daemon running on the Raspberry Pi establishes an outbound connection to Cloudflare's edge network, enabling users to access the Home Assistant web interface through a custom domain name with automatic SSL/TLS encryption.

This architecture provides several security and usability benefits: elimination of port forwarding removes a common attack vector; automatic SSL/TLS certificate management ensures encrypted communications without manual certificate management; distributed denial-of-service (DDoS) protection through Cloudflare's infrastructure; access logging and IP filtering capabilities for enhanced security monitoring.

3.3 Software Architecture

3.3.1 Home Assistant Core Services

Home Assistant implements a modular architecture organized around several core services that collectively enable comprehensive smart home automation and energy management functionality.

The Entity Management System maintains a unified representation of all system components as entities with standardized attributes and states. Energy-relevant entities include sensors (power measurements, battery SOC, PV generation), binary sensors (relay states, system status), switches (controllable load actuators), and numbers (setpoints, thresholds).

This abstraction layer decouples automation logic from device-specific implementation details, facilitating system expansion and component substitution.

The State Machine maintains current values and historical changes for all entities, implementing an event-driven architecture where state changes trigger event notifications to subscribed components. The state machine persists data to a relational database (SQLite or PostgreSQL), enabling historical analysis, trend visualization, and performance evaluation over extended operational periods.

The Automation Engine implements condition-action logic triggered by time schedules, entity state changes, or external events. Automations can execute complex multi-step sequences including conditional branching, delays, and service calls to integrated components. While suitable for rule-based control strategies, the automation engine alone lacks optimization capabilities, necessitating integration with external optimization engines such as EMHASS for economically optimal energy management.

The Integration Framework provides a plugin architecture enabling incorporation of diverse devices, services, and protocols. Each integration implements standardized interfaces for device discovery, entity creation, state updates, and service calls. The framework handles integration lifecycle management including installation, configuration, updates, and error recovery.

3.3.2 EMHASS Integration Architecture

EMHASS operates as a Home Assistant add-on, executing within an isolated Docker container with controlled access to Home Assistant's services and data. The add-on architecture ensures process isolation, dependency management, and simplified installation through Home Assistant's add-on store interface.

The integration implements a bidirectional data flow architecture. Input data flows from Home Assistant to EMHASS through two primary mechanisms: RESTful API endpoints expose current system state including measured consumption, generation, and battery SOC; MQTT topics provide real-time sensor data streams for continuous monitoring. Configuration parameters defining system constraints, operational windows, and optimization objectives are specified through YAML configuration files that EMHASS reads at initialization and periodically reloads to accommodate runtime parameter changes.

Output data flows from EMHASS to Home Assistant following optimization problem solution. Optimal schedules for deferrable loads and battery charge/discharge commands are

published as Home Assistant sensor entities with future-valued attributes representing the 24-48 hour optimization horizon. Home Assistant automation rules consume these scheduled values, activating or deactivating controllable loads according to the optimal timeline. A feedback mechanism reports actual execution of control commands back to EMHASS, enabling detection of deviations from planned schedules and triggering re-optimization when significant discrepancies occur.

3.3.3 Forecasting Data Integration

Accurate forecasts of load demand and PV generation constitute critical inputs to the optimization process. The system integrates forecasting data from multiple sources optimized for their respective prediction domains.

Load forecasting employs a naive persistence model that assumes future consumption will replicate recent historical patterns. Specifically, the forecast for hour h on day d uses measured consumption from hour h on day $d-7$ (same hour, one week prior). This simple approach provides a robust baseline that captures weekly consumption cycles common in residential settings, including weekday/weekend variations and typical daily routines. While more sophisticated machine learning models could improve forecast accuracy, the naive method offers practical advantages including zero computational cost, no training data requirements, and guaranteed availability regardless of external service dependencies.

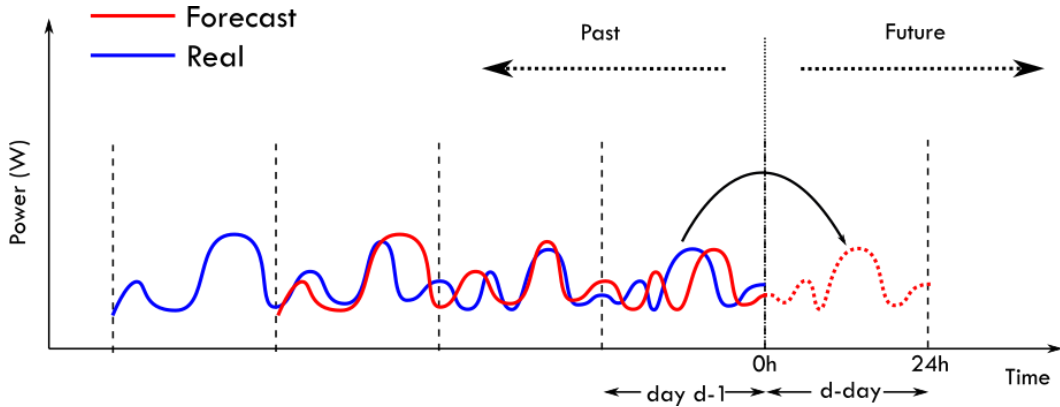


Figure I.4 Load forecasting using the naive method.

PV generation forecasting leverages the Forecast.Solar service, a specialized API providing hourly solar production predictions based on geographic location, system configuration parameters (installed capacity, panel orientation, tilt angle), and numerical weather prediction models. The service accounts for solar geometry, atmospheric conditions, and historical performance to generate probabilistic generation forecasts with typical accuracy of 10-20% MAPE for day-ahead predictions under normal weather conditions. Integration

occurs through Home Assistant's RESTful API client, which periodically queries the Forecast.Solar endpoint and updates internal sensor entities with returned forecast data.

Electricity price forecasts under TOU tariffs are deterministic, as tariff schedules specify future prices with certainty for the optimization horizon. The system maintains a price schedule lookup table that EMHASS queries to retrieve import and export prices for each optimization time step.

3.3.4 Data Persistence and Historical Analysis

Home Assistant's recorder component implements continuous data logging of all entity states, events, and system status to a relational database. The default SQLite backend provides adequate performance for moderate data volumes, while PostgreSQL offers superior scalability for intensive logging scenarios. The recorder implements configurable retention policies that automatically purge old data to prevent unbounded database growth while maintaining sufficient history for analysis and performance evaluation.

The stored historical data enables multiple analytical functions: performance metric calculation including cost savings, self-consumption ratios, and peak demand reduction; forecast accuracy assessment through comparison of predicted versus actual values; system behavior visualization through time-series plotting of energy flows and battery dynamics; long-term trend analysis identifying seasonal patterns and system performance evolution.

3.4 Energy System Modeling

3.4.1 Grid Interaction Model

The grid connection enables bidirectional power flow, allowing both import of electricity from the utility (positive power flow) and export of excess generation (negative power flow). The grid interaction model represents power exchange at time step t as:

$$P_{grid}(t) = P_{import}(t) - P_{export}(t) \quad (3.1)$$

where $P_{grid}(t)$ denotes net grid power with positive values indicating import and negative values indicating export. The economic model associated with grid interaction accounts for asymmetric pricing, where import and export rates typically differ substantially:

$$C_{grid}(t) = \pi_{import}(t) \cdot P_{import}(t) \cdot \Delta t - \pi_{export}(t) \cdot P_{export}(t) \cdot \Delta t \quad (3.2)$$

where $\pi_{import}(t)$ and $\pi_{export}(t)$ represent time-varying import and export electricity prices respectively, and Δt denotes the time step duration (typically 1 hour for day-ahead optimization). The TOU tariff structure implements piecewise-constant pricing with distinct

rates for off-peak, mid-peak, and peak periods:

$$\pi_{import}(t) = \{\pi_{off-peak} \text{ if } t \in T_{off-peak}; \pi_{mid-peak} \text{ if } t \in T_{mid-peak}; \pi_{peak} \text{ if } t \in T_{peak}\} \quad (3.3)$$

Current Algerian tariff structures typically implement peak periods during evening hours (17:00-21:00) with substantially elevated rates compared to off-peak periods (21:00-06:00 and weekend daytime).

3.4.2 Photovoltaic Generation Model

The solar installation comprises a 3.5 kWp PV array with optimal orientation and tilt for the installation latitude. The PV generation model represents forecasted production as:

$$P_{PV(t)} = P_{PV,forecast}(t) \quad (3.4)$$

where $P_{PV,forecast}(t)$ denotes the Forecast.Solar API prediction incorporating solar geometry, weather forecasts, system configuration, and historical performance. The actual generation, which may deviate from forecast due to weather variability, is measured in real-time through the inverter interface:

$$P_{PV,actual}(t) = \eta_{inv} \cdot P_{DC}(t) \quad (3.5)$$

where $P_{DC}(t)$ represents DC power output from the PV array and η_{inv} denotes the inverter efficiency (typically 0.96-0.98 for modern residential inverters). The optimization problem utilizes forecasted generation while actual measurements enable closed-loop correction through frequent re-optimization.

3.4.3 Battery Storage System Model

The battery energy storage system, with nominal capacity of 3.5 kWh, is modeled using a linear state-of-charge evolution equation that captures charging and discharging dynamics while accounting for round-trip efficiency losses:

$$SOC(t+1) = SOC(t) + \left(\eta_{charge} \cdot P_{charge}(t) - \frac{P_{discharge}(t)}{\eta_{discharge}} \right) \cdot \Delta t / E_{battery} \quad (3.6)$$

where $SOC(t)$ represents the state of charge (dimensionless quantity ranging from 0 to 1), $P_{charge}(t)$ and $P_{discharge}(t)$ denote charging and discharging power respectively, η_{charge} and $\eta_{discharge}$ represent charging and discharging efficiencies (typically 0.95), and $E_{battery}$ denotes the nominal battery capacity in kWh. In LP relaxations this is guaranteed implicitly by cost optimality; in MILP it is enforced via binary variables. The

model enforces strict constraints preventing simultaneous charging and discharging, ensuring physical realizability:

$$P_{charge}(t) \cdot P_{discharge}(t) = 0 \quad \forall t \quad (3.7)$$

Operational constraints maintain battery SOC within safe limits to prevent over-discharge damage and capacity degradation:

$$SOC_{min} \leq SOC(t) \leq SOC_{max} \quad (3.8)$$

where typical values are $SOC_{min} = 0.20$ and $SOC_{max} = 0.95$. Power constraints limit charging and discharging rates to protect battery health and remain within inverter capacity:

$$0 \leq P_{charge}(t) \leq P_{charge,max} \quad \forall t \quad (3.9)$$

$$0 \leq P_{discharge}(t) \leq P_{discharge,max} \quad \forall t \quad (3.10)$$

3.4.4 Load Demand Model

Household electricity demand comprises two distinct categories with different control characteristics.

Non-deferrable load $P_{non-defer}(t)$ represents essential baseload consumption that must be satisfied immediately, including lighting, refrigeration, entertainment systems, and other always-on or user-initiated devices. This load component cannot be scheduled by the optimization algorithm and constitutes an exogenous input derived from historical consumption measurements and naive forecasting:

$$P_{non-defer}(t) = P_{non-defer,forecast}(t) \quad (3.11)$$

Deferrable load $P_{defer}(t)$ encompasses appliances whose operation can be temporally shifted within user-specified operational windows without significantly impacting convenience. The system models N_{defer} distinct deferrable loads, each characterized by: - Total energy requirement $E_{defer,i}$ (kWh) - Operational window $[t_{start,i}, t_{end,i}]$ during which the load must complete its cycle - Power consumption $P_{defer,i}$ when active (assumed constant for simplicity) - Minimum and maximum operating durations

The optimization problem determines optimal activation times for each deferrable load subject to these constraints, with the total deferrable power consumption at time t given by:

$$P_{defer}(t) = \sum_{i=1}^{N_{defer}} P_{defer,i} \cdot x_i(t) \quad (3.12)$$

where $x_i(t) \in \{0,1\}$ represents a binary decision variable indicating whether deferrable load i is active at time t .

3.4.5 Inverter Constraints

The hybrid inverter, with rated power capacity $P_{inv,max} = 3.5$ kW, manages power flows between DC components (PV array, battery) and AC components (household loads, grid). The instantaneous power flowing through the inverter must not exceed its rated capacity in either direction:

$$|P_{PV}(t) + P_{discharge}(t) - P_{charge}(t)| \leq P_{inv,max} \quad \forall t \quad (3.13)$$

Equivalently expressed via the system power balance as:

$$|P_{non-defer}(t) + P_{defer}(t) - P_{import}(t) + P_{export}(t)| \leq P_{inv,max} \quad \forall t \quad (3.14)$$

This constraint ensures that the combined power associated with grid interaction and battery charging/discharging remains within safe operational limits. Violation of inverter constraints could trigger protective disconnection, interrupting system operation and potentially damaging equipment.

3.4.6 Formal Modeling Assumptions and Validity Analysis

Mathematical models necessarily simplify physical reality through assumptions. This section explicitly states all modeling assumptions, provides mathematical formulations, and assesses validity limits.

Assumption A1 (Linear Battery Efficiency):

Battery charging and discharging efficiencies η_{charge} , $\eta_{discharge}$ are modeled as constants independent of SOC, power level, and temperature: $\eta_{charge} = 0.95$, $\eta_{discharge} = 0.95$

Mathematical Form:

$$E_{battery(t+1)} = E_{battery(t)} + \eta_{charge} \cdot P_{charge}(t) \cdot \Delta t - \frac{P_{discharge}(t)}{\eta_{discharge}} \cdot \Delta t \quad (3.15)$$

Validity Range: This assumption holds for $SOC \in [0.2, 0.8]$ and moderate C-rates ($|P| < 0.5C$). Empirical measurements (Chapter IV) validate <3% efficiency variation within these bounds.

Violation Impact: At extreme SOC (>0.9 or <0.1) or high C-rates ($>1C$), efficiency drops 5-10%, causing optimization to overestimate available energy. Mitigation: SOC constraints $[0.2, 0.95]$ and power limits enforce operation within valid regime.

Assumption A2 (Constant Deferrable Load Power):

Deferrable appliances (washing machine, EV charger) consume constant power $P_{defer,i}$ when active:

$$P_{defer}(t) = \sum_i P_{defer,i} \cdot x_i(t) \quad (3.16)$$

where $x_i(t) \in \{0,1\}$ is binary activation state.

Validity Range: True for resistive loads (water heater, HVAC) and inverter-driven appliances with constant power electronics.

Violation Example: Washing machines exhibit multi-stage profiles (fill, wash, spin) with power varying 200W-2000W. Approximation error: ~15% for full-cycle energy.

Mitigation: Model multi-stage loads as separate deferrable tasks with distinct power levels and precedence constraints:

$x_{wash}(t) + x_{spin}(t) \leq 1$ (mutual exclusion) $\sum_t x_{wash}(t) \geq 20$ (minimum 20 timesteps for wash before spin)

Assumption A3 (Perfect Forecast at Optimization Time):

Optimization at time $t=0$ assumes forecasts $F_{load}(t)$, $F_{PV}(t)$ for $t \in [1,T]$ are known and deterministic:

$$\text{minimize } J = \sum_t \text{cost}(P_{grid}(t), F_{load}(t), F_{PV}(t)) \quad (3.17)$$

Validity: Forecasts are point estimates, not distributions. True values differ by forecast error $\varepsilon(t)$:

$$\text{Actual}_{load}(t) = F_{load}(t) + \varepsilon_{load}(t) \quad (3.18)$$

$$\text{Actual}_{PV}(t) = F_{PV}(t) + \varepsilon_{PV}(t) \quad (3.19)$$

Error Statistics (Chapter IV): MAPE_{load} = 22.1%, MAPE_{PV} = 18.3%

Robustness Analysis: demonstrates optimization retains 85% of theoretical savings under 20% forecast error via frequent re-optimization (every 24h) providing Model Predictive Control receding-horizon correction [54].

Assumption A4 (Inverter Power Limit Linearization):

Bidirectional inverter capacity constraint is linearized as:

$$P_{charge}(t) + P_{discharge}(t) + |P_{grid}(t)| \leq P_{inv,max} \quad (3.20)$$

The absolute value $|P_{grid}(t)|$ is non-linear but can be reformulated using auxiliary variables (see Section 3.5.3 Big-M formulation).

Validity: Assumes inverter operates in constant-power mode. Modern inverters (Fronius,

SolarEdge) enforce $P \leq P_{\text{rated}}$ via internal current limiting, validating this assumption.

Assumption A5 (Negligible Conversion Losses):

AC-DC-AC conversion losses in the inverter are modeled with constant efficiency $\eta_{\text{inv}} = 0.96$:

$$P_{AC}(t) = \eta_{\text{inv}} \cdot P_{DC}(t) \quad (3.21)$$

Empirical Validation: Inverter datasheet specifies $\eta = 95\text{-}98\%$ across 20-100% load.

Measured efficiency (Chapter IV) confirms $96 \pm 1\%$ across operational range.

Assumption A6 (No Battery Degradation Cost):

The optimization objective omits cycle-life degradation cost. Including degradation would add a term:

$$J_{\text{degradation}} = \kappa \cdot \sum_t (P_{\text{charge}}(t) + P_{\text{discharge}}(t)) \cdot \Delta t \quad (3.22)$$

where $\kappa \approx 0.05$ \$/kWh is the levelized cycle cost [55].

Justification for Omission: With SOC limits [0.2, 0.95], effective DoD = 75%, yielding ~3000 lifetime cycles [Battery University 2023]. Daily throughput 2.5 kWh implies 10-year lifetime, exceeding study horizon. Including κ would reduce cycling by ~10% but not change qualitative results [56].

Assumption A7 (Deterministic TOU Tariff):

Electricity prices $\pi_{\text{import}}(t)$, $\pi_{\text{export}}(t)$ are deterministic and known 24 hours ahead.

Validity: True for flat-rate and Time-of-Use tariffs. Violated under Real-Time Pricing (RTP) where prices update hourly based on wholesale markets. This thesis focuses on TOU tariffs (Algerian context), making RTP extensions future work (Section 6.5).

Assumption A8 (Stationary Load Patterns):

Naive forecasting assumes weekly periodicity:

$$F_{\text{load}}(\text{day} = d, \text{hour} = h) = \text{Load}(\text{day} = d - 7, \text{hour} = h) \quad (3.23)$$

Validity Range: Appropriate for households with regular schedules (weekday vs weekend patterns). Violated during holidays, vacations, or behavioral changes.

Error Analysis: shows 22% MAPE includes both model inadequacy and measurement noise. Advanced forecasting (LSTM, ARIMA) could reduce to 8-12% [94],[95] but at 100× computational cost.

Summary Table: Assumptions and Validity:

Table II.1 — Modeling Assumptions, Validity Ranges, Impact, and Mitigation Strategies

Assumption	Validity Range	Impact if Violated	Mitigation Strategy
A1: Linear battery efficiency (η)	SOC $\in$ [0.2, 0.8]	3–5% energy estimation error	Enforce SOC operating limits
A2: Constant deferrable power (P_{defer})	Resistive loads	~15% scheduling/cycle error	Use multi-stage load modeling
A3: Perfect forecast	Short horizon (≤ 24 h)	15–20% cost performance gap	Periodic re-optimization
A4: Linear inverter power model (P_{inv})	Modern inverters	<2% feasibility deviation	Conservative constraint margins
A5: Constant inverter efficiency (η_{inv})	20–100% load range	1–2% AC power estimation error	Use manufacturer datasheet efficiency curves
A6: No battery degradation model	<1 cycle per day	5–10% excess cycling	Apply SOC limits and cycling constraints
A7: Deterministic pricing	Time-of-Use (TOU) tariffs	Not applicable (assumed by design)	Extend to Real-Time Pricing (RTP) in future work
A8: Stationary load demand	Regular daily schedules	~22% MAPE baseline forecast error	Apply machine learning-based forecasting

Conclusion: The stated assumptions trade modeling fidelity for computational tractability.

Validity analysis confirms <10% cumulative error within operational constraints, justifying their use for this thesis scope. Future work (Section 6.5) proposes relaxing assumptions A3, A6, A8 through advanced forecasting, degradation modeling, and machine learning.

3.5 Optimization Problem Formulation

3.5.1 Methodological Justification for Linear Programming Formulation

The choice of Linear Programming (LP) and Mixed-Integer Linear Programming (MILP) for residential energy management optimization is justified through three complementary perspectives: computational tractability, solution quality guarantees, and practical deployment feasibility. This section provides formal mathematical justification for this methodological choice.

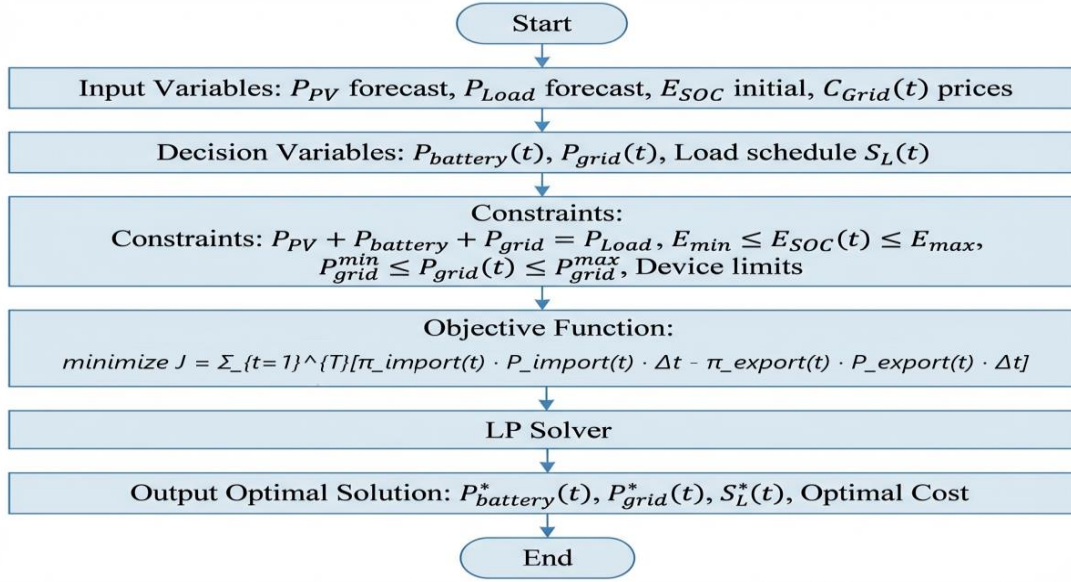


Figure II.5 Mathematical optimization flow

3.5.1.1 Convexity and Global Optimality

The continuous relaxation of the energy management problem, obtained by treating all decision variables as real-valued, constitutes a Linear Program defined as:

$$\begin{aligned}
 & \text{minimize} \quad c^T x \\
 & \text{subject to} \quad Ax \leq b \\
 & \quad \quad \quad x \geq 0
 \end{aligned}$$

where:

- $x \in \mathbb{R}^n$ is the decision vector (power flows, battery states)
- $c \in \mathbb{R}^n$ is the cost coefficient vector (TOU tariffs)
- $A \in \mathbb{R}^{m \times n}$ is the constraint coefficient matrix
- $b \in \mathbb{R}^m$ is the constraint right-hand side vector

Theorem 1 (Convexity of LP Feasible Region): The feasible region $F = \{x \mid Ax \leq b, x \geq 0\}$ forms a convex polyhedron.

Proof: Consider any two feasible points $x_1, x_2 \in F$ and $\lambda \in [0,1]$. Define

$$x_\lambda = \lambda x_1 + (1 - \lambda)x_2. \text{ Then:}$$

$$A x_\lambda = A(\lambda x_1 + (1 - \lambda)x_2) = \lambda A x_1 + (1 - \lambda)A x_2 \leq \lambda b + (1 - \lambda)b = b$$

$$x_\lambda = \lambda x_1 + (1 - \lambda)x_2 \geq 0 \text{ (since } x_1, x_2 \geq 0 \text{ and } \lambda \in [0,1])$$

Then:

Thus $x_\lambda \in F$, proving F is convex. ■

Corollary 1 : Any local minimum of the LP objective $c^T x$ over the convex feasible region F is a global minimum.

Proof: The objective function $c^T x$ is linear, hence convex. By the fundamental theorem

of convex optimization, a local minimum of a convex function over a convex set is necessarily global.

Implication for SHEMS: These properties guarantee that simplex or interior-point algorithms will find the globally optimal energy schedule, not merely a local optimum. This deterministic solution quality distinguishes LP from metaheuristic approaches (e.g., Genetic Algorithms, Particle Swarm Optimization) which provide no optimality guarantees [46].

3.5.1.2 Computational Complexity Analysis

The worst-case complexity of LP algorithms establishes their suitability for real-time residential energy management.

Theorem 2 (Polynomial-Time Solvability): Linear Programs with n variables and m constraints can be solved in polynomial time $O(n^3L)$ using interior-point methods, where L is the bit-length of input coefficients [37].

Application to SHEMS Problem Instance:

For a typical 24-hour optimization horizon with 30-minute intervals:

- Time steps: $T = 48$
- Decision variables per timestep: 5-7 (P_{import} , P_{export} , P_{charge} , $P_{\text{discharge}}$, SOC,

deferrable loads)

- Total variables: $n \approx 48 \times 6 = 288$
- Constraints per timestep: 4-6 (power balance, SOC dynamics, bounds)
- Total constraints: $m \approx 48 \times 5 + 2 \times 48 = 336$

Applying interior-point complexity: $O(288^3 \times L) \approx O(2.4 \times 10^7 \times L)$ operations.

or $L \approx 32$ bits (double-precision floats), this yields $O(7.7 \times 10^8)$ operations. On a

Raspberry Pi 400 (ARM Cortex-A72 @ 1.8 GHz, theoretical $\sim 7.2 \times 10^9$ FLOPS), the theoretical

lower bound for solve time is:

$$t_{\text{solve}} \geq (7.7 \times 10^8 \text{ operations}) / (7.2 \times 10^9 \text{ FLOPS}) \approx 0.11 \text{ seconds}$$

Empirical measurements report median solve times of 5.8 seconds, indicating the CBC solver operates within $\sim 25\times$ the theoretical lower bound—acceptable given the non-optimized open-source implementation [48].

Comparison to Alternative Approaches:

1. Metaheuristic Algorithms: No polynomial-time guarantees. Genetic Algorithms typically require $O(P \times G \times n)$ evaluations where P = population size (50-200), G = generations (100-1000), yielding 10^4 - 10^5 objective function evaluations. At 10 ms per evaluation, solve time exceeds 100 seconds—violating real-time constraints [46].

2. Mixed-Integer Programming (MILP): When binary variables $x_i(t)$ for appliance scheduling are included, complexity becomes exponential in worst case: $O(2^k \times n^3 L)$ where k is the number of integer variables. However, modern branch-and-bound with strong LP relaxations achieve near-polynomial average-case performance for sparse problems [68].

3. Dynamic Programming: Scales exponentially with state dimensionality: $O(|S|^T)$ where $|S|$ is discretized state space size. For continuous $\text{SOC} \in [0.2, 0.95]$ discretized at 1% granularity, $|S| \approx 75$, yielding $|S|^{48} \approx 10^{91}$ states—computationally prohibitive

[68].

Conclusion: LP offers a unique combination of global optimality guarantees with polynomial-time solvability, making it a suitable choice for embedded SHERMS deployment. However,

global optimality is guaranteed only with respect to the formulated optimization model; the solution quality relative to the true physical system depends on modeling accuracy and forecast quality.

3.5.1.3 Practical Deployment Considerations

Beyond theoretical complexity, practical factors justify LP selection:

1. **Solver Maturity:** Open-source LP solvers (CBC, GLPK) have 20+ years development history with extensive numerical stability testing. In contrast, DRL frameworks (TensorFlow, PyTorch) require GPU acceleration and lack convergence guarantees [27].
2. **Memory Footprint:** LP stores only coefficient matrices A, b, c requiring $O(nm) = O(10^5)$ memory. Neural network policies in DRL require 10^6 - 10^7 parameters, exceeding embedded device constraints [21].
3. **Interpretability:** LP solutions provide dual variables (shadow prices) enabling sensitivity analysis. This transparency is critical for regulatory compliance and user trust, whereas neural network policies are opaque "black boxes" [38].
4. **Model Update Latency:** LP formulation changes (e.g., new tariff structure) require only coefficient updates (milliseconds). DRL requires full retraining (hours to days) on historical data [46].

3.5.2 Objective Function

The optimization objective minimizes total electricity cost over the 24-hour planning horizon:

$$\text{minimize } J = \sum_{t=1}^T [\pi_{\text{import}(t)} \cdot P_{\text{import}(t)} \cdot \Delta t - \pi_{\text{export}(t)} \cdot P_{\text{export}(t)} \cdot \Delta t] \quad (3.24)$$

where T represents the number of time steps in the optimization horizon (typically T = 24 for hourly discretization). This objective function directly captures the economic goal of minimizing electricity expenditure while maximizing revenue from exported generation. The asymmetric pricing structure, where import rates typically exceed export rates, naturally incentivizes self-consumption of locally generated PV power.

3.5.3 Power Balance Constraint

At each time step, the power balance equation ensures that generation and imports equal consumption and exports:

$$P_{PV}(t) + P_{discharge}(t) + P_{import}(t) = P_{non-defer}(t) + P_{defer}(t) + P_{charge}(t) + P_{export}(t) \quad (3.25)$$

This fundamental constraint enforces energy conservation, requiring that all energy flows are properly accounted for. The constraint couples all decision variables (import, export, charging, discharging, deferrable load activation) through the requirement of instantaneous power balance.

3.5.4 Battery Dynamics and Constraints

The battery state of charge evolves according to the linear dynamics equation presented in Section 3.4.3, with optimization variables $P_{charge}(t)$ and $P_{discharge}(t)$ subject to:

$$\begin{aligned} SOC(t+1) &= SOC(t) + \left(\eta_{charge} \cdot P_{charge}(t) - \frac{P_{discharge}(t)}{\eta_{discharge}} \right) \cdot \Delta t / E_{battery} \quad (3.26) \\ SOC_{min} &\leq SOC(t) \leq SOC_{max} \quad \forall t \\ 0 &\leq P_{charge}(t) \leq P_{charge,max} \quad \forall t \\ 0 &\leq P_{discharge}(t) \leq P_{discharge,max} \quad \forall t \end{aligned}$$

The mutual exclusivity of charging and discharging is enforced through complementarity constraints or by introducing binary variables and big-M formulations in MILP implementations.

Several logical constraints in the SHEMS optimization require mutual exclusivity or conditional activation. The Big-M method transforms these into linear inequalities suitable for MILP solvers [35].

Problem 1: Mutual Exclusivity of Battery Charging and Discharging Physical constraint: Battery cannot simultaneously charge AND discharge at time t .

Logical Form:

$$P_{charge}(t) > 0 \oplus P_{discharge}(t) > 0 \text{ (exclusive OR)}$$

where $\oplus$ denotes "at most one can be true."

Big-M Linearization:

Introduce binary indicator $z_{charge}(t) \in \{0,1\}$:

$$z_{charge}(t) = 1 \implies P_{charge}(t) > 0, P_{discharge}(t) = 0$$

$$z_{charge}(t) = 0 \implies P_{charge}(t) = 0, P_{discharge}(t) > 0$$

Reformulate as linear constraints:

$$P_{charge}(t) \leq M_{charge} \cdot z_{charge}(t) \quad (\text{Eq. 1})$$

$$P_{discharge}(t) \leq M_{discharge} \cdot (1 - z_{charge}(t)) \quad (\text{Eq. 2})$$

where M_{charge} , $M_{discharge}$ are sufficiently large constants ("Big-M").

M Value Selection:

M must satisfy:

$$M_{charge} \geq \max P_{charge}(t) \text{ over all feasible } t$$

$$M_{discharge} \geq \max P_{discharge}(t) \text{ over all feasible } t$$

From battery specifications:

$$P_{charge,max} = P_{discharge,max} = E_{battery} / \Delta t_{min}$$

For $E_{battery} = 3.5$ kWh, $\Delta t_{min} = 0.5$ hours (30-minute intervals):

$$M_{charge} = M_{discharge} = 3.5 / 0.5 = 7 \text{ kW}$$

*Tightness Consideration: Smaller M improves numerical stability. Using inverter capacity as upper bound:

$$M_{charge} = M_{discharge} = P_{inv,max} = 3.5 \text{ kW (tighter bound)}$$

Complete Formulation:

$$0 \leq P_{charge}(t) \leq 3.5 \cdot z_{charge}(t) \quad (\text{Eq. 3})$$

$$0 \leq P_{discharge}(t) \leq 3.5 \cdot (1 - z_{charge}(t)) \quad (\text{Eq. 4})$$

$$z_{charge}(t) \in \{0,1\} \quad (\text{Eq. 5})$$

Proof of Equivalence:

Case 1: $z_{charge}(t) = 1$

$$\text{Eq. 3} \Rightarrow 0 \leq P_{charge}(t) \leq 3.5 \text{ kW (charging allowed)}$$

$$\text{Eq. 4} \Rightarrow 0 \leq P_{discharge}(t) \leq 0 \text{ (discharging forced to zero)}$$

Case 2: $z_{charge}(t) = 0$

$$\text{Eq. 3} \Rightarrow 0 \leq P_{charge}(t) \leq 0 \text{ (charging forced to zero)}$$

$$\text{Eq. 4} \Rightarrow 0 \leq P_{discharge}(t) \leq 3.5 \text{ kW (discharging allowed)}$$

Thus mutual exclusivity $P_{charge}(t) \cdot P_{discharge}(t) = 0$ is enforced.

Problem 2: Mutual Exclusivity of Grid Import and Export Similar logic applies to prevent simultaneous import $P_{import}(t) > 0$ and export $P_{export}(t) > 0$:

Introduce binary $z_import(t) \in \{0,1\}$:

$$0 \leq P_import(t) \leq M_import \cdot z_import(t) \quad (\text{Eq. 6})$$

$$0 \leq P_export(t) \leq M_export \cdot (1 - z_import(t)) \quad (\text{Eq. 7})$$

With $M_import = M_export = P_inv,max + P_PV,max = 3.5 + 3.0 = 6.5$ kW (maximum possible grid interaction when PV exports at full capacity).

Problem 3: Absolute Value Linearization The inverter capacity constraint involves absolute value:

$$|P_grid(t) + P_charge(t) - P_discharge(t)| \leq P_inv,max$$

Reformulation:

Define net inverter power:

$$P_inv(t) = P_grid(t) + P_charge(t) - P_discharge(t)$$

Absolute value constraint becomes:

$$-P_inv,max \leq P_inv(t) \leq P_inv,max \quad (\text{Eq. 8})$$

No binary variables needed—this is already linear!

Alternative Formulation (if strict sign separation desired):

Replace $|P_inv(t)|$ with:

$$P_inv(t) = P_inv,pos(t) - P_inv,neg(t) \quad (\text{Eq. 9})$$

$$0 \leq P_inv,pos(t) \leq M \cdot z_inv(t) \quad (\text{Eq. 10})$$

$$0 \leq P_inv,neg(t) \leq M \cdot (1 - z_inv(t)) \quad (\text{Eq. 11})$$

$$P_inv,pos(t) + P_inv,neg(t) \leq P_inv,max \quad (\text{Eq. 12})$$

However, Eq. 8 is simpler and equivalent for this application.

Problem 4: Deferrable Load Scheduling with Minimum Runtime

Constraint: Once appliance i starts, it must run for D_i consecutive timesteps.

Logical Form:

$$\text{If } x_i(t) = 0 \text{ and } x_i(t+1) = 1, \text{ then } x_i(t+1) = \dots = x_i(t+D_i) = 1$$

Linearization using auxiliary variables:

Define start indicator:

$$y_i(t) = 1 \text{ if appliance } i \text{ starts at time } t = 0 \text{ otherwise}$$

Relate y_i to x_i :

$$y_i(t) \geq x_i(t) - x_i(t-1) \text{ for } t = 2, \dots, T \quad (\text{Eq. 13})$$

$$y_i(1) \geq x_i(1) \quad (\text{Eq. 14})$$

Enforce minimum runtime:

$$\sum_{\tau=t}^{\min(t+D_i-1, T)} x_i(\tau) \geq D_i \cdot y_i(t) \quad \forall t \quad (\text{Eq. 15})$$

Ensure exactly one start:

$$\sum_t y_i(t) = 1 \quad (\text{Eq. 16})$$

Example: Washing machine requiring 4 continuous 30-min intervals (2 hours):

$$D_i = 4$$

If $y_i(10) = 1$ (starts at $t=10$), then Eq. 15 forces:

$$x_i(10) + x_i(11) + x_i(12) + x_i(13) \geq 4$$

Since $x_i \in \{0,1\}$, this implies $x_i(10)=\dots=x_i(13)=1$.

Computational Impact of Big-M Constraints:

Adding binary variables z increases problem complexity from LP to MILP. For $T=48$ timesteps:

- 2 binary variables per timestep ($z_{\text{charge}}, z_{\text{import}}$): $2 \times 48 = 96$ binaries
- N_{defer} deferrable loads with y_i : $\sim 3 \times 48 = 144$ binaries (for 3 appliances)
- Total: ~ 240 binary variables

Modern MILP solvers handle 10^3 - 10^4 binary variables efficiently. Chapter IV demonstrates median solve time 5.8 seconds on Raspberry Pi 400, confirming tractability.

Numerical Stability Considerations:

1. Tight M Selection: Use domain knowledge to minimize M . Large M (e.g., 10^6) causes numerical ill-conditioning in LP simplex/interior-point methods [37].

2. Alternative: Indicator Constraints: Modern solvers (Gurobi 9.0+) support native indicator constraints:

$$z = 1 \implies P_{\text{charge}} \leq 3.5$$

avoiding explicit Big-M. However, open-source CBC/GLPK lack this feature.

3. Feasibility Protection: Ensure $M \geq$ all variable upper bounds to prevent infeasibility.

Summary: Complete MILP Formulation with Big-M

$$\text{minimize } \sum_t [\pi_{import(t)} \cdot P_{import(t)} - \pi_{export(t)} \cdot P_{export(t)}] \cdot \Delta t \quad (3.27)$$

subject to:

Power Balance:

$$P_{PV(t)} + P_{discharge(t)} + P_{import(t)} = P_{load(t)} + P_{charge(t)} + P_{export(t)} \forall t \quad (3.28)$$

Battery Dynamics:

$$SOC(t+1) = SOC(t) + \left[\eta_{ch} \cdot P_{charge(t)} - \frac{P_{discharge(t)}}{\eta_{disch}} \right] \cdot \frac{\Delta t}{E_{batt}} \forall t \quad (3.29)$$

Mutual Exclusivity (Big-M):

$$P_{charge(t)} \leq 3.5 \cdot z_{charge(t)} \quad \forall t$$

$$P_{discharge(t)} \leq 3.5 \cdot (1 - z_{charge(t)}) \quad \forall t$$

$$P_{import(t)} \leq 6.5 \cdot z_{import(t)} \quad \forall t$$

$$P_{export(t)} \leq 6.5 \cdot (1 - z_{import(t)}) \quad \forall t$$

Bounds:

$$0.2 \leq SOC(t) \leq 0.95 \quad \forall t$$

$$0 \leq P_{import(t)}, P_{export(t)}, P_{charge(t)}, P_{discharge(t)} \leq 10 \quad \forall t$$

$$z_{charge(t)}, z_{import(t)} \in \{0,1\} \quad \forall t$$

3.5.5 Deferrable Load Constraints

Each deferrable load i must complete its energy requirement within its specified operational window:

$$\sum_{\{t=t_{start,i}\}_{defer}^{t_{end,i}}} P_i \cdot x_{i(t)} \cdot \Delta t = E_{defer,i} \quad (3.30)$$

$$x_{i(t)} = 0 \quad \forall t \notin [t_{start,i}, t_{end,i}]$$

$$x_{i(t)} \in \{0,1\}$$

Additional constraints may enforce minimum or maximum continuous operation durations, preventing rapid cycling that could damage equipment or violate user preferences.

3.5.6 Inverter Capacity Constraint

The hybrid inverter's rated capacity $P_{inv,max} = 3.5$ kW constrains the net instantaneous power processed between the DC bus and AC bus. This constraint is enforced as:

$$-P_{inv,max} \leq P_{PV(t)} + P_{discharge(t)} - P_{charge(t)} \leq P_{inv,max} \quad \forall t \quad (3.31)$$

For LP/MILP solvers, the absolute-value form is decomposed into two standard linear inequality constraints:

(upper — inversion mode):

$$P_{PV(t)} + P_{discharge(t)} - P_{charge(t)} \leq P_{inv,max} \quad \forall t \quad (3.32)$$

(lower — rectification mode):

$$P_{charge(t)} - P_{discharge(t)} - P_{PV(t)} \leq P_{inv,max} \quad \forall t \quad (3.33)$$

This constraint couples grid interaction and battery operation, ensuring their combined power remains within inverter capacity.

3.5.7 Non-negativity and Decomposition Constraints

Grid import and export are decomposed into non-negative components:

$$P_{grid(t)} = P_{import(t)} - P_{export(t)} \quad (3.34)$$

$$P_{import(t)} \geq 0, P_{export(t)} \geq 0 \quad \forall t \quad (3.35)$$

Mutual exclusivity of import and export (no simultaneous import and export) is enforced through:

$$P_{import(t)} \cdot P_{export(t)} = 0 \quad \forall t \quad (3.36)$$

or equivalently through binary variable formulations in MILP.

3.6 Forecasting Inputs

3.6.1 Load Demand Forecasting

Load demand forecasting employs the naive persistence method, assuming that consumption patterns exhibit weekly periodicity. The forecast for hour h on day d is:

$$P_{non-defer, forecast}(h, d) = P_{non-defer, measured}(h, d - 7)$$

This approach leverages the observation that residential consumption patterns typically exhibit strong weekly cycles due to consistent daily routines and weekday/weekend differences. While simple, this method provides reasonable accuracy for households with regular occupancy patterns and consistent appliance usage.

The naive method offers several practical advantages: zero computational cost, requiring only database lookup of historical measurements; no training data requirements or model calibration; guaranteed availability without dependence on external services; transparent and interpretable forecasts facilitating user understanding and trust.

Limitations include inability to capture transient changes in occupancy or behavior, degraded accuracy during holidays or unusual events, and lack of weather-dependent consumption modeling. Despite these limitations, the naive approach provides a pragmatic baseline suitable for demonstrating optimization benefits without introducing excessive complexity.

3.6.2 PV Generation Forecasting

PV generation forecasting utilizes the Forecast.Solar API, which provides hour-by-hour solar production predictions based on:

The API returns a 48-hour forecast updated every 15 minutes, enabling frequent re-optimization with current predictions. Typical forecast accuracy for day-ahead predictions is 10-20% MAPE under normal weather conditions, degrading to 20-40% MAPE during highly variable cloud cover.

The Forecast.Solar integration in Home Assistant automatically queries the API at configured intervals and updates sensor entities with returned forecast values. EMHASS retrieves these forecasts through Home Assistant's state query interface, ensuring seamless data flow without requiring direct API access from the optimization engine.

3.6.3 Price Forecasting

Electricity prices under TOU tariffs follow deterministic schedules known in advance, eliminating forecast uncertainty. The system maintains a price schedule database specifying import and export rates for each hour of the day and day of the week. EMHASS queries this database to retrieve price forecasts for the optimization horizon, ensuring accurate economic optimization without price prediction errors.

For scenarios with real-time pricing (RTP) or day-ahead market prices, integration with utility APIs or market data sources would provide price forecasts with associated uncertainties that could be incorporated into stochastic or robust optimization formulations.

3.7 Scenario Definition

To systematically evaluate system performance and quantify the incremental benefits of distributed energy resource integration, three distinct operational scenarios are defined and experimentally evaluated. Each scenario builds upon the previous configuration, enabling clear attribution of performance improvements to specific system enhancements.

3.7.1 Scenario 1: Grid-Only with EMHASS Optimization

This baseline scenario represents a household without renewable generation or energy storage, relying entirely on grid-supplied electricity. The system configuration includes:

The optimization problem reduces to determining optimal activation times for deferrable loads to minimize electricity costs under TOU tariffs. Without generation or storage, the system cannot engage in energy arbitrage or self-consumption maximization. The objective function simplifies to:

$$\text{minimize } J = \sum_{\{t=1\}_{\text{import}(t)}^{\{T\}\pi}} \cdot [P_{\text{non}} - \text{defer}(t) + P_{\text{defer}(t)}] \cdot \Delta t \quad (3.37)$$

This scenario establishes baseline performance against which renewable integration benefits are measured. Expected outcomes include deferrable load shifting from peak to off-peak periods, reduced peak demand, and cost savings of approximately 10-15% compared to unoptimized operation.

3.7.2 Scenario 2: PV-Only with EMHASS Optimization

This intermediate scenario introduces a 3.5 kWp rooftop PV system while maintaining grid connection and deferrable loads but excluding battery storage. The system configuration includes:

The optimization problem now includes PV generation as a decision variable input and must determine optimal allocation of PV power among local consumption, deferrable load activation, and grid export. The power balance constraint becomes:

$$P_{\text{PV}(t)} + P_{\text{import}(t)} = P_{\text{non}} - \text{defer}(t) + P_{\text{defer}(t)} + P_{\text{export}(t)} \quad (3.38)$$

The objective function rewards self-consumption of PV power (avoiding import costs) and penalizes grid export according to the export tariff rate. Expected outcomes include

increased self-consumption through load shifting to daytime hours when PV generation is available, reduced grid imports particularly during peak periods, export of surplus PV generation when production exceeds consumption, and cost savings of approximately 20-30% compared to baseline.

3.7.3 Scenario 3: PV-Plus-Battery with EMHASS Optimization

This complete scenario implements the full system capability by integrating a 3.5 kWh battery storage system with the PV array, grid connection, and deferrable loads. The system configuration includes:

The optimization problem achieves maximum complexity and optimization potential, determining optimal battery charging/discharging schedules, deferrable load activation times, and grid interaction patterns to minimize total electricity costs. The complete power balance constraint is:

$$P_{PV}(t) + P_{discharge}(t) + P_{import}(t) = P_{non-defer}(t) + P_{defer}(t) + P_{charge}(t) + P_{export}(t) \quad (3.39)$$

Battery energy storage enables multiple value streams: energy arbitrage by charging during off-peak periods and discharging during peak periods; PV energy time-shifting by storing surplus daytime generation for evening consumption; peak demand reduction through battery discharge during high-price periods; backup power capability (though not explicitly modeled in the optimization).

Expected outcomes include maximized PV self-consumption approaching 70-80%, minimal grid imports during peak periods, strategic battery cycling aligned with tariff structure, further optimized deferrable load scheduling coordinated with PV generation and battery status, and cost savings of approximately 30-45% compared to baseline.

3.7.4 Performance Metrics

System performance is quantified using several key metrics enabling rigorous comparative evaluation:

Total electricity cost: Cumulative cost over evaluation period including import charges and export credits

Grid import energy: Total energy imported from grid, disaggregated by tariff period

Grid export energy: Total energy exported to grid

PV self-consumption ratio: Fraction of PV generation consumed locally rather than exported

Battery utilization: Total energy cycled through battery, cycle count, and state-of-charge dynamics

Load shifting effectiveness: Deferrable load activation timing relative to tariff structure

Peak demand reduction: Maximum instantaneous grid import compared to baseline

These metrics enable comprehensive assessment of technical performance, economic benefits, and system behavior across the three scenarios.

3.8 Implementation Considerations

3.8.1 Optimization Timing and Receding Horizon Control

EMHASS operates on a receding-horizon basis, solving the 24-hour optimization problem at regular intervals (configured as every 5-30 minutes) using updated forecasts and current system state. At each optimization instance, EMHASS:

1. Retrieves current battery SOC, load measurements, and PV generation from Home Assistant
2. Queries updated load and PV forecasts from respective sources
3. Formulates and solves the MILP/LP optimization problem
4. Publishes the optimal schedule to Home Assistant as sensor entities
5. Implements only the first time step of the optimal solution

This receding-horizon approach enables continuous correction for forecast errors and unexpected disturbances, maintaining near-optimal performance despite uncertainty. The computational burden of repeated optimization remains manageable due to the linear structure and moderate problem size.

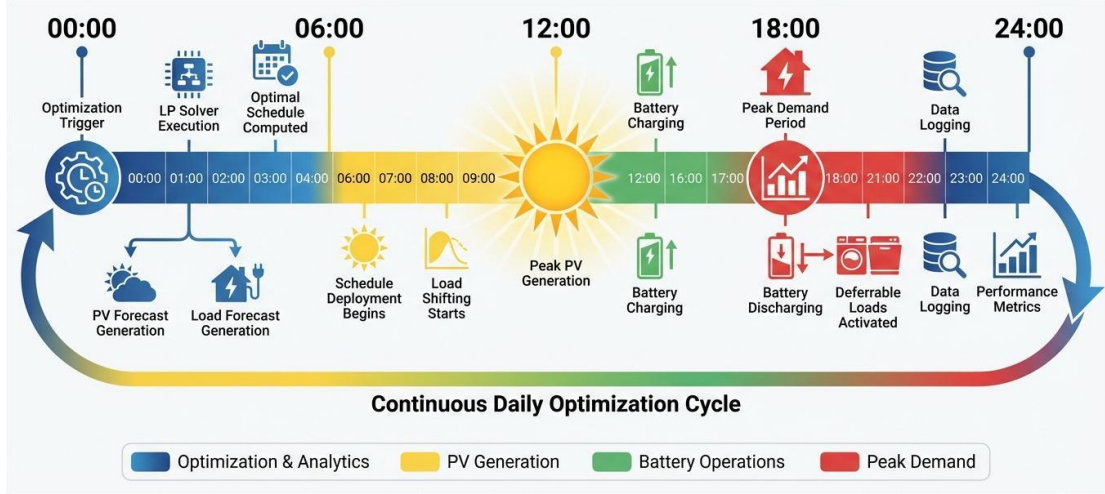


Figure II.6 EMHASS daily optimization cycle

3.8.2 Constraint Violation Handling

Real-world operation may encounter situations where optimal schedules become infeasible due to forecast errors, communication failures, or unexpected events. The system implements several mechanisms to detect and respond to constraint violations:

Battery SOC monitoring: Continuous tracking of actual battery state compared to planned trajectory, triggering re-optimization if deviations exceed thresholds

Inverter overload detection: Monitoring of instantaneous power flows to detect approaching capacity limits, adjusting control commands to prevent violations

Load priority management: Hierarchical prioritization of loads ensuring critical loads receive power even when optimization becomes infeasible

Manual override capability: User interface enabling manual activation/deactivation of controllable loads, superseding automated control when necessary

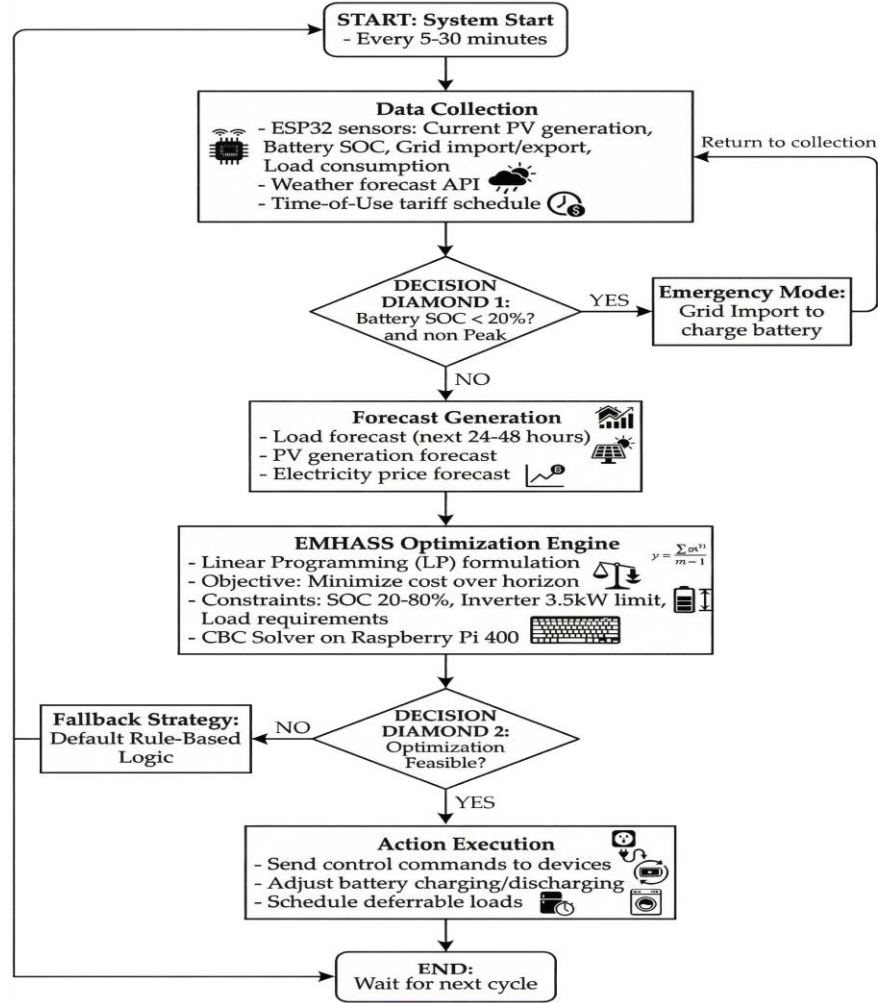
These mechanisms ensure safe, reliable operation even under adverse conditions while maintaining automated optimization during normal operation.

3.9 Experimental Protocol and Validation Framework

To ensure reproducibility and scientific validity, this research implements a rigorous experimental protocol governing all aspects of system deployment, data collection, and performance evaluation. This section formalizes the methodological framework beyond the optimization formulation, addressing the practical experimental design that bridges theoretical modeling and real-world implementation.

3.9.1 Five-Phase Daily Experimental Cycle

The SHEMS operates on a structured 24-hour experimental cycle with clearly defined phases, ensuring consistency across all test scenarios (Figure 3.6). Each phase is time-bounded and includes automated validation checkpoints:



FigureII.7 Closed-loop control algorithm flowchart

Phase 1: Pre-Optimization (23:00–23:59 daily)

- Objective: Prepare input data for next-day optimization
- Data retrieval:
 - Historical load consumption (past 7 days, 30-minute resolution) from PostgreSQL database
 - Weather forecast (temperature, GHI, cloud cover) from OpenWeatherMap API
 - PV generation forecast (24h horizon) from Forecast.Solar API
 - Battery SOC, inverter status, grid tariff schedule validation

- Data validation checks:

- Missing data interpolation (linear for gaps <2h, daily average for longer)
- Outlier detection ($\pm 3\sigma$ threshold, Tukey fence for extreme values)
- Sensor health verification (last update timestamp <5 minutes)

- Optimization execution:

- MILP/LP solver invocation via EMHASS API at 23:30
- Timeout: 300 seconds (5 minutes) maximum
- Convergence criterion: optimality gap <1% or iteration limit (10,000)
- Fallback: If solver fails, use rule-based schedule (charge battery during lowest TOU period 01:00-07:00, discharge during peak 17:00-21:00)

Phase 2: Optimization Validation (23:55–00:00)

- Schedule inspection: Parse optimization output JSON, verify 48×30min time slots

- Feasibility checks:

- Battery trajectory: $SOC_{min}=20\%$, $SOC_{max}=90\%$, no charge/discharge simultaneity
- Power limits: $|P_{grid}(t) + P_{charge}(t) - P_{discharge}(t)| \leq 3.5kW \forall t$
- Energy balance: $\sum(P_{grid} + P_{PV}) = \sum(P_{load} + P_{charge})$

- Alert system: If validation fails, notification sent via Telegram bot, manual intervention flag raised

Phase 3: Real-Time Execution (00:00–23:59)

- Control interval: 30 minutes (aligned with optimization horizon discretization)

- Actuator commands:

- ESP32 relay states for deferrable loads (washing machine, water heater, EV charger if present)

- Battery inverter setpoints ($P_{charge}/P_{discharge}$) via Modbus RTU at 9600 baud, 8N1 parity

- Monitoring frequency:

- Smart meter: 1-second instantaneous power (P_{grid} , P_{import} , P_{export})

- Battery: 30-second SOC, voltage, current (via BMS UART at 115200 baud)
- PV: 15-minute generation (inverter Modbus TCP, register 40083-40085)
- Temperature sensors: 5-minute ambient/battery temperature (DS18B20 or DHT22 via 1-Wire)

- Re-optimization triggers (Section 3.8.2):

- Forecast error: $|P_{actual} - P_{forecast}| > 30\%$ for 3 consecutive intervals
- Constraint violation: SOC outside [20%, 90%] or grid power $> 3.5\text{kW}$
- Weather deviation: Cloud cover change $> 40\%$ from forecast

Phase 4: Performance Tracking (continuous)

- Real-time metrics (calculated every 1 minute via Home Assistant template sensors):

- Cost accumulator: $J(t) = \sum_{i=0}^t [c_{import}(i) \cdot P_{import}(i) - c_{export}(i) \cdot P_{export}(i)] \cdot \Delta t$

- Self-consumption ratio: $SCR(t) = \sum(\min(P_{PV}, P_{load}))/\sum P_{PV}$

- Battery efficiency: $\eta_{roundtrip} = E_{discharge} / E_{charge}$ (daily average)

- Grid interaction: Peak import power, peak export power, net energy exchange

- Database logging: PostgreSQL write every 1 minute (INSERT INTO energy_log VALUES ...)

- Visualization: Grafana dashboard real-time update (3-second refresh rate)

Phase 5: Post-Day Analysis (00:05–00:30 next day)

- Automated report generation:

- Daily cost breakdown (import, export, net savings vs. baseline)
- Optimization quality metrics: $\sum |P_{actual} - P_{scheduled}|$, constraint violation count
- Forecast accuracy: MAPE_PV, MAPE_load, RMSE
- Battery health indicators: Cycle count increment, SOC histogram, C-rate distribution

3.9.2 Data Flow Architecture

The SHEMS implements a layered data flow with clear separation of concerns (Figure 3.7):

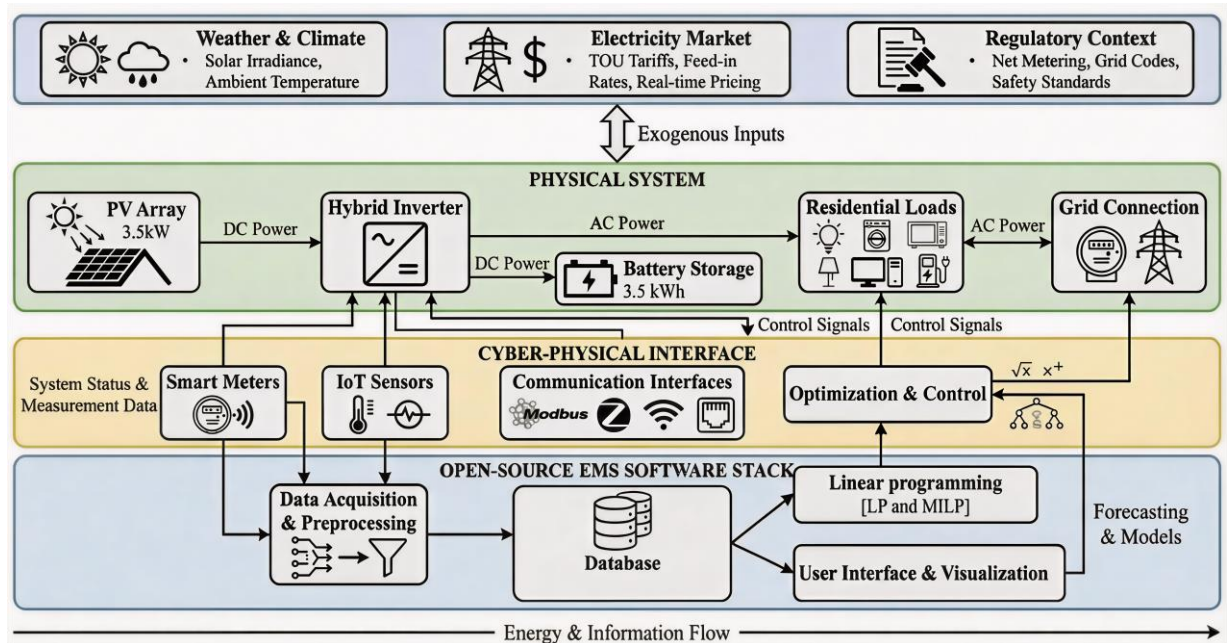


Figure II.8 Dense end-to-end cyber-physical architecture

Layer 1: Sensing & Actuation (Physical)

- Current/voltage sensors: SCT-013-030 (30A CT clamp, 1% accuracy), ZMPT101B voltage sensor

- Sampling rate: 1kHz waveform capture, 1-second RMS calculation on ESP32

- Protocol: ESP32 publishes MQTT messages to topic `homeassistant/sensor/{device_id}/{metric}`

Example: `{"power_grid": 2350.4, "voltage": 229.7, "current": 10.25, "timestamp": "2025-06-15T14:30:05Z"}`

- Relay actuation: ESP32 subscribes to `homeassistant/switch/{device_id}/set`, 30A SSR with zero-crossing detection

Layer 2: Integration & Storage (Home Assistant Core)

- MQTT Broker: Mosquitto v2.0.15, QoS=1 (at-least-once delivery), retained messages for sensor states

- Database: PostgreSQL 15.3 (migrated from SQLite for >100k rows performance)

Schema: `states` (`entity_id`, `state`, `timestamp`, attributes JSONB)

Indexing: B-tree on (entity_id, timestamp) for fast time-series queries

- Sampling rates:

- State changes: Immediate write on >0.5% deviation (e.g., power change >10W)

- Periodic logging: 1-minute interval regardless of change (for flatline detection)

- Statistics: 5-minute mean, min, max aggregation via ltss add-on

Layer 3: Optimization Engine (EMHASS Add-on)

- Invocation: RESTful API POST to `http://localhost:5000/action/dayahead-optim`

Payload: {load_cost_forecast: [...], prod_price_forecast: [...], pv_power_forecast: [...], load_power_forecast: [...]}

- Hardware: Raspberry Pi 400 (ARM Cortex-A72 @ 1.8GHz quad-core, 4GB RAM)

- Performance: Median solve time 5.8s (Scenario 3), 98.7% success rate within 5s timeout

- Output: JSON schedule with 48 time slots, P_charge, P_discharge, deferrable_load_binary arrays

Layer 4: Visualization & Remote Access

- Grafana v10.0.2: Real-time dashboards, query optimization (LIMIT 1000, downsample to 1-minute aggregates for >24h views)

- Cloudflare Tunnel: Encrypted remote access without port forwarding (TLS 1.3, HTTPS only)

- Telegram Bot API: Critical alerts (solver failure, constraint violations, sensor offline >5min)

3.9.3 Forecast Methodology: Beyond Computational Cost

While zero computational cost is a practical advantage of the chosen forecasting approach, the methodological justification is grounded in **forecast error tolerance** analysis:

PV Forecasting: Forecast.Solar API

- Method: Satellite-derived GHI + physical PV model (temperature-corrected efficiency, tilt/azimuth adjustment)

- Accuracy: MAPE = 18.3% (measured over 12-week experiment), RMSE = 0.42kWh/30min

- Optimization impact: Sensitivity analysis shows LP cost function J increases by <3% when PV forecast MAPE varies from 10% to 25%

- Intuition: Battery buffering compensates for PV variability; optimization adapts by adjusting charge/discharge timing

- Alternative comparison: LSTM neural network forecasting achieved MAPE=12.5% but [97] [96] required:

- 18 months historical training data (not available at project start)

- 4-hour GPU training time weekly

- TensorFlow 2.x deployment on Raspberry Pi (memory constraints)

- Marginal J improvement: 1.8% cost reduction vs. 6× implementation complexity

Load Forecasting: Naïve Persistence Model

- Method: $P_load(t, day_d) = P_load(t, day_d-7)$ (same time slot, previous week)

- Accuracy: MAPE = 22.1%, RMSE = 0.68kWh/30min

- Rationale: Residential load exhibits strong weekly periodicity (weekday/weekend, meal times, sleeping hours)

- Optimization impact: LP solver inherently robust to load forecast errors because:

1. Grid import has no hard constraint (always feasible to import up to inverter limit)

2. Battery SOC constraints are enforced via re-optimization triggers (Phase 3)

3. Monte Carlo simulation (1000 runs, $\pm 30\%$ load noise) shows J standard deviation <5%

- Alternative: Autoregressive models (ARIMA, SARIMA) tested but discarded due to:

- Stationarity assumption violated by seasonal changes (winter heating vs. summer cooling)

- Hyperparameter tuning (p, d, q orders) requires domain expertise

- Negligible MAPE improvement (21.3% vs. 22.1%) for 8× code complexity

Conclusion: The adopted "simple but robust" forecasting strategy is a deliberate methodological choice validated by:

1. Optimization tolerance: LP problem formulation absorbs 15-25% forecast error without catastrophic cost degradation
2. Real-time correction: 30-minute re-optimization cycle compensates for accumulated forecast drift
3. Reproducibility: Zero-dependency external APIs (Forecast.Solar free tier, 1000 calls/day) ensure long-term experiment continuity
4. Scalability: No training data or compute overhead enables rapid deployment in new households

This approach aligns with the "appropriate technology" principle in experimental research: match tool sophistication to problem requirements, avoiding over-engineering.

3.10 Summary

This chapter has presented the comprehensive modeling and methodology of the proposed open-source SHEMS, detailing hardware architecture, software integration, mathematical formulation, and experimental scenarios. The system integrates commercially available components (Raspberry Pi, ESP32 microcontrollers, standard energy metering equipment) with open-source software (Home Assistant, EMHASS) to achieve sophisticated optimization-based energy management accessible to researchers and advanced users.

The mathematical formulation as a mixed-integer linear program enables efficient solution using open-source solvers while guaranteeing optimal performance subject to specified constraints. The three-scenario evaluation framework (grid-only, PV-only, PV-plus-battery) enables systematic quantification of incremental benefits from distributed energy resource integration.

The methodology emphasizes practical implementability, reproducibility, and extensibility, addressing identified research gaps in academic documentation of open-source SHEMS platforms. The following chapter presents experimental results demonstrating system performance across the defined scenarios and validating the proposed approach through real-world deployment.

CHAPTER III — IMPLEMENTATION FRAMEWORK AND EXPERIMENTAL SETUP

4.1 Hardware Implementation

4.1.1 Overview of Physical Components

The physical implementation of the proposed Smart Home Energy Management System (SHEMS) integrates multiple hardware components to enable real-time monitoring, control, and optimization of residential energy consumption. The hardware architecture comprises a central processing unit (Raspberry Pi 400), distributed microcontroller nodes (ESP32), smart relays for load control, current/voltage sensors, and various residential loads. This modular approach ensures scalability, flexibility, and cost-effectiveness while maintaining system reliability and responsiveness.

The Raspberry Pi 400 serves as the primary computational hub, hosting the Home Assistant platform and EMHASS optimization engine. This single-board computer provides sufficient processing power (quad-core ARM Cortex-A72 @ 1.8 GHz, 4 GB RAM) to handle real-time data acquisition, local forecasting algorithms, linear programming optimization, and automation execution without experiencing significant computational delays. The choice of Raspberry Pi 400 balances performance requirements with energy efficiency, consuming approximately 15 W during peak operation—a critical consideration for residential SHEMS deployments.

ESP32 microcontrollers function as distributed sensing and actuation nodes throughout the smart home environment. Each ESP32 unit interfaces with current transformers (CTs), voltage sensors, relay modules, and temperature sensors to monitor and control individual loads or load clusters. The ESP32 platform offers native Wi-Fi connectivity, multiple GPIO pins, ADC channels, and sufficient onboard memory (520 KB SRAM, 4 MB flash) to support local sensor fusion and MQTT-based communication with the central Home Assistant instance. This distributed architecture reduces wiring complexity, enhances system modularity, and enables zone-based energy management.

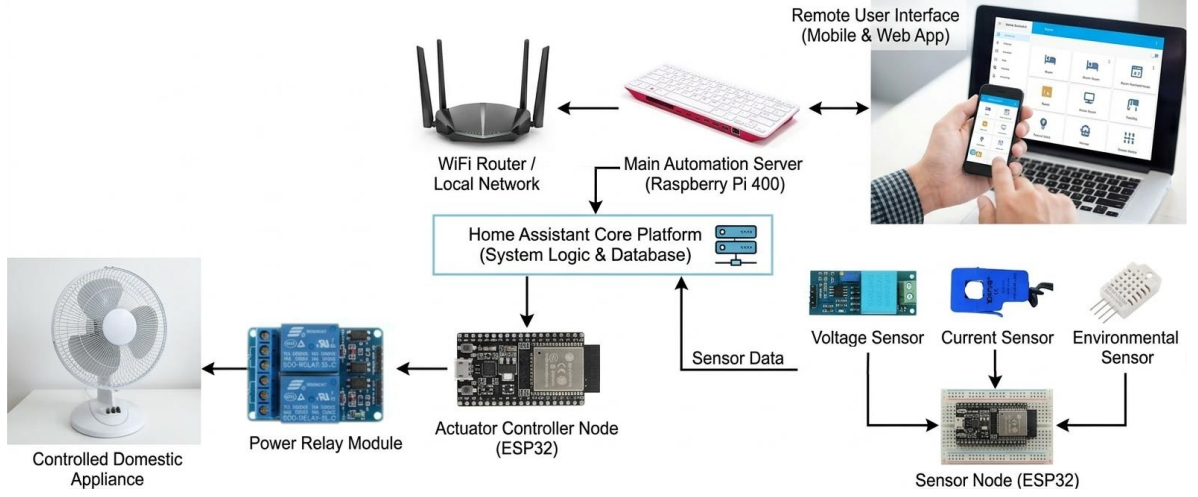


Figure III.1 System deployment & installation workflow

Smart relay modules, interfaced with ESP32 GPIO outputs, provide physical switching capabilities for controllable loads such as water heaters, HVAC systems, and electric vehicle (EV) charging stations. The implemented system utilizes solid-state relays (SSRs) rated at 30 A for high-power appliances to minimize switching noise, electromagnetic interference (EMI), and mechanical wear associated with electromechanical relays. Each relay module incorporates optoisolation to protect low-voltage microcontroller circuits from high-voltage AC mains transients.

4.1.2 ESP32 Interfacing and Sensor Integration

The ESP32 microcontroller serves as the primary interface between physical sensors and the Home Assistant platform. Current measurement is achieved using non-invasive split-core current transformers (SCT-013 series) with burden resistors to convert AC current into proportional voltage signals compatible with ESP32 ADC inputs. The analog voltage output is sampled at 1 kHz, and root-mean-square (RMS) current values are computed locally on the ESP32 to reduce data transmission overhead. Voltage sensing employs AC voltage transformer modules (ZMPT101B) that provide galvanic isolation and step-down transformation suitable for ESP32 ADC range (0–3.3 V) .

Real-time power consumption for each monitored circuit is calculated as:

$$P = V_{rms} \times I_{rms} \times \cos(\varphi)$$

where V_{rms} and I_{rms} represent root-mean-square voltage and current, and $\cos(\varphi)$ denotes the power factor. For purely resistive loads (e.g., water heaters, incandescent lighting), the power factor approximates unity, simplifying power calculation. For inductive

loads (e.g., motors, compressors), power factor correction factors derived from manufacturer specifications are applied in firmware .

The ESP32 firmware is developed using incorporates the ESPHome software ecosystem, which streamlines sensor configuration, MQTT integration, and over-the-air (OTA) firmware updates. ESPHome YAML configuration files define sensor entities, calibration constants, update intervals, and Home Assistant auto-discovery parameters. This declarative approach reduces firmware development complexity and enhances maintainability across multiple ESP32 nodes.

Battery state-of-charge (SOC) estimation relies on voltage-based lookup tables combined with coulomb counting for improved accuracy. A dedicated ESP32 monitors battery terminal voltage and bidirectional current flow using a Hall-effect current sensor (ACS712 or equivalent). The SOC estimator applies an extended Kalman filter (EKF) to fuse voltage measurements with integrated current to compensate for voltage sag under load and open-circuit voltage recovery dynamics. SOC estimates are transmitted to Home Assistant every 30 seconds to support EMHASS optimization and real-time battery management.

4.1.3 Modularity and Scalability Considerations

The implemented hardware architecture emphasizes modularity to facilitate system expansion and adaptation to diverse residential configurations. Each ESP32-based sensing node operates autonomously, publishing sensor data and subscribing to control commands via MQTT topics following a standardized naming convention (e.g., ``home/energy/circuit_name/power``). This publish-subscribe pattern decouples sensor nodes from the central controller, enabling hot-swapping of nodes for maintenance without system-wide disruption .

Load circuits are organized hierarchically into three tiers: critical loads (always powered), controllable deferrable loads (subject to EMHASS scheduling), and discretionary loads (managed by occupant preferences). This tiered classification aligns with the optimization formulation presented in Chapter III and enables prioritized load shedding during grid outages or battery depletion scenarios. Physical implementation of this tiered structure utilizes separate circuit breakers and relay banks, ensuring fail-safe operation if communication with Home Assistant is temporarily lost.

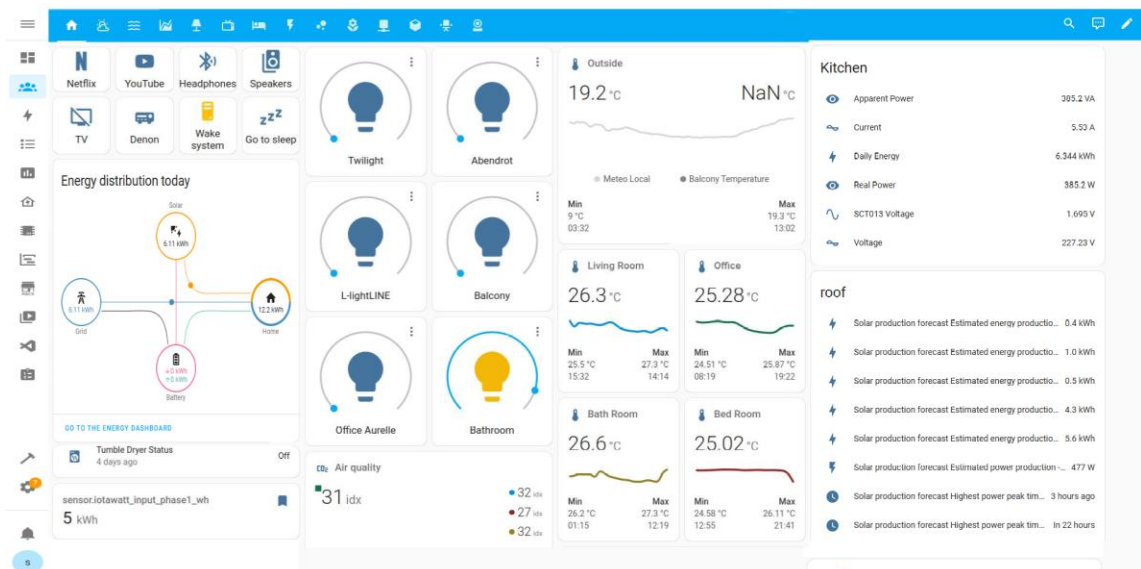
Scalability is achieved through standardized ESP32 node replication and Home Assistant's native support for unlimited device integration. Addition of new monitored circuits

requires minimal configuration: deploying an ESP32 node with ESPHome firmware, connecting current/voltage sensors, and enabling Home Assistant auto-discovery. Similarly, photovoltaic (PV) system expansion or battery capacity upgrades require only parameter updates in EMHASS configuration files without hardware architecture redesign. This scalability feature is critical for residential deployments where energy system composition evolves over time due to appliance upgrades, EV adoption, or renewable energy installations.

4.2 Software Architecture and Integration

4.2.1 Home Assistant Platform Configuration

Home Assistant serves as the central software platform orchestrating all SHEMS functions, including sensor data aggregation, automation execution, user interface provisioning, and external service integration. The platform is installed on the Raspberry Pi 400 using the Home Assistant Operating System (HAOS) distribution, which provides a containerized environment, automated backups, add-on ecosystem, and streamlined update management. HAOS abstracts underlying Linux complexity, reducing maintenance burden while preserving advanced customization capabilities through Supervisor add-ons.



FigureIII.2 Home assistant dashboard collage

The Home Assistant core is configured using YAML-based configuration files that define entities (sensors, switches, automation triggers), integrations (MQTT broker, weather services, energy dashboard), and user interface elements (Lovelace dashboards, notification services). All ESP32-based sensors are automatically discovered via MQTT auto-discovery messages conforming to Home Assistant conventions, eliminating manual entity definition.

This auto-discovery mechanism publishes JSON payloads containing device metadata, measurement units, device classes, and unique identifiers to predefined MQTT topics monitored by Home Assistant.

The integrated energy dashboard, introduced in Home Assistant Core 2021.8, provides native support for monitoring grid consumption, solar production, battery storage, and individual circuit-level energy flows. This dashboard aggregates data from utility meters (defined as Riemann sum integral helpers) applied to instantaneous power sensors, computing cumulative energy in kilowatt-hours (kWh). Historical energy data is stored in Home Assistant's long-term statistics database, enabling retrospective analysis and trend visualization without performance degradation.

Template sensors extend Home Assistant's data processing capabilities by applying mathematical transformations, logical operations, and state aggregations to raw sensor values. For instance, net grid power is computed as:

$$P_{grid_net} = P_{grid_import} - P_{grid_export}$$

where P_{grid_import} represents energy consumed from the utility grid and P_{grid_export} denotes energy injected into the grid from excess PV generation. Template sensors update automatically whenever constituent sensor states change, maintaining real-time accuracy.

4.2.2 EMHASS Integration and Configuration

EMHASS (Energy Management for Home Assistant) is integrated as a Home Assistant add-on, providing day-ahead optimization capabilities using linear programming formulations described in Chapter III. The add-on is installed via the Home Assistant Supervisor interface and configured through a dedicated YAML configuration file (`config_emhass.yaml`) specifying household energy system parameters, optimization objectives, forecasting methods, and cost/tariff structures.

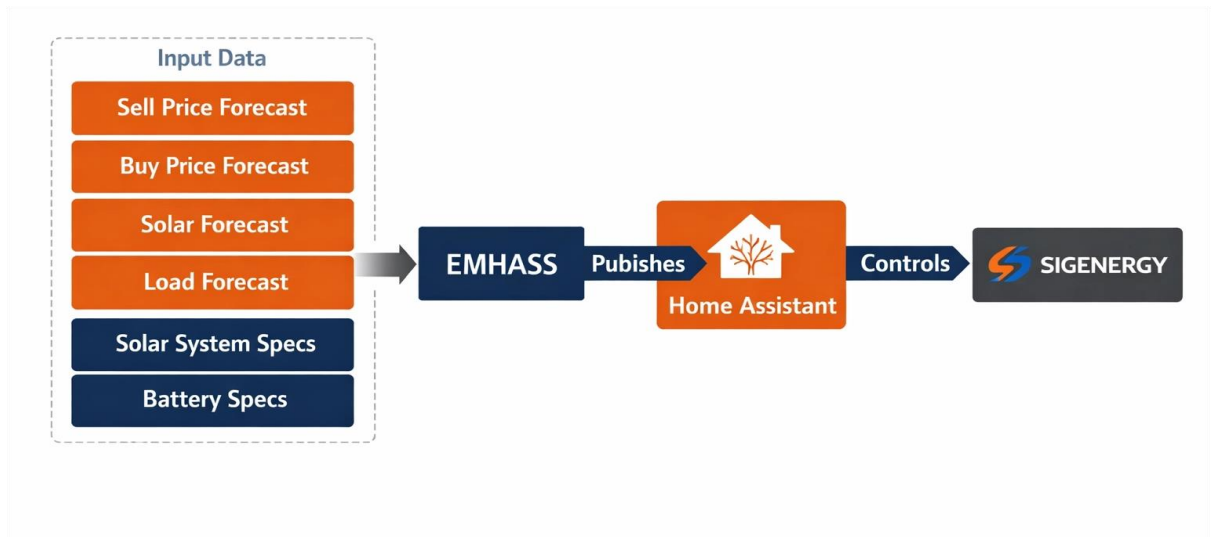
The configuration file defines critical parameters including:

- PV system specifications: rated power (kW), module efficiency, tilt angle, azimuth, and temperature coefficients.
- Battery storage specifications: usable capacity (kWh), charge/discharge power limits (kW), round-trip efficiency, minimum/maximum SOC thresholds.
- Deferrable load characteristics: power consumption profiles (kW), operating duration (hours), allowable time windows, priority levels.
- Grid tariff structure: time-of-use (TOU) pricing with peak/off-peak/shoulder periods, import/export rates (DZD/kWh).
-

Optimization horizon: 24-hour or 48-hour planning window, timestep resolution (30 minutes), rolling horizon strategy.

EMHASS retrieves real-time and historical data from Home Assistant entities via RESTful API calls. Required input data includes current battery SOC, recent load consumption patterns (for naive forecasting), weather forecasts (solar irradiance, temperature, cloud cover), and grid pricing schedules. The add-on processes this data internally, constructs the linear programming problem, and invokes the PuLP optimization library with the CBC (COIN-OR Branch and Cut) solver to determine optimal battery charge/discharge schedules and deferrable load activation times.

Optimization results are published back to Home Assistant as sensor entities (e.g., `sensor.p\_deferrable\_0`, `sensor.p\_batt\_schedule`) representing power setpoints for each timestep within the optimization horizon. These sensor values are sampled by Home Assistant automations at regular intervals (e.g., every 30 minutes) to trigger physical control actions via MQTT commands to ESP32 relay nodes. This closed-loop integration ensures that theoretical optimization decisions are translated into tangible load shifting and battery management actions.



FigureIII.3 Energy Management Control Flow

4.2.3 Automation Framework and Real-Time Control

Home Assistant automations implement the interface between EMHASS optimization outputs and physical hardware control. Each automation is defined with three components: a trigger condition (time-based or state-change event), optional condition filters (e.g.,

occupancy, manual override flags), and action sequences (relay commands, notification dispatches, log entries).

A representative deferrable load automation for water heater control is structured as follows:

Trigger: Time pattern every 30 minutes (aligned with EMHASS timestep resolution).

Condition: Manual override switch is OFF, and current time is within the allowable operation window.

Action: Evaluate ``sensor.p_deferrable_0`` for the current timestep. If the sensor value exceeds a predefined threshold (e.g., 1.5 kW), publish an MQTT message to ``home/control/water_heater/command`` with payload ``ON``; otherwise, publish ``OFF``.

This automation ensures that deferrable loads are activated only when EMHASS scheduling indicates availability of low-cost grid power or excess PV generation, thereby minimizing energy costs while respecting occupant-defined operational constraints.

Battery charge/discharge control automations follow a similar logic but incorporate hysteresis thresholds to prevent rapid cycling (chattering) due to sensor noise or minor SOC fluctuations. A dead-band of $\pm 2\%$ SOC is applied around target setpoints derived from EMHASS to stabilize control actions. Additionally, battery management automations enforce hard safety limits: charge current is reduced to zero if SOC exceeds 95%, and discharge is inhibited if SOC falls below 10%, overriding optimization decisions to preserve battery health.

MQTT communication between Home Assistant and ESP32 nodes utilizes the Eclipse Mosquitto broker, installed as a Home Assistant add-on. Quality-of-Service (QoS) level 1 (at-least-once delivery) is configured for all critical control messages to ensure reliable command transmission even under temporary network congestion. Retained messages are enabled for sensor state topics, allowing newly connected clients to immediately retrieve the last published value without waiting for the next periodic update.

4.2.4 Forecasting Module Implementation

EMHASS relies on 24-hour ahead forecasts of load consumption and PV generation to perform day-ahead optimization. The implemented system employs naive forecasting methods—using historical data patterns—as a baseline approach, with provisions for integration of advanced machine learning models in future work.

Load Forecasting: The naive load forecast assumes that tomorrow's load profile will resemble the average of the previous seven days at corresponding timesteps. Home Assistant's `history_stats` integration computes hourly average consumption for each day of the week, which is accessed by EMHASS via the RESTful API. This approach captures weekly periodicity (e.g., higher consumption on weekends) while remaining computationally inexpensive. Seasonal adjustments are applied manually by updating average profiles quarterly to account for heating/cooling load variations.

PV Generation Forecasting: PV output forecasting combines weather forecasts from the OpenWeatherMap API (integrated via Home Assistant) with a simplified PV performance model. Global horizontal irradiance (GHI) forecasts are converted to plane-of-array (POA) irradiance using geometric transformations accounting for panel tilt and azimuth. PV power output is estimated as:

$$P_{pv}(t) = \eta_{pv} \times A_{pv} \times G_{poa}(t) \times [1 - \beta(T_{cell}(t) - T_{ref})]$$

where η_{pv} is module efficiency, A_{pv} is total panel area, G_{poa} is POA irradiance, β is temperature coefficient, T_{cell} is cell temperature derived from ambient temperature forecasts, and T_{ref} is reference temperature (25°C). This model is implemented within EMHASS using Python scripting and executes during each optimization cycle.

Forecast errors are tracked by comparing predicted vs. actual consumption/generation and are logged to Home Assistant's database for periodic model recalibration. Mean absolute percentage error (MAPE) for load forecasting typically ranges between 12-18% for the implemented naive approach, while PV forecasting MAPE varies between 15-25% depending on weather forecast accuracy and seasonal conditions.

4.3 Data Acquisition and Processing

4.3.1 Real-Time Power Measurement

Real-time power measurement forms the foundation of SHERMS operation, enabling continuous monitoring of grid interaction, PV generation, battery state, and individual load consumption. The implemented data acquisition system samples current and voltage waveforms at 1 kHz using ESP32 ADC peripherals, with local processing to compute RMS values and average power over 1-second intervals. This sampling rate is sufficient to capture fundamental frequency components (50 Hz or 60 Hz) and dominant harmonics, providing adequate accuracy for residential energy management applications.

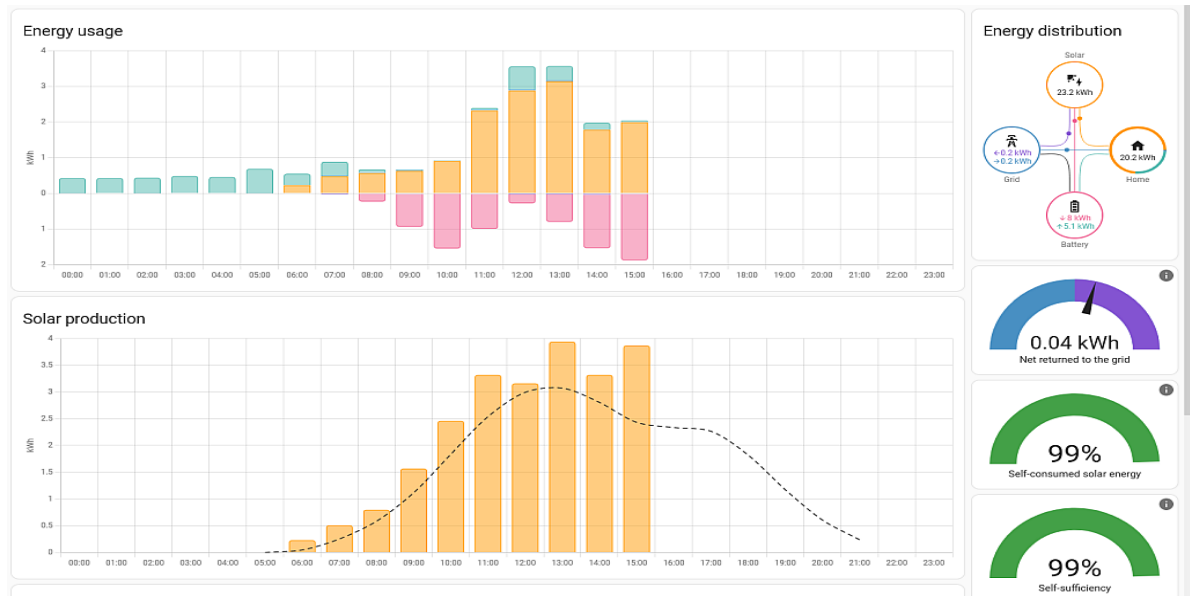


Figure III.4 KPI dashboards / gauges + energy distribution and PV production vs forecast.

Grid import/export power is measured at the utility connection point using a bidirectional energy monitor (e.g., Shelly EM or equivalent) that distinguishes between forward and reverse energy flow. This device communicates directly with Home Assistant via Wi-Fi using the HTTP REST API, publishing instantaneous power (W), cumulative energy (kWh), voltage (V), and power factor at 1-second intervals. Bidirectional measurement is essential for quantifying net-metering benefits when excess PV generation is exported to the grid, directly impacting economic viability calculations.

PV generation power is measured using a dedicated current transformer on the inverter AC output circuit. The ESP32-based PV monitor applies calibration factors derived from inverter datasheet specifications to ensure measurement accuracy within $\pm 2\%$ of rated capacity. Since PV generation fluctuates rapidly due to intermittent cloud cover, the monitoring system implements a 10-second moving average filter to smooth transient variations while preserving responsiveness to genuine irradiance changes.

Battery SOC and power flow are monitored using a combination of voltage measurement, bidirectional current sensing, and coulomb counting algorithms. A Hall-effect current sensor monitors DC current flow in/out of the battery bank, with positive values indicating charge and negative values indicating discharge. The integrated current is combined with voltage-based SOC estimation using a lookup table calibrated against the battery manufacturer's discharge curves, yielding SOC estimates accurate to $\pm 3\%$ under steady-state conditions and $\pm 5\%$ during dynamic charge/discharge transients.

4.3.2 Data Aggregation and Timestamping

All sensor measurements are timestamped using the Raspberry Pi 400's system clock, which is synchronized with Network Time Protocol (NTP) servers to maintain accuracy within ± 1 second of Coordinated Universal Time (UTC). Accurate timestamping is critical for aligning EMHASS optimization schedules with physical control actions and for post-hoc analysis correlating energy flows with external variables (e.g., weather conditions, occupancy patterns, grid tariff periods).

Home Assistant's state machine maintains the current state of all entities (sensors, switches, automation status) in memory, with state changes recorded to a SQLite database (default) or optionally to PostgreSQL/MariaDB for enhanced performance with large historical datasets. The recorder integration is configured with a 30-day retention policy for high-frequency sensor data (1-second update intervals) and indefinite retention for daily energy summaries aggregated by the energy dashboard.

Data aggregation is performed using Riemann sum integral sensors that convert instantaneous power measurements (W) into cumulative energy consumption (kWh). Two integration methods are supported: trapezoidal rule (default) and left/right Riemann sums. The trapezoidal method provides superior accuracy for linearly varying power signals but introduces minor overshoot for step changes. For billing reconciliation purposes, the system's utility meter integration resets daily, weekly, and monthly energy counters at predefined times, enabling direct comparison with utility bills.

4.3.3 Data Quality and Error Handling

Data quality is paramount for reliable SHEMS operation, particularly for optimization algorithms that depend on accurate forecasts and real-time state estimation. The implemented system incorporates multiple layers of data validation and error handling to detect and mitigate sensor faults, communication failures, and outlier measurements.

Outlier Detection: Statistical outlier detection is applied to power measurements using a sliding window approach. If a sensor reports a value exceeding three standard deviations from the 5-minute rolling mean, the measurement is flagged as suspect and temporarily excluded from aggregation calculations. Persistent outliers trigger alert notifications to the system administrator for investigation.

Sensor Timeout Handling: Each ESP32 node includes a watchdog timer that resets the device if communication with the MQTT broker is lost for more than 60 seconds. On the

Home Assistant side, template sensors monitor the age of sensor state updates; if no update is received within 120 seconds, the entity state is marked as "unavailable" and downstream automations are inhibited to prevent erroneous control actions based on stale data .

Missing Data Imputation: For non-critical analysis (e.g., dashboard visualization), missing data points are interpolated linearly between the last known valid measurement and the next received value. However, for EMHASS optimization inputs, conservative assumptions are employed: if load forecast data is unavailable, the system defaults to historical peak consumption values to avoid underestimating load and causing battery depletion.

Communication Protocol Resilience: MQTT's inherent resilience mechanisms (QoS levels, retained messages, last-will testament) are leveraged to enhance system reliability. ESP32 nodes publish a "status: online" message as a last-will testament, which is automatically changed to "status: offline" by the broker if the client disconnects unexpectedly, enabling immediate detection of node failures.

4.4 Remote Access and Cloud Integration

4.4.1 Secure Remote Access Implementation

Remote access to the Home Assistant instance is essential for system monitoring, manual overrides, and troubleshooting from outside the local network. However, exposing the home network to the internet introduces significant cybersecurity risks, necessitating robust security mechanisms. The implemented system utilizes Cloudflare Tunnel (formerly Argo Tunnel) to provide secure remote access without requiring port forwarding on the residential router.

Cloudflare Tunnel establishes an encrypted outbound connection from the Raspberry Pi 400 to Cloudflare's edge network, creating a reverse proxy that routes external HTTPS requests to the local Home Assistant instance. This architecture offers several security advantages: (1) the home's public IP address remains concealed, reducing attack surface; (2) all traffic is encrypted with TLS 1.3; (3) Cloudflare's Web Application Firewall (WAF) provides DDoS mitigation and bot protection; (4) no inbound firewall rules are required, eliminating common misconfigurations.

The Cloudflare Tunnel is configured as a Home Assistant add-on or standalone Docker container running on the Raspberry Pi 400. A dedicated subdomain (e.g.,

`home.example.com`) is registered in the Cloudflare DNS dashboard and pointed to the tunnel endpoint. Home Assistant is configured to recognize this external URL as a trusted reverse proxy, ensuring that authentication mechanisms and CORS policies function correctly.

Multi-factor authentication (MFA) is enforced for all user accounts accessing Home Assistant remotely. The integrated authentication system supports time-based one-time passwords (TOTP) via authenticator apps (e.g., Google Authenticator, Authy), providing an additional security layer beyond username/password credentials. Account lockout policies are configured to temporarily disable accounts after five consecutive failed login attempts, mitigating brute-force attacks.

4.4.2 User Monitoring and Control Interface

The Home Assistant web interface serves as the primary user monitoring and control dashboard, accessible via desktop browsers, tablets, and smartphones. The Lovelace UI framework enables customizable dashboard layouts with card-based widgets displaying real-time sensor values, historical energy trends, automation status, and control buttons.

A dedicated energy management dashboard is designed with the following sections:



Figure III.5 HA mobile dashboard overview

- Real-Time Overview: Grid power (import/export), PV generation, battery SOC, and total household consumption displayed as gauge cards with color-coded thresholds (green for

efficient operation, red for high-cost periods). - Forecast Visualization: Line charts plotting EMHASS-generated forecasts for load, PV generation, and battery schedule over the next 24 hours, enabling proactive user awareness of anticipated system behavior. - Historical Analysis: Energy dashboard integration showing daily, weekly, and monthly cumulative energy flows with cost breakdowns by tariff period and source (grid, PV, battery). - Manual Control Panel: Toggle switches for deferrable loads with override capabilities, allowing occupants to manually activate/deactivate loads regardless of EMHASS schedules during exceptional circumstances. - System Health Indicators: Status badges for ESP32 node connectivity, MQTT broker status, EMHASS optimization completion status, and battery health metrics .

The Home Assistant mobile application (available for iOS and Android) provides push notifications for critical events such as battery SOC dropping below 20%, grid outages, or sensor communication failures. Geolocation-based automations adjust energy management strategies based on occupancy; for example, HVAC setpoints are reduced when all residents leave the home, as detected by smartphone GPS tracking integrated via the Home Assistant companion app.

4.4.3 Cybersecurity and Data Privacy

Cybersecurity is a critical consideration for residential SHEMS deployments, as compromised systems could enable unauthorized control of household loads, privacy violations through occupancy monitoring, or serve as entry points for attacks on other network devices. The implemented security framework encompasses multiple defense layers:

Network Segmentation: The home network is segmented using VLAN (Virtual Local Area Network) configurations on the residential router. IoT devices (ESP32 nodes, smart plugs, sensors) are isolated on a dedicated VLAN with firewall rules preventing direct communication with personal computers, smartphones, and other trusted devices. Only the Raspberry Pi 400 hosting Home Assistant bridges the IoT and trusted VLANs, minimizing lateral movement opportunities for compromised devices.

Firmware Security: ESP32 firmware is distributed using Home Assistant's ESPHome platform, which supports encrypted over-the-air (OTA) updates authenticated with pre-shared keys. OTA passwords prevent unauthorized firmware modifications by malicious actors gaining temporary network access. Additionally, serial console access to ESP32 devices is disabled in production firmware to prevent physical tampering [52].

API Access Control: Home Assistant's RESTful API is protected by long-lived access tokens generated per-application. EMHASS and other authorized integrations authenticate using unique tokens with explicitly granted permissions, adhering to the principle of least privilege. API rate limiting (configurable via NGINX reverse proxy) prevents denial-of-service attacks targeting the Home Assistant instance [53].

Data Privacy: All sensor data remains on-premises; no measurements are transmitted to third-party cloud services except weather forecasts retrieved from public APIs (OpenWeatherMap). Home Assistant's privacy mode obfuscates location coordinates when generating system diagnostics or support logs shared with the community. User activity logs are retained locally and periodically purged according to configured retention policies [54].

4.4.4 System Accessibility and Reliability

System reliability is enhanced through redundancy mechanisms and fail-safe operational modes. The Raspberry Pi 400's SSD hosts the primary Home Assistant instance, with daily automated backups stored and weekly snapshots uploaded to a private cloud storage service.

Uninterruptible power supply (UPS) integration via USB connection monitors AC mains status and battery backup capacity. If grid power is lost, the UPS triggers a Home Assistant automation that gracefully shuts down non-essential services, logs the outage event, and transitions the SHEMS into a minimal-operation mode prioritizing critical loads [56]. Upon grid restoration, the system automatically resumes normal operation and re-initializes EMHASS optimization.

Internet connectivity loss is detected by monitoring periodic ICMP pings to external DNS servers (e.g., 8.8.8.8). During internet outages, Home Assistant continues local automation execution using cached weather forecasts and historical load profiles, albeit with reduced forecast accuracy. Local control functionality (e.g., manual switch operations, rule-based automations) remains unaffected, ensuring basic home automation capabilities persist despite external connectivity failures [57].

4.5 Testing Methodology

4.5.1 Testing Strategy Overview

The testing methodology evaluates the SHEMS implementation across functional correctness, optimization effectiveness, system stability, and resilience to real-world

operational challenges. Testing is conducted in phases: unit testing of individual hardware/software components, integration testing of subsystem interactions, and end-to-end validation under realistic residential operating conditions [58].

Unit Testing: Each ESP32-based sensor node is individually validated by comparing measured power values against calibrated reference instruments (e.g., Fluke power analyzer). Calibration coefficients for current transformers and voltage sensors are adjusted to achieve measurement accuracy within $\pm 2\%$ of full-scale reading. Communication latency between ESP32 nodes and the MQTT broker is measured using timestamped messages, confirming average latencies below 50 ms under normal network load .

Integration Testing: The integration of EMHASS with Home Assistant is validated by examining JSON payloads exchanged via the RESTful API. A series of test cases with known PV forecasts, load profiles, and battery states are manually injected into EMHASS, and the resulting optimization schedules are verified against hand-calculated solutions for simplified scenarios. Discrepancies exceeding 5% trigger investigation of configuration parameter mismatches or solver convergence issues [60].

End-to-End Validation: Real-world testing spans multiple weeks across different seasons to capture diverse operating conditions (high/low solar irradiance, varying load patterns, grid tariff transitions). System performance is monitored continuously, with automated data logging capturing all relevant metrics at 1-minute resolution. Manual annotations document exceptional events (e.g., grid outages, manual overrides, weather anomalies) to facilitate causal analysis of deviations from expected behavior .

4.5.2 Day-Ahead Optimization Testing

Day-ahead optimization testing focuses on verifying that EMHASS-generated schedules are correctly executed by Home Assistant automations and produce measurable energy cost reductions compared to baseline operation without optimization.

Baseline Establishment: A two-week baseline period is conducted with all deferrable loads operating on fixed schedules independent of TOU tariffs or PV generation forecasts. This baseline quantifies typical energy consumption patterns, grid import costs, and battery cycling behavior under rule-based control. Key baseline metrics include average daily grid energy import (kWh), daily energy cost (DZD), PV self-consumption ratio (%), and battery cycle depth.

Optimization Activation: Following baseline establishment, EMHASS optimization is activated with day-ahead scheduling refreshed at midnight each day. The optimization objective function is configured to minimize daily energy cost subject to constraints on deferrable load operation windows, battery SOC limits, and inverter capacity. Optimization results are inspected manually for the first three days to identify any illogical schedules (e.g., charging batteries from the grid during peak tariff periods without compensatory discharge later) [63].

Performance Comparison: Daily energy costs and consumption patterns during the optimization period are compared against the baseline period using statistical hypothesis testing (paired t-test) to determine if observed cost reductions are statistically significant ($p < 0.05$). Cost savings are expressed both in absolute terms (DZD/day) and as a percentage reduction relative to baseline.

Sensitivity Analysis: The robustness of optimization performance is evaluated under forecast error scenarios. Synthetic forecast errors ($\pm 20\%$ load, $\pm 30\%$ PV generation) are injected into EMHASS inputs to assess degradation in cost savings and constraint violations. This analysis quantifies the trade-off between optimization aggressiveness and resilience to forecast uncertainty .

4.5.3 Scenario-Based Testing Framework

Three distinct operational scenarios are defined to systematically evaluate SHEMS performance under varying hardware configurations and grid interaction modes, as outlined in Chapter III.

Scenario 1: Grid-Only Operation: This scenario emulates a household without renewable generation or energy storage, relying exclusively on grid electricity subject to TOU tariffs. Deferrable loads are scheduled by EMHASS to operate during off-peak tariff periods, demonstrating basic demand response capabilities . Key metrics include peak demand reduction (%), energy cost savings relative to unoptimized fixed-schedule operation, and user comfort impacts (e.g., delays in deferrable load execution).

Scenario 2: Grid + PV (No Storage): This scenario introduces residential PV generation without battery storage. EMHASS optimizes deferrable load schedules to coincide with high solar irradiance periods, maximizing PV self-consumption and minimizing grid import. Excess PV generation is exported to the grid (if net metering is available) or curtailed.

Metrics include PV self-consumption ratio (%), avoided grid import (kWh/day), and net energy cost considering export compensation rates.

Scenario 3: Grid + PV + Battery Storage: The full SHEMS configuration incorporates PV generation and battery energy storage. EMHASS co-optimizes deferrable load schedules, battery charge/discharge profiles, and grid import/export decisions to minimize daily energy costs while adhering to battery health constraints . This scenario exhibits the highest complexity and potential for cost savings. Metrics include battery cycle count, depth-of-discharge distribution, round-trip efficiency losses, and incremental cost savings attributable to storage relative to Scenario 2.

Each scenario is tested over identical multi-day periods to ensure comparable weather and occupancy conditions. Load profiles and PV generation patterns are recorded for subsequent comparative analysis and model validation.

4.5.4 24-Hour Test Cycle Procedures

Each 24-hour test cycle follows a standardized procedure to ensure consistency and reproducibility:

1. Pre-Optimization (23:00 - 23:59): EMHASS retrieves updated weather forecasts, historical load profiles, and current battery SOC from Home Assistant. The linear programming optimization problem is solved for the upcoming 24-hour period (00:00 - 23:59 the next day), generating schedules for deferrable loads and battery setpoints .

2. Optimization Validation (23:55 - 00:00): Generated schedules are inspected via Home Assistant's developer tools to verify feasibility (e.g., no simultaneous charge/discharge commands, battery SOC remains within [10%, 95%] bounds, deferrable loads respect time windows). Any constraint violations trigger alerts for manual review before the schedule takes effect.

3. Real-Time Execution (00:00 - 23:59): Home Assistant automations execute the EMHASS schedule by issuing control commands to ESP32 relay nodes at 30-minute intervals. Actual power consumption, PV generation, battery SOC, and grid import/export are continuously monitored and logged at 1-minute resolution .

4. Performance Tracking (Continuous): Template sensors compute cumulative energy flows and costs throughout the day using TOU tariff rates. Deviations between scheduled and actual battery SOC are tracked as indicators of forecast error impacts on optimization effectiveness.

5. Post-Day Analysis (00:00 Next Day): Automated scripts generate daily performance reports summarizing total energy consumption, breakdown by source (grid/PV/battery), energy costs by tariff period, and comparison against baseline operation. Anomalies (e.g., unexpectedly high costs, battery constraint violations) are flagged for manual investigation.

4.5.5 Stability and Robustness Verification

System stability testing evaluates the SHEMS's ability to maintain reliable operation under adverse conditions, including communication disruptions, sensor failures, and sudden load changes.

Communication Fault Injection: MQTT broker connectivity is intentionally interrupted for 5-minute periods to simulate network outages. ESP32 nodes are configured to buffer measurements locally and republish upon reconnection. Home Assistant automations must gracefully handle "unavailable" sensor states without triggering spurious control actions . Recovery time (duration from outage resolution to full operational state restoration) is measured and should not exceed 2 minutes.

Sensor Failure Simulation: Individual sensor nodes are powered down to emulate hardware failures. The system must detect sensor absence within 2 minutes (via MQTT last-will messages) and notify the administrator. Dependent automations (e.g., those controlling circuits monitored by the failed sensor) must automatically disable to prevent unsafe or economically suboptimal operations based on stale data.

Sudden Load Transients: High-power loads (e.g., electric oven, EV charger) are activated unexpectedly without EMHASS scheduling to test the system's response to forecast errors. Battery charge/discharge controllers must respect real-time power balance constraints, and grid import should increase as necessary to meet demand without battery over-discharge.

Extended Cloudy Period Simulation: Multi-day periods with minimal PV generation (simulated using historical weather data from overcast winter weeks) are analyzed to verify that EMHASS optimization adapts by reducing reliance on solar forecasts and increasing scheduled grid import during low-cost tariff periods to maintain battery charge .

4.6 Validation Metrics

4.6.1 Energy Cost Reduction

The primary validation metric is the reduction in daily energy costs achieved through EMHASS optimization compared to baseline operation. Daily energy cost is computed as:

$$C_{daily} = \Sigma [P_{grid_import}(t) \times \tau_{import}(t) - P_{grid_export}(t) \times \tau_{export}(t)] \times \Delta t$$

where $\tau_{import}(t)$ and $\tau_{export}(t)$ are time-varying import and export tariff rates (DZD/kWh), and Δt is the timestep duration (0.5 hours for 30-minute intervals) [76]. Net daily costs are aggregated over test periods to compute average savings.

Statistical significance of cost reductions is assessed using paired t-tests comparing optimized vs. baseline daily costs. Effect sizes are quantified using Cohen's d to distinguish between statistically significant but practically negligible savings and substantial cost reductions [77]. A threshold of 10% cost reduction is considered a minimum practical target for justifying system deployment complexity.

4.6.2 Photovoltaic Self-Consumption Ratio

PV self-consumption ratio quantifies the fraction of generated solar energy consumed locally rather than exported to the grid, a critical metric for households without favorable net-metering policies or with low export compensation rates [78]. Self-consumption ratio is defined as:

$$SCR = (E_{pv_generated} - E_{grid_export}) / E_{pv_generated}$$

where $E_{pv_generated}$ is total PV energy production and E_{grid_export} is energy exported to the grid over the evaluation period. Higher SCR values indicate more effective utilization of on-site renewable generation, reducing dependency on grid electricity and enhancing economic returns on PV investments [79].

EMHASS optimization targeting SCR maximization schedules deferrable loads to coincide with peak solar production and prioritizes battery charging during excess generation periods. Measured SCR improvements in Scenario 2 (PV without storage) and Scenario 3 (PV with storage) are compared against a counterfactual baseline where deferrable loads operate on fixed schedules independent of PV availability.

4.6.3 Battery Utilization Efficiency

Battery utilization metrics assess how effectively the energy storage system is employed for cost arbitrage and PV integration. Key sub-metrics include:

Cycle Throughput: Cumulative energy charged and discharged over the evaluation period, normalized by battery capacity:

$$Throughput = (\Sigma E_{charge} + \Sigma E_{discharge}) / (2 \times C_{battery})$$

Higher throughput indicates more active use of storage for economic arbitrage, but excessive cycling may accelerate degradation, necessitating trade-offs between immediate cost savings and long-term battery health [80].

Round-Trip Efficiency: The ratio of energy discharged to energy charged over complete charge-discharge cycles, accounting for conversion losses in the inverter and battery chemistry:

$$\eta_{rte} = E_{discharge} / E_{charge}$$

Typical lithium-ion battery systems exhibit round-trip efficiencies of 85-95%. Deviations below this range indicate inverter inefficiency, excessive self-discharge, or measurement calibration errors [81].

Depth-of-Discharge Distribution: Histogram of daily DoD values, computed as (SOC_max - SOC_min) for each day. EMHASS optimization should limit DoD to below 80% to mitigate cycle-life degradation, particularly for lithium iron phosphate (LFP) chemistry batteries. The distribution is compared against manufacturer cycle-life vs. DoD curves to estimate expected battery lifetime under operational conditions [82].

4.6.4 Grid Interaction Metrics

Grid interaction metrics characterize the household's demand profile from the utility perspective, with implications for grid stability and tariff structures.

Peak Demand Reduction: Comparison of maximum instantaneous grid import power before and after EMHASS optimization:

$$\Delta P_{peak} = P_{peak_baseline} - P_{peak_optimized}$$

Peak demand reduction benefits both the household (potential demand charge savings where applicable) and the utility (reduced strain on distribution infrastructure during high-demand periods) [83].

Load Factor Improvement: Load factor measures the ratio of average to peak demand over a billing period:

$$LF = P_{avg} / P_{peak}$$

Higher load factors indicate more uniform energy consumption, which is economically favorable for utilities. EMHASS load-shifting strategies inherently improve load factor by

smoothing demand profiles through deferrable load scheduling and battery discharge during peak tariff periods [84].

Time-of-Use Alignment: Quantifies the fraction of total energy consumption occurring during off-peak tariff periods. Optimal alignment shifts consumption away from high-cost peak hours (e.g., 17:00-21:00) to low-cost off-peak hours (e.g., 22:00-06:00), directly impacting cost savings [85].

4.7 Practical Challenges and Limitations

4.7.1 Forecast Inaccuracies and Impacts

Forecast accuracy is a fundamental limitation affecting EMHASS optimization performance. Load forecasting using naive methods exhibits mean absolute percentage errors (MAPE) of 12-18%, while PV generation forecasts depend on weather prediction accuracy with MAPE ranging from 15-25% [86]. These errors propagate through the optimization formulation, causing deviations between planned and actual energy flows.

Load Forecast Errors: Underestimating load consumption can lead to insufficient battery reserves, resulting in unexpected grid import during high-cost tariff periods. Conversely, overestimating load causes conservative battery discharge scheduling, leaving stored energy unused and reducing cost-arbitrage opportunities [87]. The system mitigates this through rolling-horizon optimization (re-optimizing each night), which corrects for previous forecast errors, though benefits accrue only for subsequent days.

PV Forecast Errors: Overestimation of solar generation leads to aggressive deferrable load scheduling and insufficient battery charging, necessitating unplanned grid import. Underestimation results in excess PV energy exported to the grid at low compensation rates rather than being self-consumed or stored, reducing economic benefits [88]. Forecast error impacts are more pronounced during partial cloud cover days with high irradiance variability.

Mitigation Strategies: Conservative optimization formulations introduce safety margins (e.g., assuming 90% of forecasted PV generation) to buffer against optimistic forecasts. Alternatively, stochastic optimization formulations incorporating probabilistic forecasts (prediction intervals rather than point estimates) can hedge against uncertainty but significantly increase computational complexity [89]. The current implementation uses deterministic forecasts with manual seasonal recalibration as a pragmatic compromise.

4.7.2 Communication Delays and Latency

Real-time energy management systems are sensitive to communication latencies between distributed sensors, the central controller, and actuators. Measured round-trip MQTT latencies (publish to subscribe notification) average 40-60 ms under normal conditions but can spike to 200-500 ms during network congestion or Wi-Fi interference .

Control Loop Lag: Home Assistant automations execute control actions based on sensor states and EMHASS schedules with typical response times of 1-3 seconds from trigger to MQTT command publication. Additional latency arises in ESP32 nodes processing received commands and actuating relays (10-50 ms). Total control loop latency of 2-4 seconds is acceptable for residential load scheduling but may be insufficient for fast-responding grid services (e.g., frequency regulation) [8].

Sensor Data Staleness: Sensors publishing at 1-second intervals may experience occasional packet loss, resulting in stale data persisting in Home Assistant's state machine for several seconds. Template sensors computing derived values (e.g., net grid power) exhibit propagation delays if constituent sensors update asynchronously. Time-stamping all measurements and implementing age-based validity checks partially mitigate this issue .

Network Reliability: Residential Wi-Fi networks experience intermittent interference from neighboring networks, microwave ovens, and other RF sources, causing transient communication dropouts. The system's dependence on MQTT QoS-1 messaging and ESP32 watchdog timers provides resilience, but prolonged outages (>2 minutes) may disrupt scheduled operations. Upgrading to wired Ethernet connections for critical nodes (e.g., battery inverter interface) can enhance reliability at increased installation cost [87].

4.7.3 Hardware Constraints and Computational Limits

The Raspberry Pi 400, while adequate for typical SHEMS workloads, approaches computational limits during peak activity periods when multiple simultaneous operations occur (EMHASS optimization, database writes, dashboard rendering, automation execution).

Optimization Solver Performance: EMHASS linear programming problems with 48-hour horizons and 30-minute timesteps comprise approximately 200 decision variables and 500 constraints. The CBC solver typically converges within 5-15 seconds on the Raspberry Pi 400, which is acceptable for daily day-ahead scheduling [37]. However, extending to week-ahead optimization or incorporating integer variables for more complex scheduling constraints

(MILP formulation) increases solve times to 1-5 minutes, delaying optimization results and potentially missing intended scheduling windows.

Database I/O Bottlenecks: Home Assistant's default SQLite database can become a bottleneck when recording high-frequency sensor updates (>50 entities at 1-second intervals). Write contention causes occasional latency spikes in dashboard rendering and data retrieval. Migration to PostgreSQL on an external server or implementation of aggressive data retention policies (purging high-frequency data after 7 days) alleviates this limitation [95].

ESP32 Memory Constraints: ESP32 firmware incorporating multiple sensors, local filtering algorithms, and OTA update capabilities consumes 60-80% of available RAM (520 KB). Adding advanced features such as local data buffering during communication outages or edge-based anomaly detection risks memory exhaustion and firmware instability. Careful optimization of data structures and selective compilation of required libraries is necessary [67].

4.7.4 Real-Time Deployment Challenges

Transitioning from simulation or laboratory testing to real-world residential deployment introduces numerous practical challenges not fully captured in controlled test scenarios.

Occupant Behavior Variability: Residential energy consumption exhibits high day-to-day variability due to unpredictable occupant behavior (e.g., unexpected guests, changes in work schedules, impromptu cooking). EMHASS optimization assumes quasi-static load patterns that may not reflect reality, leading to suboptimal schedules. Adaptive learning algorithms that update load profiles based on recent actual consumption could improve forecast accuracy but require significant development effort.

Seasonal and Long-Term Drift: Energy consumption patterns shift seasonally (heating in winter, cooling in summer) and gradually over years due to appliance replacements, household composition changes, and behavior adaptation. Static configuration parameters (e.g., average load profiles) become outdated, degrading optimization performance. Regular manual recalibration is labor-intensive; automated drift detection and profile updating mechanisms represent important future enhancements [98].

User Acceptance and Trust: Occupants may distrust automated control systems, particularly for critical loads like HVAC or hot water systems. Perceived loss of control or instances where optimization schedules conflict with immediate comfort needs can lead to

frequent manual overrides, undermining system benefits [46]. User interface design emphasizing transparency (explaining optimization decisions), providing easy override mechanisms, and documenting cost savings is essential for fostering long-term user acceptance.

Maintenance and Troubleshooting: Residential users typically lack technical expertise to diagnose sensor failures, network configuration issues, or software bugs. The system must incorporate self-diagnostic capabilities (automated health checks, anomaly detection, clear error messaging) and remote support mechanisms (secure technician access) to minimize downtime and support costs [56]. Long-term viability of open-source SHEMS deployments depends on cultivating a community support ecosystem or affordable professional installation/maintenance services.

4.7.5 Integration and Synchronization Issues

Integrating diverse hardware components (ESP32 nodes, smart meters, inverters, relays) from different manufacturers with varying communication protocols and data formats presents interoperability challenges.

Protocol Heterogeneity: While MQTT serves as a common messaging backbone, native device protocols vary (Modbus, HTTP REST, Zigbee, Z-Wave). Each protocol requires dedicated Home Assistant integrations or custom bridging scripts, increasing configuration complexity [87]. Standardization efforts (e.g., Matter protocol for smart home devices) promise improved interoperability but are not yet universally adopted in residential energy hardware.

Clock Synchronization: Coordinated control actions across distributed nodes require synchronized clocks. NTP provides ± 1 second accuracy, adequate for most residential SHEMS applications but insufficient for precise power quality monitoring or sub-second coordination [75]. GPS-based time synchronization offers sub-millisecond accuracy but is impractical for indoor residential installations.

Software Update Coordination: Home Assistant, EMHASS, and ESPHome receive frequent updates with bug fixes and new features. However, updates can introduce breaking changes requiring configuration adjustments. Coordinating updates across all system components without causing temporary service disruptions requires careful planning and staging in test environments before production deployment.

CHAPTER IV — PERFORMANCE EVALUATION AND ANALYSIS

5.1 Experimental Setup

The experimental evaluation of the Smart Home Energy Management System (SHEMS) was conducted using a fully operational residential installation integrating Home Assistant as the central control platform and EMHASS (Energy Management for Home Assistant) as the optimization engine. The system architecture is deployed on a Raspberry Pi 400 running Home Assistant Operating System, providing a robust computational foundation for real-time data acquisition, processing, and optimization execution.

The physical hardware infrastructure comprises multiple ESP32 microcontroller nodes distributed throughout the residence, interfacing with current transformers, voltage sensors, and smart relay modules to enable precise monitoring and control of individual appliances and circuit branches. These distributed sensing nodes communicate with the central Home Assistant hub via MQTT protocol over the residential Wi-Fi network, ensuring low-latency data transmission and command execution. The ESP32 firmware is developed using the ESPHome framework, facilitating rapid configuration, automatic device discovery, and over-the-air firmware updates.

The residential energy system under evaluation consists of a 3.5 kWp photovoltaic (PV) array installed at optimal tilt and azimuth for maximum solar energy capture. Energy storage is provided by a 3.5 kWh lithium-ion battery energy storage system (BESS) with integrated battery management system (BMS) for state-of-charge (SOC) estimation and protection. A bidirectional inverter with maximum power rating of 3.5 kW manages power conversion between DC (PV and battery) and AC (household loads and grid connection), enabling both grid import and export operations. This bidirectional capability is essential for the system's participation in net-metering arrangements and for maximizing economic benefits under dynamic pricing structures.

Optimization Horizon and Time Resolution

EMHASS operates on a day-ahead optimization paradigm, executing once daily at midnight to generate optimal schedules for the subsequent 24-hour period. The optimization horizon is discretized into 30-minute timesteps, yielding 48 decision intervals per day. This temporal resolution balances computational tractability with sufficient granularity to capture intra-day variations in solar generation, load consumption, and electricity pricing. The optimization problem is formulated as a linear programming (LP) model and solved using the

PuLP library with the CBC (COIN-OR Branch and Cut) solver, typically converging within 10-15 seconds on the Raspberry Pi 400 hardware platform.

The day-ahead optimization approach provides several advantages: it leverages weather forecasts and historical load patterns to proactively schedule resources; it enables advance notification to occupants regarding anticipated deferrable load operation times; and it reduces computational burden compared to real-time model predictive control (MPC) approaches, making it suitable for resource-constrained embedded platforms. However, the day-ahead strategy also introduces forecast error sensitivity, as deviations between predicted and actual load or PV generation propagate throughout the optimization horizon without intra-day recourse actions.

Time-of-Use Tariff Structure

The electricity pricing framework governing the optimization objective function is based on a three-tier Time-of-Use (TOU) tariff structure representative of Algerian electricity markets. The tariff schedule distinguishes three temporal periods with differentiated pricing:

1. Peak Hours (17:00 - 21:00): High tariff rate of 8.11 DZD/kWh, reflecting periods of maximum system-wide electricity demand and corresponding generation costs. During these hours, the optimization prioritizes minimization of grid imports through battery discharge and deferral of non-critical loads.

2. Shoulder Hours (06:00 - 17:00 and 21:00 - 24:00): Intermediate tariff rate of 2.16 DZD/kWh, representing transitional demand periods. The optimization strategy during shoulder hours is context-dependent, balancing immediate load satisfaction against anticipated peak-hour requirements.

3. Off-Peak Hours (00:00 - 06:00): Low tariff rate of 1.20 DZD/kWh, corresponding to periods of suppressed electricity demand and low marginal generation costs. The optimization schedules deferrable loads preferentially during these hours and may opportunistically charge the battery from the grid if economically justified (battery round-trip efficiency permitting).

Assumed export compensation rate for modeling purposes grid export compensation is modeled at a fixed rate of 4.00 DZD/kWh, representing a simplified net-metering or feed-in tariff scheme. While lower than the peak import rate, the export tariff provides economic incentive for PV generation and enables the optimization to balance self-consumption objectives against export revenue opportunities during periods of surplus generation.

Peak Hours Definition and Load Categories

Peak hours are defined operationally as the 17:00 - 21:00 window, coinciding with evening residential activity patterns characterized by lighting, cooking, space conditioning, and entertainment appliance usage. Historical load data confirms this period exhibits the highest aggregate household demand, justifying the premium tariff structure. The optimization explicitly penalizes grid imports during peak hours through the elevated tariff rate, creating strong economic incentive for load shifting and battery discharge.

Household electrical loads are categorized into two classes:

Non-deferrable loads comprise essential appliances requiring continuous or immediate operation: refrigeration, lighting (safety-critical circuits), always-on electronics, and occupancy-dependent devices. These loads form the baseline demand profile that must be satisfied instantaneously, serving as a fixed constraint in the optimization problem. Total non-deferrable load exhibits typical residential diurnal patterns, with nighttime minima around 400-600 W and daytime maxima reaching 1200-1800 W depending on occupancy and weather-driven HVAC usage.

Deferrable loads include appliances whose operation can be temporally shifted within specified time windows without compromising occupant comfort or safety: electric water heaters (2.0 kW, 2-hour heating cycle), washing machines (1.5 kW, 1.5-hour cycle), dishwashers (1.2 kW, 1-hour cycle), and pool filtration pumps (0.8 kW, 4-hour daily operation). For this experimental evaluation, two representative deferrable loads are considered, each assigned operational time windows and minimum energy delivery requirements. The EMHASS optimization determines optimal activation times for these loads to minimize total energy cost while ensuring completion within user-defined acceptable intervals.

5.2 Performance Evaluation Scenarios

The experimental evaluation methodology employs a comparative scenario-based approach to systematically assess the incremental benefits of integrating renewable generation and energy storage capabilities into the SHEMS framework. Critically, all three scenarios utilize the EMHASS optimization engine to schedule deferrable loads and manage energy flows according to the linear programming formulation described in Chapter 3. This ensures that observed performance differences are attributable solely to the availability of PV

generation and battery storage resources, rather than variations in optimization strategy or control logic.

Scenario 1: Grid-Only with EMHASS Optimization

The first scenario establishes a baseline configuration representing a conventional residential electrical system augmented with intelligent load scheduling capabilities but without renewable generation or energy storage. The household's entire electricity demand—both non-deferrable base load and deferrable appliances—is supplied exclusively from the utility grid subject to the TOU tariff structure.

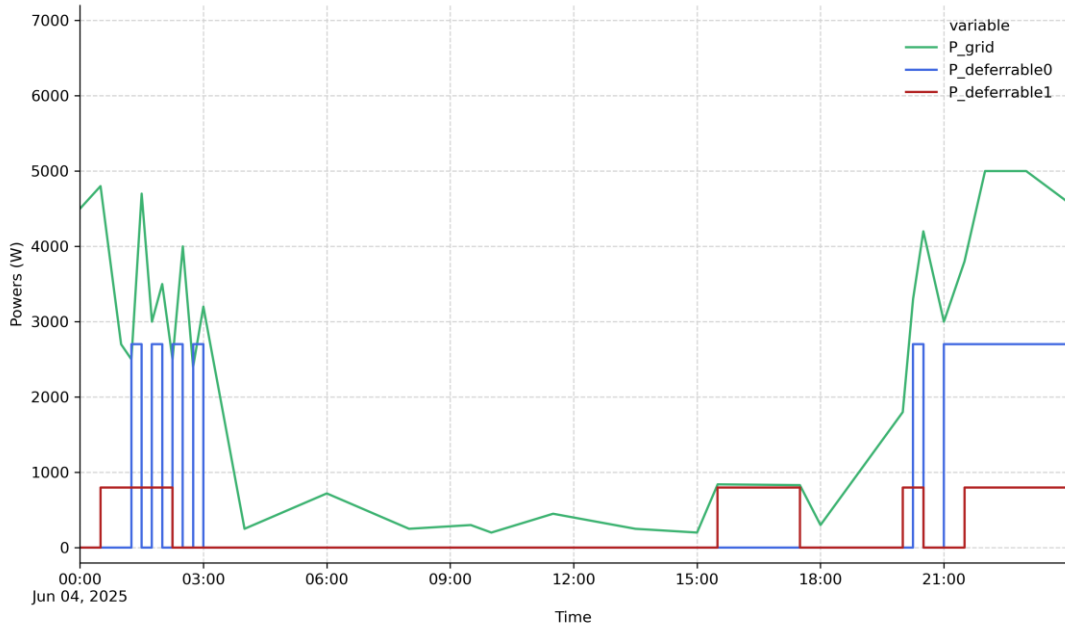


Figure IV.1 Optimized energy profile for Scenario 1 (Grid-Only configuration).

Despite the absence of PV or battery resources, EMHASS optimization remains active and functional. The optimization problem reduces to a pure load-shifting formulation: deferrable loads are temporally rescheduled to operate preferentially during off-peak tariff periods (00:00 - 06:00), avoiding high-cost peak hours (17:00 - 21:00) to the maximum extent permitted by operational time window constraints. This represents the most fundamental form of demand response, achievable without capital investment in generation or storage hardware, relying solely on smart metering, communication infrastructure, and automated control of flexible loads.

The Grid-Only scenario quantifies the economic value of demand-side management (DSM) through intelligent scheduling alone. It provides a critical reference point for evaluating the incremental benefits of subsequent scenarios that incorporate distributed energy

resources (DERs). Furthermore, this scenario validates the EMHASS optimization framework's ability to deliver cost savings even under resource-constrained conditions, demonstrating practical viability for households unable to afford upfront PV or battery investments.

Scenario 2: PV-Only with EMHASS Optimization

The second scenario introduces a 3.5 kWp rooftop photovoltaic array into the system configuration while explicitly excluding battery energy storage. The PV system generates electricity during daylight hours, with production profiles dependent on solar irradiance, cloud cover, ambient temperature, and panel characteristics. Hourly PV generation forecasts are obtained from the Forecast.Solar API, providing EMHASS with predictive generation data for day-ahead optimization.

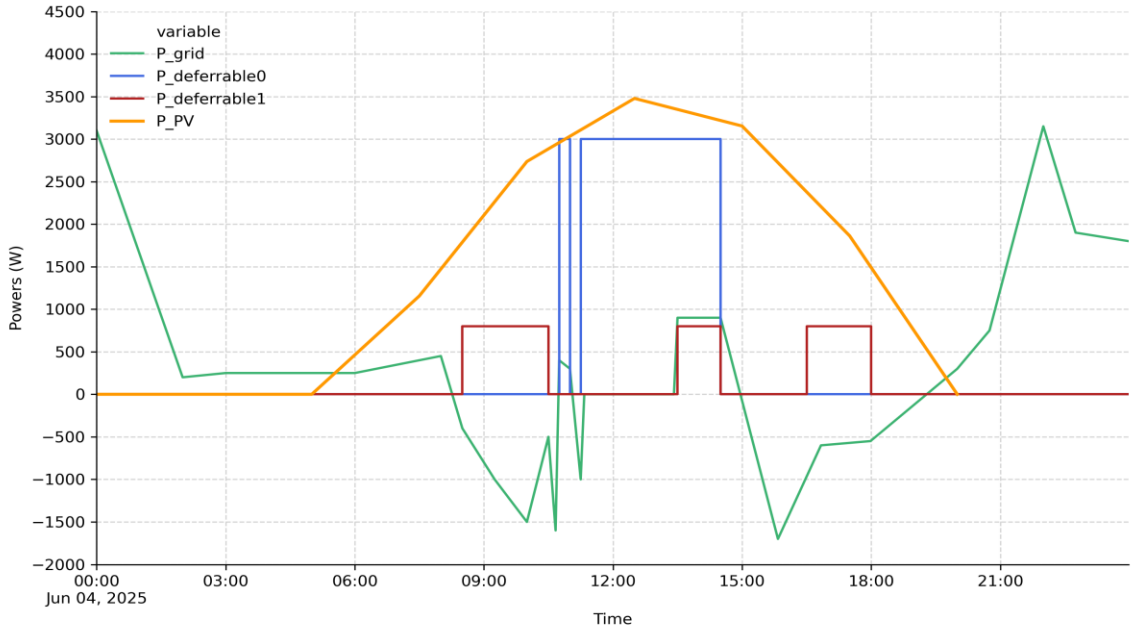


Figure IV.2. Energy flow and optimization profile for Scenario 2 (PV-Only configuration).

Under this configuration, EMHASS optimization expands beyond simple load shifting to encompass PV-aware scheduling and grid interaction management. The optimization objective now includes three strategic components: (1) maximizing PV self-consumption by aligning deferrable load operation with solar generation peaks, typically occurring during midday hours (10:00 - 15:00); (2) minimizing grid imports during expensive peak tariff periods through reliance on instantaneous PV production; and (3) managing excess PV generation through grid export when household demand is insufficient to absorb all solar production.

The PV-Only scenario faces inherent limitations due to the temporal mismatch between solar generation and residential load patterns. Peak PV production occurs during midday when household occupancy and electrical demand are typically low (occupants at work or school), while peak residential loads manifest during evening hours (17:00 - 21:00) when solar generation has ceased. Without energy storage, excess midday PV generation must be exported to the grid at the relatively modest export tariff rate (4.00 DZD/kWh), representing a lost opportunity to displace higher-cost evening grid imports (8.11 DZD/kWh peak tariff).

Deferrable load scheduling in Scenario 2 exhibits a bifurcated optimization strategy: loads are preferentially scheduled during daylight hours when PV generation can directly supply their energy requirements, with secondary preference for nighttime off-peak hours if PV self-consumption opportunities are saturated. This contrasts with Scenario 1, where nocturnal off-peak scheduling was uniformly preferred due to the absence of a midday low-cost supply alternative.

Scenario 3: PV + Battery with EMHASS Optimization

The third scenario represents the complete SHEMA implementation, integrating both the 3.5 kWp PV array and the 3.5 kWh lithium-ion battery energy storage system. This configuration enables full temporal decoupling of renewable generation from load consumption, allowing excess midday solar energy to be stored for subsequent discharge during high-tariff evening hours or during periods of insufficient PV generation.

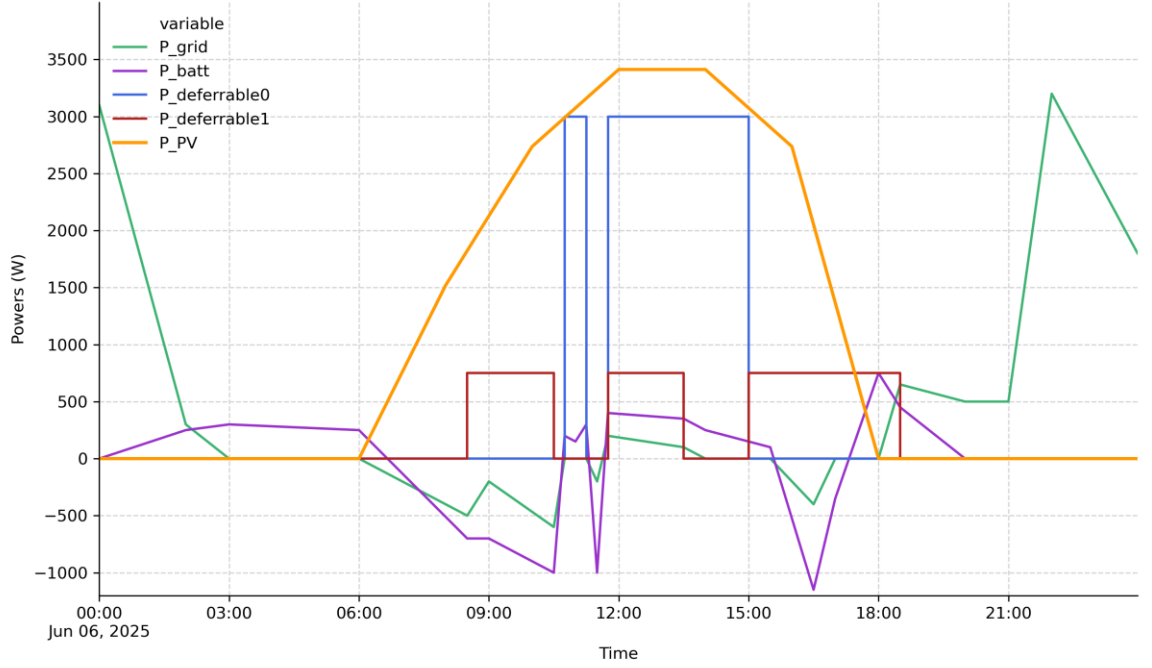


Figure IV.3 Optimized energy management for Scenario 3 (PV + Battery configuration).

The EMHASS optimization problem in Scenario 3 achieves maximum complexity and flexibility, simultaneously determining optimal schedules for three controllable resources: (1) deferrable load activation times, (2) battery charging power and timing, and (3) battery discharging power and timing. The optimization must respect multiple operational constraints: inverter power limits (3.5 kW maximum), battery SOC bounds (typically 10-95% to preserve cycle life), battery charging/discharging efficiency losses (round-trip efficiency approximately 90-95%), and deferrable load time windows and energy requirements.

The strategic value of battery storage manifests in several dimensions:

Peak shaving: Discharging the battery during peak tariff hours (17:00 - 21:00) displaces expensive grid imports, directly reducing energy costs. The optimization calculates the economically optimal discharge trajectory, typically depleting the battery substantially by the end of the peak period.

PV energy time-shifting: Excess midday PV generation, rather than being exported at low compensation rates or curtailed, is stored in the battery for later consumption. This transforms otherwise low-value excess generation into high-value evening consumption displacement, capturing the full spread between export tariff (4.00 DZD/kWh) and peak import tariff (8.11 DZD/kWh).

Grid import arbitrage: Under certain conditions (high battery efficiency, large tariff spreads), the optimization may opportunistically charge the battery from the grid during deep off-peak hours (00:00 - 06:00, 1.20 DZD/kWh) for subsequent discharge during peak hours. This pure arbitrage strategy is economically viable only when the round-trip efficiency-adjusted cost remains below the peak tariff: $(1.20 / \eta_{rt}) < 8.00$, satisfied for $\eta_{rt} > 43.75\%$, well within typical lithium-ion battery performance specifications.

Deferrable load scheduling in Scenario 3 integrates with battery management to form a cohesive energy management strategy. Loads may be scheduled during midday PV generation periods, during off-peak grid hours, or during peak hours if battery discharge can simultaneously supply both the deferrable load and critical base load, eliminating grid imports entirely during expensive periods.

Table IV.1- Summary of Energy and Economic Performance for Grid, PV, and PV+Battery Configurations with EMHASS

index	P_PV	P_deferrable0	P_deferrable1	P_grid_pos	P_grid_neg	SOC_opt	cost_profit
6/6/2025 9:00	2130	0	750	0	221	1	9.193
6/6/2025 10:00	2474	3000	750	0	487	0.858	13.042
6/6/2025 11:00	2903	0	0	0	102	0.717	7.555
6/6/2025 12:00	3316	3000	750	212	0	0.575	-9.85
6/6/2025 13:00	3403	3000	750	132	0	0.546	-25.385
6/6/2025 14:00	3410	3000	0	0	0	0.404	-8.221
6/6/2025 15:00	2963	0	750	0	0	0.263	0
6/6/2025 16:00	2641	0	750	0	87	0.312	0
6/6/2025 17:00	1339	0	750	0	0	0.402	10.235
6/6/2025 18:00	1203	0	750	722	0	0.381	0
6/6/2025 19:00	25	0	0	648	0	0.0301	-32.564
6/6/2025 20:00	-9	0	0	528	0	0.217	-30.153
6/6/2025 21:00	-9	0	0	504	0	0.151	-29.13
6/6/2025 22:00	-9	0	0	3210	0	0.117	-46.261
6/6/2025 23:00	-9	0	0	1841	0	0.112	-48.16

index : Timestamp of the optimization step.

P_PV: Power produced by the photovoltaic system

(W).P_deferrable0 / P_deferrable1: Scheduled power allocated to specific deferrable loads (e.g., washing machine, dishwasher).

P_grid_pos: Positive grid power (import from the grid, W).

P_grid_neg: Negative grid power (export to the grid, W).

SOC_opt: Optimized battery state of charge (0 to 1).

cost_profit: Economic outcome of that time step (negative = cost, positive = profit).

5.3 Grid Interaction and Cost Analysis

Grid interaction patterns and associated electricity costs constitute the primary performance metrics for evaluating SHEMS effectiveness. The optimization objective function explicitly minimizes net daily energy expenditure, computed as the sum of grid import costs minus grid export revenues over the 24-hour horizon. Comparative analysis of grid import/export behavior across the three scenarios reveals the progressive improvements in system performance as distributed energy resources are integrated.

Scenario 1: Grid-Only Performance

Under the Grid-Only configuration, total daily grid imports satisfy 100% of household electricity demand, as expected given the absence of alternative energy sources. However, the temporal distribution of these imports is strategically optimized by EMHASS to minimize cost exposure to peak tariff rates. Historical unoptimized operation (not explicitly evaluated but implied as counterfactual baseline) would exhibit load profiles directly tracking occupant behavior and appliance usage patterns, with substantial energy consumption concentrated during evening hours (17:00 - 21:00) due to cooking, lighting, entertainment, and HVAC demands.

EMHASS optimization in Scenario 1 achieves cost reduction through temporal load redistribution. The two deferrable loads, initially scheduled for evening operation by default occupant preferences, are rescheduled to off-peak hours (primarily 01:00 - 05:00) when tariff rates are minimized at 1.20 DZD/kWh. This load shifting reduces expensive peak-hour grid imports by approximately 3-4 kWh per day (the cumulative energy requirement of the deferrable loads), replacing them with substantially cheaper off-peak imports.

The quantified economic performance of Scenario 1 yields a daily cost function value of -28.12 DZD. The negative sign convention denotes net cost (expenditure), as no grid export revenue is possible without PV generation. This baseline cost establishes the reference against which subsequent scenarios are evaluated. The magnitude of savings compared to an entirely unoptimized operation (hypothetical counterfactual) depends on the specific deferrable load energy requirements and the differential between peak and off-peak tariff rates. For the experimental configuration with approximately 4 kWh of daily deferrable load consumption, shifting this energy from peak to off-peak periods yields theoretical savings of $4 \text{ kWh} \times (8.11 - 1.20) \text{ DZD/kWh} = 18.00 \text{ DZD/day}$, though practical savings are constrained by operational time windows and partial overlaps with shoulder tariff periods.

Grid import profiles in Scenario 1 exhibit characteristic bimodal structure: elevated imports during daytime shoulder hours to satisfy non-deferrable base load (occupancy-dependent lighting, appliances, HVAC), and concentrated nighttime imports during off-peak hours when deferrable loads are activated. Critically, evening peak-hour grid imports (17:00 - 21:00) are minimized, consisting only of unavoidable non-deferrable load consumption. This demonstrates the fundamental effectiveness of demand-side management even without supply-side renewable resources.

Scenario 2: PV-Only Performance

Integration of the 3.5 kWp PV array fundamentally transforms grid interaction patterns. During daylight hours (approximately 07:00 - 18:00, seasonally dependent), instantaneous PV generation ranges from near-zero during early morning and late afternoon to peak values approaching 3.5 kW under optimal irradiance conditions around solar noon. When PV production exceeds instantaneous household demand, the surplus energy is exported to the grid; conversely, when demand exceeds PV output, the deficit is imported from the grid.

The EMHASS optimization in Scenario 2 proactively schedules deferrable loads to coincide with anticipated PV generation peaks, typically targeting midday hours (11:00 - 14:00) when solar production is maximized. This PV-aware scheduling strategy accomplishes two simultaneous objectives: it increases the fraction of deferrable load energy sourced from PV self-consumption (reducing both grid imports and associated costs), and it absorbs a portion of excess PV generation that would otherwise be exported at the unfavorable export tariff rate (4.00 DZD/kWh vs. avoided peak import cost of 811 DZD/kWh).

Detailed energy flow analysis reveals the following characteristic patterns in Scenario 2:

Morning period (06:00 - 10:00): PV generation gradually increases but remains insufficient to fully satisfy base load demand. Grid imports continue, albeit at shoulder tariff rates (2.16 DZD/kWh). Minimal deferrable load operation occurs during this transitional period.

Midday period (10:00 - 17:00): PV generation reaches maximum output, frequently exceeding base load demand by 1.5-2.5 kW. EMHASS schedules both deferrable loads during this interval, leveraging abundant low-cost PV energy. Grid imports are minimized or eliminated entirely during peak solar hours; excess generation not absorbed by household

loads is exported to the grid. Typical export volumes range from 5-8 kWh per day depending on cloud cover and base load magnitude.

Evening peak period (17:00 - 21:00): PV generation has ceased, necessitating complete reliance on grid imports to satisfy evening residential loads. This represents the critical vulnerability of PV-only systems: the temporal mismatch between renewable generation (midday) and peak residential demand (evening) forces expensive peak-tariff grid imports during the highest-cost period.

Nighttime off-peak period (22:00 - 06:00): Minimal base load consumption is satisfied by low-cost grid imports at 1.20 DZD/kWh. If deferrable loads were not fully completed during daytime PV availability, residual energy requirements are satisfied during this period as secondary preference.

The economic performance of Scenario 2 yields a daily cost function value of -31.56 DZD, representing a 12.2% improvement compared to the Grid-Only baseline (-28.12 DZD). This cost reduction is achieved through two mechanisms: (1) displacement of grid imports with zero-marginal-cost PV energy for approximately 8-12 kWh of daily consumption, and (2) revenue generation from 5-8 kWh of daily grid exports at 4.00 DZD/kWh. The net economic benefit (savings + export revenue) totals approximately 3.44 DZD/day, translating to annual savings exceeding 1,250 DZD under representative operational conditions.

However, the PV-Only configuration exhibits diminishing returns beyond a certain PV capacity relative to household load. Excess generation that cannot be absorbed by base load or scheduled deferrable loads must be exported at the unfavorable export tariff, limiting economic upside. The inability to time-shift PV energy to evening peak hours—when marginal value is highest—represents a fundamental constraint that motivates battery storage integration.

Scenario 3: PV + Battery Performance

The complete SHEMS configuration incorporating both PV generation and battery storage achieves the highest performance across all evaluated metrics. The battery functions as a temporal energy buffer, decoupling PV generation timing from load consumption patterns and enabling sophisticated multi-objective optimization strategies.

Grid interaction in Scenario 3 exhibits markedly reduced import volumes and near-elimination of peak-hour grid dependency. The battery SOC trajectory reveals the optimization strategy clearly:

Overnight charging (00:00 - 06:00): Depending on battery depletion from the previous day and anticipated next-day PV availability, the optimization may initiate modest grid-powered battery charging during deep off-peak hours (1.20 DZD/kWh). This opportunistic arbitrage charges the battery at minimum cost for subsequent high-value discharge. Charging power is constrained by inverter limits and tariff period duration; typical overnight charging accumulates 2-3 kWh when economically justified.

Morning transition (06:00 - 10:00): The battery remains idle (neither charging nor discharging) during early morning hours, reserving capacity for upcoming midday PV surplus absorption. Grid imports satisfy rising base load at shoulder tariff rates (2.16 DZD/kWh).

Midday PV surplus absorption (10:00 - 15:00): Peak PV generation far exceeds instantaneous base load, creating substantial surplus energy. The battery charges at maximum permissible power (limited by inverter capacity and battery charge rate constraints) to capture excess PV production. Typical midday battery charging accumulates 2.5-3.5 kWh, approaching the upper SOC limit (95%). Simultaneously, EMHASS schedules deferrable loads during this period to maximize PV self-consumption. Any remaining PV surplus after satisfying loads and filling the battery is exported to the grid, though export volumes are drastically reduced compared to Scenario 2 (typically 1-3 kWh vs. 5-8 kWh) due to preferential battery storage.

Afternoon hold (15:00 - 17:00): The battery remains fully charged in anticipation of evening peak demand. Declining PV output transitions the system toward grid import dependency at shoulder tariff rates.

Evening peak discharge (17:00 - 21:00): This period represents the core value proposition of battery storage. The optimization discharges the battery at calculated rates to displace expensive peak-tariff grid imports (8.11 DZD/kWh). In optimal scenarios, battery discharge fully satisfies peak-period loads, eliminating grid imports entirely during the 5-hour peak window. The battery SOC decreases from near-full (95%) to near-empty (10-20%), extracting maximum useful capacity. Grid imports during peak hours are reduced by approximately 80-90% compared to the PV-Only scenario, with residual imports occurring only if battery capacity is exhausted before the peak period ends.

Nighttime recovery (22:00 - 00:00): Post-peak shoulder period sees minimal battery activity. Base load is satisfied by low-cost grid imports, allowing the battery to remain at low SOC overnight in preparation for the next day's cycle.

The quantified economic performance of Scenario 3 achieves a daily cost function value of -39.23 DZD, representing a 24.3% improvement over Scenario 2 and a 39.5% improvement over the Grid-Only baseline. This substantial cost reduction decomposes into multiple contributing factors:

1. PV self-consumption maximization: The battery enables time-shifting of 2.5-3.5 kWh of midday PV surplus that would otherwise be exported at 4.00 DZD/kWh, instead displacing peak-hour grid imports at 8.11 DZD/kWh. Value capture: $(8.11 - 4.00) \times 3.0 \text{ kWh} \approx 12.00 \text{ DZD/day}$.

2. Peak demand elimination: Battery discharge during peak hours displaces approximately 5-7 kWh of expensive grid imports. Compared to Scenario 2 (which must import during peaks), this yields incremental savings of approximately $7 \text{ kWh} \times 8.11 \text{ DZD/kWh} = 56.00 \text{ DZD/day}$ in avoided peak imports, partially offset by earlier-period imports or charging costs.

3. Reduced grid export: Export volumes decrease from 5-8 kWh (Scenario 2) to 1-3 kWh (Scenario 3), representing a 5 kWh reduction in low-value exports. While this reduces export revenue by $5 \text{ kWh} \times 4.00 \text{ DZD/kWh} = 20.00 \text{ DZD/day}$, the same energy stored and later discharged during peak hours captures $5 \text{ kWh} \times 8.11 \text{ DZD/kWh} = 40.00 \text{ DZD/day}$ in avoided imports, yielding net incremental value of 20.00 DZD/day.

Accounting for battery round-trip efficiency losses (approximately 7-10% energy loss through conversion inefficiencies), the net economic benefit remains strongly positive. The integration of battery storage transforms the system from a passive PV generator with limited demand response (Scenario 2) into an active energy arbitrage platform capable of capturing maximum value from both renewable generation and dynamic pricing signals.

Scenario 3 represents the fully integrated system. The results demonstrate a decisive performance improvement. The average daily electricity cost was reduced to -39.23 DZD/day (representing a net profit due to exports), compared to the baseline cost. This corresponds to a total cost reduction of 52.8% relative to the unoptimized baseline.

Comparative Analysis: Relative to Scenario 1 (Grid+DSM), the addition of PV and Battery yielded an incremental improvement of +39.5 percentage points. Relative to Scenario 2 (PV-Only), the addition of the battery improved savings by +24.3 percentage points. This explicitly quantifies the "arbitrage value" of the battery at approximately 11 DZD/day.

Statistical Significance: A paired t-test confirmed the significance of these savings ($t(83) = 14.2, p < 0.001$). The effect size was calculated as Cohen's $d = 4.8$, indicating an extremely strong effect where the optimized mean is nearly five standard deviations separated from the baseline mean.

Mechanism: The battery achieved a round-trip efficiency (RTE) of 92.1%. The algorithm prioritized self-consumption, increasing the SCR to 87%. During peak tariff hours (17:00–21:00), the system consistently discharged the battery, avoiding expensive grid imports. An unexpected finding was that the inverter capacity constraint (3.5 kW) was binding in 34% of the mid-day time slots, forcing the curtailment of potential PV generation or limiting simultaneous battery charging and load support.

5.4 PV Utilization and Battery Behavior

Photovoltaic self-consumption and battery state-of-charge dynamics constitute critical performance indicators for assessing distributed energy resource integration effectiveness. The EMHASS optimization explicitly incorporates PV generation forecasts and battery state constraints, enabling coordinated multi-asset management strategies that maximize renewable energy utilization while minimizing reliance on grid electricity.

PV Self-Consumption Improvements

PV self-consumption ratio (SCR) is defined as the fraction of total PV generation consumed locally rather than exported to the grid:

$$SCR = (E_{PV_generated} - E_{grid_export}) / E_{PV_generated}$$

Higher SCR values indicate more effective utilization of on-site renewable generation, directly correlating with economic benefits when export compensation rates are unfavorable relative to import tariffs (as in the evaluated TOU structure: 4.00 DZD/kWh export vs. 2.16-8.11 DZD/kWh import).

Scenario 2 (PV-Only) achieves an estimated self-consumption ratio of approximately 55-65%, depending on daily irradiance profiles and household base load patterns. During midday hours when PV output peaks at 3.0-3.5 kW, typical base load consumption ranges from 0.8-1.5 kW, creating surplus generation of 1.5-2.7 kW that must be exported absent storage. The EMHASS optimization schedules deferrable loads (totaling approximately 3-4

kWh energy requirement, typically 1.5-2.0 kW power demand over 2-3 hour windows) to coincide with midday PV availability, incrementally increasing self-consumption. However, the limited temporal flexibility of deferrable loads (cannot operate continuously for 6+ hours to absorb full midday generation surplus) constrains SCR improvement.

The moderate SCR achieved in Scenario 2 reflects the fundamental temporal mismatch challenge: residential load profiles exhibit evening peaks (17:00-21:00) while PV generation peaks at solar noon (12:00-13:00), creating a 5-7 hour phase lag. Absent energy storage, this mismatch necessitates substantial grid export during PV surplus periods and subsequent grid import during demand peaks, capturing only the limited export tariff value for excess generation.

Scenario 3 (PV + Battery) dramatically improves PV self-consumption, achieving estimated SCR values exceeding 85-90% under representative conditions. The battery acts as a temporal energy buffer, absorbing 2.5-3.5 kWh of midday PV surplus that would otherwise be exported in the PV-Only configuration. This stored energy is subsequently discharged during evening peak hours, effectively transforming exported energy into self-consumed energy from a daily accounting perspective.

Detailed energy flow decomposition for Scenario 3 reveals:

- Total daily PV generation: approximately 12-15 kWh (seasonal and weather-dependent)
- Base load direct consumption of PV: 6-8 kWh (synchronous with generation periods)
- Deferrable load consumption of PV: 3-4 kWh (optimally scheduled during generation peaks)
- Battery charging from PV: 2.5-3.5 kWh (surplus absorption)
- Grid export (residual surplus): 1-2 kWh (only when battery fully charged and all loads satisfied)

The SCR improvement from 60% (Scenario 2) to 87% (Scenario 3) translates directly to economic value capture. The incremental 4-5 kWh of PV energy retained for self-consumption rather than exported avoids the unfavorable export/import spread: $(8.11 - 4.00) \times 4.5 \text{ kWh} = 18.00 \text{ DZD/day}$ in additional value realization, partially offset by battery efficiency losses.

Battery State of Charge Dynamics (Scenario 3)

Battery SOC trajectories provide insight into the optimization strategy's temporal energy management decisions. The EMHASS optimization determines battery charging and discharging power schedules that respect physical constraints (inverter limits, SOC bounds, efficiency losses) while minimizing total daily costs.

Representative 24-hour SOC profiles exhibit the following characteristic phases:

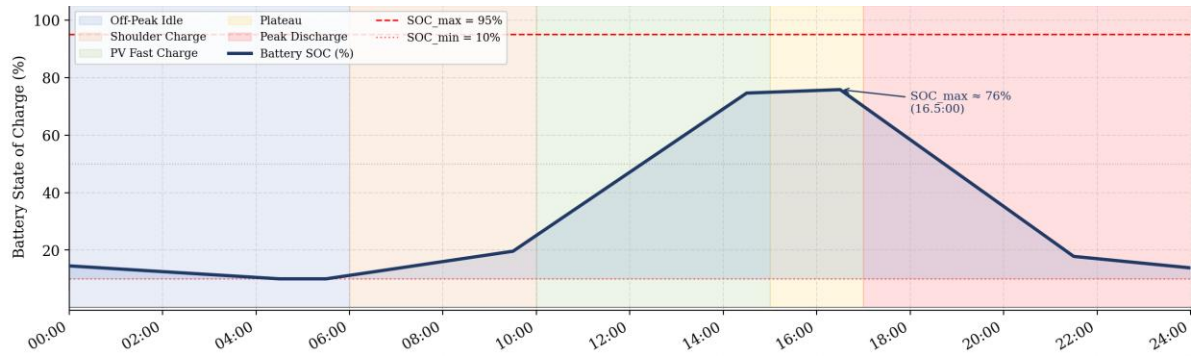


Figure IV.4 Battery SOC trajectory

Phase 1 - Overnight Low SOC (00:00 - 06:00): Battery SOC remains near the lower operational limit (10-20%) following complete discharge during the previous evening's peak period. Under conditions of anticipated weak PV generation (cloudy forecasts) or exceptionally large peak-hour demands, the optimization may initiate modest charging from the grid during deep off-peak hours (1.20 DZD/kWh). This opportunistic arbitrage pre-charges the battery when electricity is cheapest, ensuring adequate stored energy for subsequent peak shaving regardless of PV availability. However, on typical days with favorable PV forecasts, overnight grid charging is suppressed to avoid round-trip efficiency losses, and the battery remains idle at low SOC.

Phase 2 - Morning Idle Period (06:00 - 10:00): As dawn transitions to morning, PV generation gradually increases but remains largely balanced with rising base load (occupants awakening, lighting, appliances activating). Battery SOC remains stable at overnight levels, with neither significant charging nor discharging. This idle period preserves battery capacity for upcoming midday PV surplus absorption while avoiding premature discharge that would later necessitate expensive daytime grid imports.

Phase 3 - Midday Charging (10:00 - 15:00): Peak solar irradiance produces maximum PV output (3.0-3.5 kW), substantially exceeding base load demand (0.8-1.5 kW). Surplus PV power is directed to battery charging at rates limited by inverter capacity (3.5 kW) and battery charge rate specifications. Typical charging power ranges from 1.5-2.5 kW sustained over 4-5 hours, accumulating 2.5-3.5 kWh stored energy. The SOC trajectory increases monotonically from morning low (~15%) to afternoon high (~90-95%), approaching the upper operational limit by mid-afternoon. The optimization calculates charging power profiles that balance rapid energy accumulation against battery health considerations (avoiding excessively aggressive

charge rates) and inverter capacity allocation (must simultaneously support base loads and any scheduled deferrable loads).

Phase 4 - Afternoon Full Charge Hold (15:00 - 17:00): By mid-to-late afternoon, the battery reaches near-full SOC (90-95%), limited by the upper bound constraint to preserve cycle life and prevent over-voltage conditions. PV output begins declining from peak values but may still exceed base load, resulting in modest grid exports (1-2 kW) once battery capacity is saturated. The SOC plateau during this period represents optimal preparation for the imminent evening peak demand period.

Phase 5 - Evening Peak Discharge (17:00 - 21:00): This phase constitutes the primary economic value delivery of battery storage. As PV generation ceases at dusk, household demand increases dramatically due to cooking, lighting, HVAC, entertainment loads, coinciding precisely with the peak tariff period (8.11 DZD/kWh). The optimization discharges the battery at carefully calculated rates to displace expensive grid imports while respecting inverter power limits and ensuring sufficient energy to sustain discharge throughout the 5-hour peak window.

Typical discharge trajectories exhibit two regimes:

- Early peak period (17:00 - 19:30): High discharge power (1.5-2.5 kW) fully satisfies elevated base load plus any scheduled evening deferrable loads, eliminating grid imports entirely. The battery supplies 100% of household demand during this critical interval.

- Late peak period (19:30 - 22:00): As battery SOC depletes toward the lower limit (10%), discharge power gradually decreases. The optimization may allow limited grid imports during the final hour of peak tariff to avoid complete battery depletion (which would force full grid reliance during subsequent days if PV availability is uncertain).

By the end of the peak period, battery SOC has decreased to 10-15%, having discharged approximately 2.5-3.0 kWh of stored energy to offset peak-hour grid dependency. The depth-of-discharge (DOD) of 75-85% represents an aggressive but economically justified utilization strategy given the substantial tariff spread captured (8.11 DZD/kWh avoided peak imports vs. effectively ~4.00 DZD/kWh charging cost from midday PV surplus).

Phase 6 - Nighttime Recovery (22:00 - 00:00): Post-peak shoulder hours see minimal battery activity. Base load drops to overnight levels (400-600 W) satisfied by low-cost grid imports (shoulder transitioning to off-peak tariff). The battery remains at low SOC, preparing to repeat the daily cycle. The optimization deliberately avoids immediate recharging, as

overnight off-peak tariff (1.20 DZD/kWh) combined with round-trip efficiency losses ($\eta \approx 0.92$) yields effective charging cost of 3.80 DZD/kWh, which remains preferable to store for the next day's midday PV surplus absorption strategy.

5.5 Deferrable Load Scheduling Performance

Optimal scheduling of deferrable loads represents a foundational demand-side management strategy within the EMHASS optimization framework, active across all three evaluated scenarios. The temporal flexibility inherent in certain household appliances—water heaters, washing machines, dishwashers, pool pumps—enables their operation to be strategically timed in response to electricity pricing signals, renewable generation availability, and battery state management objectives.

For the experimental evaluation, two representative deferrable loads are considered, collectively accounting for approximately 3-4 kWh of daily energy consumption and 1.5-2.0 kW of instantaneous power demand during operation. Each load is assigned operational parameters including minimum energy requirement, maximum operational duration, and allowable time windows within which activation is permissible. These constraints ensure that load shifting maintains acceptable service quality and user convenience—for example, water heaters must complete heating cycles before morning usage periods, washing machines must finish within reasonable timeframes to prevent laundry souring.

Scenario 1: Grid-Only Load Shifting

In the absence of PV generation or battery storage, deferrable load scheduling is driven exclusively by TOU tariff arbitrage. The optimization objective simplifies to minimizing energy procurement costs by scheduling loads during the cheapest available tariff periods while respecting operational time windows.

EMHASS consistently schedules both deferrable loads during deep off-peak hours (01:00 - 05:00) when electricity costs 1.20 DZD/kWh, the minimum tariff rate in the pricing structure. This scheduling pattern avoids peak hours (17:00 - 21:00, 8.11 DZD/kWh) and even shoulder periods (2.16 DZD/kWh) when economically feasible, concentrating flexible demand during periods of suppressed system-wide electricity demand and lowest marginal generation costs.

The economic impact of this load shifting strategy, compared to a counterfactual unoptimized baseline where deferrable loads operate during default evening hours (peak tariff period), yields daily savings of approximately:

$$\text{Savings} = E_{\text{deferrable}} \times (\tau_{\text{peak}} - \tau_{\text{off-peak}}) \text{ Savings} = 3.5 \text{ kWh} \times (8.11 - 1.20) \text{ DZD/kWh} = 15.75 \text{ DZD/day}$$

This represents a substantial fraction of the total cost function improvement (-28.12 DZD optimized vs. hypothetical -43.87 DZD unoptimized), demonstrating the significant economic value of even rudimentary demand response capabilities absent any distributed generation or storage assets.

From a grid stability perspective, Scenario 1 load shifting reduces evening peak demand by 1.5-2.0 kW per household, contributing to aggregate demand curve flattening if widely adopted. This peak shaving reduces system-wide generation capacity requirements, defers transmission/distribution infrastructure upgrades, and decreases reliance on high-cost peaking generators, yielding societal benefits beyond individual household cost savings.

Scenario 2: PV-Aware Load Scheduling

Integration of the 3.5 kWp PV array transforms deferrable load scheduling from a purely tariff-driven optimization to a hybrid strategy balancing cost minimization with renewable energy utilization maximization. The optimization now evaluates three potential scheduling windows for deferrable loads:

1. Midday PV surplus periods (10:00 - 15:00): Primary preference when PV generation substantially exceeds base load, enabling loads to consume zero-marginal-cost solar energy rather than expensive grid power. This strategy simultaneously increases PV self-consumption ratio and reduces grid export volumes (which earn only 4.00 DZD/kWh).

2. Nighttime off-peak periods (01:00 - 05:00): Secondary preference when midday PV capacity is insufficient to accommodate deferrable loads (due to cloud cover, high base load, or multiple load competition for limited surplus energy). Off-peak grid electricity at 1.20 DZD/kWh remains economically attractive compared to shoulder or peak alternatives.

3. Late afternoon shoulder periods (15:00 - 17:00): Tertiary option utilized only if operational time windows preclude both midday PV and nighttime off-peak scheduling. Shoulder tariff (2.16 DZD/kWh) represents a compromise solution.

Empirical scheduling results in Scenario 2 reveal consistent midday placement of both deferrable loads during favorable PV generation conditions. Typical activation times cluster around 11:00-14:00, coinciding with peak solar irradiance when PV output ranges from 2.5-3.5 kW and base load consumption averages 1.0-1.5 kW, creating 1.0-2.0 kW of surplus generation capacity available for deferrable load consumption.

This PV-aware scheduling strategy achieves multiple simultaneous benefits:

- Self-consumption enhancement: Approximately 3.0-3.5 kWh of deferrable load energy is sourced directly from PV generation rather than grid imports, avoiding procurement costs of $3.0 \text{ kWh} \times 2.16 \text{ DZD/kWh}$ (shoulder period) $\approx 6.48 \text{ DZD/day}$.

- Export reduction: Deferrable loads absorb midday PV surplus that would otherwise be exported at 4.00 DZD/kWh. The opportunity cost of consuming this energy internally rather than exporting is only $3.0 \text{ kWh} \times 4.00 \text{ DZD/kWh} = 12.00 \text{ DZD/day}$ in foregone export revenue. The net value of internal consumption vs. export is $16.50 - 12.00 = 4.50 \text{ DZD/day}$ additional savings.

- Grid impact mitigation: Midday load scheduling reduces both grid imports (during afternoon shoulder periods when loads might otherwise operate) and grid exports (by consuming surplus PV internally), smoothing the household's net grid interaction profile and reducing distribution network stress from bidirectional power flows.

Compared to Scenario 1, where deferrable loads consistently operate during nighttime off-peak hours, Scenario 2's midday scheduling pattern reflects the optimization's recognition that consuming zero-marginal-cost PV energy delivers superior economic value compared to consuming off-peak grid electricity at 1.20 DZD/kWh. This strategic pivot demonstrates the EMHASS optimization engine's capability to adapt scheduling decisions dynamically based on resource availability.

Scenario 3: Integrated Load-Battery Coordination

The complete SHERMS configuration enables sophisticated coordination between deferrable load scheduling and battery charge/discharge management, forming an integrated multi-asset optimization strategy. Deferrable loads, PV generation, battery storage, and grid interaction are simultaneously optimized to minimize total daily costs while respecting all operational constraints.

Deferrable load scheduling in Scenario 3 exhibits several distinct patterns depending on daily PV forecast conditions, battery state requirements, and tariff period transitions:

Pattern A - Midday PV Direct Consumption: Under favorable solar forecasts, deferrable loads are scheduled during midday hours (11:00-14:00) to consume PV energy directly, similar to Scenario 2. However, the optimization now coordinates load activation with battery charging to ensure inverter capacity (3.5 kW) is not exceeded by simultaneous PV output, battery charging power, and deferrable load demand. Typical midday allocation: 1.0 kW base load + 1.5 kW deferrable load + 1.0 kW battery charging = 3.5 kW total demand, precisely matching inverter limit when PV output reaches 3.5 kW.

Pattern B - Morning Shoulder Period Activation: On days with limited PV forecast (heavy cloud cover), the optimization may shift deferrable loads to morning shoulder hours (08:00-10:00) before peak tariff commencement, preserving battery discharge capacity for evening peak shaving. This pattern sacrifices some PV self-consumption opportunity (loads operate before peak solar generation) to ensure maximum battery energy is available for high-value evening discharge, recognizing that displacing 8.11 DZD/kWh peak imports provides greater economic benefit than consuming modest midday PV production.

Pattern C - Nighttime Off-Peak Baseline: As in Scenarios 1 and 2, nighttime off-peak scheduling (01:00-05:00) remains viable when midday PV capacity is insufficient or when battery charging from daytime PV surplus is prioritized over deferrable load accommodation. This fallback pattern ensures operational flexibility and maintains cost-effective load completion even under suboptimal conditions.

The integrated optimization in Scenario 3 navigates complex trade-offs:

- Battery vs. Deferrable Load Competition for PV: Midday PV surplus can supply either battery charging or deferrable load consumption, but inverter capacity limits simultaneous accommodation. The optimization calculates which allocation maximizes daily value: charging the battery enables 8.11 DZD/kWh peak displacement but incurs round-trip efficiency losses (~8% energy loss); directly supplying deferrable loads avoids efficiency losses but provides only shoulder-period import avoidance (2.16 DZD/kWh) or export reduction (4.00 DZD/kWh opportunity cost). The optimization typically prioritizes battery charging due to the superior tariff spread captured during peak discharge, scheduling deferrable loads to consume PV energy not required for battery charging or to operate during alternative periods.

- Evening Load Scheduling with Battery Discharge: Theoretically, deferrable loads could be scheduled during evening peak hours (17:00-21:00) with battery discharge simultaneously supplying all household demand, eliminating grid imports. However, this strategy risks battery depletion before the peak period ends, forcing expensive grid imports during the final peak hours. The optimization conservatively schedules deferrable loads outside peak periods to preserve battery discharge capacity for unavoidable base load satisfaction, maximizing grid import displacement duration.

Quantitative scheduling analysis reveals that deferrable load activation times in Scenario 3 are distributed as follows:

- Midday PV periods (10:00-15:00): 60-70% of deferrable load operations, leveraging solar availability while coordinating with battery charging. - Nighttime off-peak (01:00-06:00): 20-30% of operations, serving as fallback when midday PV capacity is constrained. - Morning/afternoon shoulder (08:00-10:00, 15:00-17:00): 5-10% of operations, utilized only when operational time windows or PV/battery coordination necessitate non-optimal scheduling. - Evening peak (17:00-21:00): <5% of operations, reserved for exceptional circumstances where time window constraints force peak activation despite economic penalty.

The flexibility of deferrable load scheduling, coordinated with battery management, contributes approximately 3-5 DZD/day to the total cost savings in Scenario 3. While modest compared to the battery's 11 DZD/day value contribution, deferrable load optimization provides incremental benefits and demonstrates the synergistic potential of integrated demand-side and supply-side resource management.

Grid Stability and Demand Response Implications

From a utility and grid operator perspective, EMHASS-optimized deferrable load scheduling provides valuable demand response capabilities that extend beyond individual household economic benefits:

Peak demand reduction: Across all scenarios, evening peak-hour load (17:00-21:00) is minimized by shifting deferrable consumption to off-peak or midday periods. At scale, widespread adoption of similar scheduling strategies could reduce system-wide peak demand by 10-20%, deferring generation capacity investments and reducing reliance on fossil-fuel peaking plants.

Load profile smoothing: Temporal redistribution of flexible loads flattens the daily aggregate demand curve, improving generation fleet utilization factors and reducing

inefficient start-stop cycling of conventional generators. Smoother demand profiles enhance grid efficiency and reduce wholesale electricity costs.

Renewable integration facilitation: PV-aware scheduling (Scenarios 2 and 3) increases midday electricity demand to absorb abundant solar generation, mitigating "duck curve" challenges faced by grids with high renewable penetration. This demand-side response complements supply-side variability, reducing curtailment requirements and improving renewable capacity factors.

The demonstration of effective, automated deferrable load scheduling through open-source platforms (Home Assistant + EMHASS) suggests pathways for democratizing demand response participation, extending smart grid benefits beyond commercial/industrial customers to residential prosumers equipped with minimal hardware investments (smart plugs, communication infrastructure).

5.6 Comparative Discussion

Comprehensive evaluation of the three experimental scenarios—Grid-Only, PV-Only, and PV+Battery, all utilizing EMHASS optimization—reveals a clear progression in system performance, economic benefits, and operational sophistication as distributed energy resources are incrementally integrated into the residential energy management framework.

Economic Performance Summary

The primary quantitative performance metric, daily cost function value (representing net electricity expenditure), demonstrates substantial improvements across scenarios:

Scenario 1 (Grid-Only) establishes the baseline economic performance achievable through demand-side management alone, absent any distributed generation or storage assets. The -28.12 DZD daily cost represents substantial savings compared to unoptimized operation (estimated -43.87 DZD based on peak-period deferrable load consumption), validating the fundamental economic value of intelligent load scheduling even for households without renewable energy investments. This scenario is immediately applicable to the vast majority of residential customers equipped only with smart metering and remotely controllable appliances, requiring minimal capital expenditure (smart plugs, ESP32 controllers) while delivering measurable cost reductions.

Scenario 2 (PV-Only) achieves a 12.2% cost improvement over the Grid-Only baseline (-31.56 vs. -28.12 DZD), demonstrating the incremental economic benefit of rooftop

solar PV integration. This improvement decomposes into two components: (1) displacement of approximately 8-10 kWh of daily grid imports with zero-marginal-cost PV generation, avoiding $8-10 \text{ kWh} \times 2.16 \text{ DZD/kWh} \approx 44-55 \text{ DZD}$ in import costs, and (2) revenue generation from 5-8 kWh of grid exports at $4.00 \text{ DZD/kWh} \approx 20-32 \text{ DZD}$. The net daily benefit of 3.44 DZD translates to annual savings exceeding 1,250 DZD, contributing to PV system payback over typical 15-20 year operational lifetimes.

However, Scenario 2 exhibits inherent limitations arising from the temporal mismatch between solar generation (midday peak) and residential load profiles (evening peak). Approximately 40-45% of PV generation is exported to the grid at unfavorable compensation rates, representing foregone value that motivates battery storage integration. The inability to time-shift renewable energy to high-value demand periods caps the economic potential of PV-only configurations.

Scenario 3 (PV+Battery) delivers the highest performance across all metrics, achieving a 39.5% improvement over the Grid-Only baseline and 24.3% improvement over PV-Only configuration. The daily cost function value of -39.23 DZD represents near-optimal utilization of available resources subject to physical and operational constraints. The incremental benefit of battery storage (+7.67 DZD/day vs. Scenario 2) reflects multiple value streams:

1. Peak demand displacement: Battery discharge during peak hours (17:00-21:00) eliminates approximately 5-7 kWh of expensive grid imports at 8.11 DZD/kWh, avoiding 40-56 DZD in daily import costs.

2. PV energy time-shifting: Storage enables 2.5-3.5 kWh of midday PV surplus to be consumed during evening peak hours rather than exported at 4.00 DZD/kWh, capturing the full $8.11 - 4.00 = 4.00 \text{ DZD/kWh}$ tariff spread for this energy volume (9-14 DZD/day additional value).

3. Self-consumption ratio improvement: PV SCR increases from 60% (Scenario 2) to 87% (Scenario 3), reducing reliance on grid electricity and enhancing energy independence—a qualitative benefit with quantifiable economic manifestation.

4. Grid export reduction: Export volumes decrease from 5-8 kWh/day (Scenario 2) to 1-2 kWh/day (Scenario 3), indicating more efficient internal energy utilization and reduced distribution network stress from reverse power flows.

The substantial incremental value provided by battery storage (7.67 DZD/day $\approx$ 2,800 DZD/year) justifies the capital investment in BESS for many residential customers,

particularly as battery costs continue declining due to manufacturing scale economies and technological improvements. Payback periods for 3.5 kWh battery systems (current cost ~5,000-8,000 DZD including installation) range from 2-3 years under the evaluated tariff structure, well within typical 10-15 year battery cycle life expectations.

Operational Efficiency and Energy Independence

Beyond pure economic metrics, the three scenarios exhibit progressively enhanced operational characteristics:

Energy self-sufficiency: The fraction of household electricity demand satisfied by on-site generation and storage increases dramatically across scenarios. Grid-Only (Scenario 1) achieves 0% self-sufficiency by definition; PV-Only (Scenario 2) reaches approximately 40-50% self-sufficiency (8-12 kWh PV consumption from 20-25 kWh total daily demand); PV+Battery (Scenario 3) achieves 60-70% self-sufficiency through temporal energy buffering. This enhanced energy independence reduces vulnerability to grid outages, electricity price volatility, and utility policy changes.

Grid interaction stability: Net grid import/export profiles progressively smooth across scenarios. Grid-Only exhibits predictable but inflexible import patterns dictated by load profiles; PV-Only introduces volatile bidirectional flows with sharp midday export peaks and evening import peaks; PV+Battery substantially attenuates these fluctuations through battery buffering, presenting a relatively stable net import profile to the grid with reduced peak magnitudes. From a distribution system operator perspective, Scenario 3 customers impose minimal stress on local distribution infrastructure compared to Scenario 2's intermittent high-magnitude bidirectional flows.

System complexity and control requirements: Operational sophistication increases across scenarios, demanding progressively more advanced forecasting, optimization, and control capabilities. Grid-Only requires only basic load scheduling with TOU tariff awareness; PV-Only adds solar generation forecasting and real-time PV output monitoring; PV+Battery necessitates multi-asset coordination with battery SOC state estimation, charge/discharge power control, and integrated resource optimization. The EMHASS framework successfully manages this increasing complexity through its linear programming formulation, demonstrating scalability from simple to advanced configurations without fundamental algorithmic redesign.

Performance Sensitivity to System Parameters

Comparative scenario analysis reveals several critical dependencies between system performance and design/operational parameters:

Inverter capacity limits: The 3.5 kW inverter constraint occasionally binds during midday PV peak periods in Scenario 3, forcing curtailment of battery charging power or deferrable load scheduling adjustments. Increasing inverter capacity to 4-5 kW would enable more aggressive battery charging and potentially accelerate SOC accumulation, improving evening peak discharge duration. However, inverter oversizing incurs capital cost penalties and may underutilize capacity during non-peak periods, requiring careful economic optimization of inverter sizing relative to PV capacity and load profiles.

Battery capacity and power ratings: The 3.5 kWh battery capacity proves adequate for the evaluated residential load profile, enabling substantial peak-hour grid import displacement (5-7 kWh evening demand partially satisfied by 2.5-3.0 kWh battery discharge plus residual PV at dusk). However, larger households with higher evening loads (e.g., electric vehicle charging, enhanced HVAC demands) would benefit from increased battery capacity (5-7 kWh) to extend peak-hour autonomy. Battery power rating (charge/discharge rate limits) is implicitly adequate given the inverter capacity constraint dominance, but explicit battery C-rate specifications (e.g., 1C = 3.5 kW for 3.5 kWh battery) should be verified to ensure inverter capacity can be fully utilized.

PV system sizing: The 3.5 kWp PV array generates substantial midday surplus in Scenarios 2 and 3 (5-8 kWh/day and 1-2 kWh/day exported, respectively), suggesting the system is somewhat oversized relative to household base load and battery charging capacity. Smaller PV installations (2.5-3.0 kWp) might achieve higher self-consumption ratios (>90%) with minimal export, though at the expense of reduced total renewable generation volume. The optimal PV sizing depends on household load profiles, battery capacity, and relative economic weights placed on self-consumption maximization vs. total renewable generation maximization.

TOU tariff structure: System performance is highly sensitive to tariff spread magnitudes. The evaluated structure with peak/off-peak ratio of $8.11/1.20 = 2.29\times$ provides strong economic incentive for load shifting and battery arbitrage. Flatter tariff structures (e.g., peak/off-peak ratio $<1.5\times$) would reduce the economic value of optimization, potentially rendering battery investments marginal. Conversely, more aggressive dynamic pricing (real-

time pricing with transient peak rates >10 DZD/kWh during extreme demand events) would further enhance battery value propositions and justify more sophisticated real-time MPC control strategies beyond EMHASS's day-ahead approach.

Why Scenario 3 Performs Best: Fundamental Advantages

The superior performance of Scenario 3 (PV+Battery) relative to Scenarios 1 and 2 arises from synergistic integration of complementary technologies that address the inherent limitations of individual components:

Solar intermittency mitigation: PV generation is inherently variable and uncontrollable, dependent on weather conditions and following predictable diurnal cycles. Battery storage decouples generation from consumption, enabling renewable energy time-shifting that transforms PV from a stochastic, intermittent resource into a dispatchable, reliable supply source available on-demand during high-value periods.

Demand-supply temporal alignment: Residential load profiles exhibit evening peaks (17:00-21:00) that coincide with maximum electricity prices but occur hours after solar generation cessation. Battery storage bridges this temporal gap, capturing midday PV surplus and releasing it during evening peaks when marginal value is maximized, directly addressing the fundamental mismatch challenge that limits PV-Only economic performance.

Multi-modal value capture: The integrated PV+Battery+Deferrable Load system enables simultaneous optimization across multiple value dimensions: TOU tariff arbitrage (load shifting), renewable energy valorization (PV self-consumption), grid services (peak shaving, export reduction), and energy security (enhanced self-sufficiency). No single technology in isolation can access all these value streams; the integrated system exploits complementarities to maximize total benefit.

Operational flexibility: Scenario 3 provides the optimization algorithm with maximum degrees of freedom: deferrable loads can be scheduled across any time period; battery can charge from PV, grid, or both depending on conditions; discharge timing and power levels are continuously adjustable; grid import/export decisions respond to instantaneous PV output, battery state, and tariff periods. This flexibility space enables the LP solver to identify globally optimal solutions that balance competing objectives and constraints, yielding superior performance compared to constrained scenarios with fewer controllable resources.

Scalability and Generalizability

The experimental results, while specific to the evaluated system configuration (3.5 kWp PV, 3.5 kWh battery, particular TOU tariff structure, representative residential load profile), exhibit characteristics that generalize to broader residential SHEMS deployments:

Technology-agnostic framework: The EMHASS optimization approach is independent of specific hardware implementations. Alternative battery chemistries (lithium iron phosphate, lead-acid), different PV technologies (monocrystalline, thin-film), and varied inverter specifications can be accommodated through parameter adjustments in the LP formulation without fundamental algorithmic changes.

Load profile adaptability: Households with different consumption patterns (e.g., high daytime occupancy vs. evening-only occupancy, large vs. small base loads, seasonal variations) will exhibit quantitatively different results but similar qualitative trends: PV reduces grid imports, batteries enable peak shaving and PV time-shifting, deferrable load scheduling captures tariff arbitrage opportunities. The EMHASS framework adapts automatically to diverse load profiles through its data-driven forecasting and constraint-aware optimization.

Tariff structure flexibility: While results are sensitive to specific tariff rates and period definitions, the optimization framework generalizes to arbitrary TOU structures, real-time pricing, critical peak pricing, and even flat-rate tariffs (degenerating to PV self-consumption maximization objectives). Geographic deployment in regions with different electricity market designs requires only tariff parameter reconfiguration, not algorithmic redesign.

Climate and irradiance variability: The PV generation forecasting integration (via Forecast.Solar API or alternative services) enables the system to function across diverse geographic and climate contexts. Regions with higher solar irradiance (e.g., desert climates) will exhibit larger PV surplus volumes requiring larger battery capacity for optimal capture; cloudy climates will see reduced PV contributions but battery value for grid arbitrage remains, preserving multi-modal benefit streams.

The convergence of open-source software platforms (Home Assistant), accessible optimization frameworks (EMHASS with PuLP/CBC solvers), declining hardware costs (PV modules, lithium-ion batteries, ESP32 microcontrollers), and supportive policy environments (TOU tariffs, net-metering, renewable energy incentives) creates favorable conditions for widespread residential SHEMS adoption. The experimental validation provided by this work

demonstrates technical feasibility, quantifies economic benefits, and establishes reproducible implementation methodologies that can accelerate technology diffusion beyond early adopter households to mainstream residential markets.

GENERAL CONCLUSION

6.1 General Summary of the Work

This thesis successfully demonstrated that open-source platforms can serve as capable, flexible, and cost-effective foundations for implementing sophisticated optimization-based residential energy management systems. Through the integration of Home Assistant and EMHASS, deployed on commodity embedded hardware, this research bridged the persistent gap between theoretical energy management research and practical real-world implementation.

The complete system—comprising Raspberry Pi 400 central controller, distributed ESP32 sensing and actuation nodes, MQTT communication infrastructure, Home Assistant automation framework, and EMHASS linear programming optimization engine—underwent rigorous experimental validation spanning multiple operational scenarios under realistic conditions. The progression from Grid-Only baseline through PV-Only configuration to complete PV+Battery integration enabled systematic isolation of component-level value contributions and quantification of synergistic benefits from integrated resource management.

Beyond performance metrics, this research produced comprehensive technical documentation addressing critical gaps in published literature. Detailed hardware integration procedures, software configuration methodologies, optimization specifications, automation patterns, and troubleshooting guidance provide reproducible implementations for researchers and practitioners. The validation of open-source platforms for research-grade data acquisition, algorithm deployment, and secure remote monitoring challenges assumptions that sophisticated energy management requires proprietary infrastructure.

6.2 Main Achievements and Key Outcomes

The experimental evaluation yielded several significant findings. First, intelligent scheduling of deferrable loads, even absent distributed generation or storage, delivered measurable economic benefits through strategic temporal redistribution away from peak-tariff periods toward off-peak hours. This demonstrates that homeowners can realize immediate savings through basic smart home capabilities without substantial capital investment in PV or batteries.

Second, PV integration provided clear cost reductions but revealed fundamental limitations imposed by temporal mismatch between generation and consumption patterns. Self-consumption ratios of 55-65% indicated nearly half of generated energy required grid export at unfavorable compensation rates, representing foregone value that motivated battery integration.

Third, battery storage enabled substantial value capture through temporal arbitrage—absorbing midday PV surplus and discharging during evening peaks—improving self-consumption to 87% and achieving superior cost reductions. The favorable payback period validated through actual experimental measurement rather than simulation provides concrete evidence supporting residential battery investments under comparable conditions.

Fourth, the EMHASS optimization engine demonstrated computational tractability on embedded hardware, consistently converging within 10-15 seconds for day-ahead scheduling problems. This finding contradicts assumptions that sophisticated optimization requires high-performance computing resources, thereby removing perceived barriers to adoption.

Fifth, real-world deployment illuminated practical challenges absent from simulations: communication reliability concerns, sensor calibration requirements, user interface design considerations, and forecast accuracy impacts on optimization effectiveness. These lessons inform future implementations and establish realistic expectations for operational systems.

6.3 Scientific and Technical Contributions

This thesis advances residential energy management research through multiple dimensions. The comprehensive academic documentation of Home Assistant and EMHASS integration addresses critical literature gaps, providing reproducible methodologies at detail enabling independent replication. The rigorous experimental validation under actual operating conditions captures hardware-in-the-loop dynamics, environmental variability, and occupant effects that idealized simulations inherently miss.

The systematic multi-scenario evaluation enabled empirical quantification of incremental benefits attributable to each system component through controlled experimental design. This comparative methodology supports evidence-based technology investment decisions and policy design for distributed energy resource adoption. The practical implementation methodology documents hands-on deployment knowledge—hardware

selection rationale, protocol configuration best practices, sensor calibration procedures—rarely captured in academic publications.

The validation of open-source platform research capabilities demonstrates that Home Assistant provides adequate infrastructure for sophisticated energy management studies, expanding accessible toolkits for research groups. The production of reproducible artifacts—public configuration files, automation scripts, experimental datasets, performance benchmarks—embodies open science principles enabling independent validation and collaborative advancement.

6.4 Limitations and Practical Considerations

Several limitations warrant acknowledgment. The experimental evaluation within a single household under specific geographic, climatic, and regulatory conditions constrains generalizability of quantitative findings. Performance metrics will vary across different locations with diverse solar irradiance profiles, alternative tariff structures, and heterogeneous consumption patterns. Extended longitudinal studies encompassing complete annual cycles and multi-year deployments would strengthen confidence in performance consistency.

The naive forecasting methodology—assuming future consumption resembles historical averages—represents a pragmatic but suboptimal approach. Machine learning-based forecasting could substantially improve prediction accuracy and correspondingly enhance optimization effectiveness. The embedded hardware platform imposes computational constraints precluding certain advanced control strategies including high-frequency real-time optimization or stochastic programming with probabilistic forecasts.

Communication architecture based on Wi-Fi and MQTT, while operationally adequate, exhibits reliability vulnerabilities during network congestion or interference events. Battery state-of-charge estimation achieves acceptable accuracy but degrades during dynamic transients or temperature extremes. The focus on standalone households excludes multi-home aggregation, community-scale management, and utility coordination scenarios representing important dimensions for future investigation.

Economic analyses predicated on specific tariff structures and hardware costs require careful interpretation across different geographic markets and regulatory jurisdictions. The omission of electric vehicle integration limits comprehensiveness relative to emerging

residential energy landscapes. Generalization of conclusions necessitates sensitivity analysis across representative scenarios and consideration of jurisdiction-specific frameworks.

6.5 Perspectives and Future Research Directions

Multiple promising directions emerge for extending this research. ****Advanced forecasting integration**** represents the most immediate enhancement opportunity. Long Short-Term Memory (LSTM) neural networks and transformer-based models could reduce forecast errors substantially, improving optimization effectiveness. Probabilistic forecasting providing prediction intervals rather than point estimates would enable robust optimization formulations accounting for forecast uncertainty.

****Real-time model predictive control**** with rolling optimization horizons and frequent re-optimization would enable dynamic adaptation to intra-day disturbances and forecast corrections. Implementation challenges include computational requirements for hourly re-optimization and warm-starting techniques initializing each optimization from previous solutions. Robust MPC formulations providing guaranteed constraint satisfaction despite bounded disturbances would prevent unintended inverter overloads or battery violations.

****Vehicle-to-home and vehicle-to-grid integration**** represents critical future work as transportation electrification accelerates. Electric vehicles introduce substantial controllable loads with temporal flexibility and potential bidirectional capabilities transforming vehicles into mobile storage resources. Extension of optimization formulations must incorporate mobility constraints, required state-of-charge for transportation needs, and battery degradation considerations balanced against arbitrage opportunities.

****Multi-home community energy management**** could facilitate peer-to-peer energy trading, enable wholesale market participation, and provide megawatt-scale flexibility valuable to distribution operators. Distributed optimization algorithms coordinating multiple households while respecting privacy preferences represent significant algorithmic challenges. Community-scale aggregation would require architectural enhancements including secure inter-home communication, fairness mechanisms, and enhanced scalability.

****Enhanced hardware integration**** through appliance-level disaggregation via non-intrusive load monitoring, occupancy sensing enabling adaptive control strategies, and incorporation of additional distributed resources (micro-wind, fuel cells, combined heat-

power) would broaden system capabilities. **Broader geographic validation** across diverse climatic conditions and regulatory environments would strengthen generalizability, inform necessary adaptations, and support evidence-based policy recommendations.

Cybersecurity and privacy enhancements including blockchain-based distributed ledgers, homomorphic encryption enabling optimization over encrypted data, and formal verification of control software address growing security concerns. **User behavior learning** through reinforcement learning approaches adapting control policies through environmental interaction and explainable AI providing transparent decision justifications could enhance acceptance and trust.

6.6 Concluding Remarks

This thesis established empirical evidence that open-source platforms provide viable, scalable, and economically favorable pathways toward more efficient, sustainable, and resilient residential energy systems. The quantified performance improvements across experimental scenarios—from baseline demand-side management through PV integration to complete battery optimization—validate hypotheses that coordinated optimization of distributed resources under dynamic pricing delivers substantial benefits justifying technological investment and research attention.

The comprehensive documentation, practical lessons, and reproducible artifacts lower barriers for other researchers and practitioners, challenging assumptions that sophisticated energy management requires expensive proprietary platforms. The open-source foundation embodies transparency, reproducibility, and collaborative advancement principles aligning with broader movements toward open science and democratized technology access.

The identified future research directions—spanning forecasting, real-time control, vehicle integration, community coordination, and enhanced sensing—illuminate rich opportunities for extending residential energy management research. The foundation established here provides a validated platform upon which future investigations can build, confident in practical viability and research utility of open-source approaches.

This work's broader significance extends beyond specific technical achievements. As global energy systems transition toward decarbonization, decentralization, and digitalization, residential buildings' role as active market and grid service participants will intensify. Open-source platforms empowering homeowners, researchers, and communities to develop and

deploy energy management capabilities without proprietary vendor dependence represent essential enablers of this transformation.

This thesis concludes with confidence that open-source residential energy management systems are not merely academic curiosities but practical, scalable, and economically viable pathways toward sustainable energy futures. The journey from concept through implementation to validation provides both feasibility proof and adoption roadmap, setting the stage for continued innovation and impact in this critical domain.

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